

Formal Methods Update Meeting 2022

# Equivalence Checking as the Backbone of Compiler Development

Sorav Bansal

IIT Delhi and CompilerAI Labs

Joint work with Alex Aiken, Manjeet Dahiya, Shubhani, Abhishek Rose  
and several other past members of our research group

# Ten Algorithms with the greatest influence on science and engg. in the 20th century

- the Metropolis algorithm for Monte Carlo
- the simplex method for linear programming
- Krylov subspace iteration methods
- the decompositional approach to matrix computations
- the Fortran optimizing compiler
- the QR algorithm for computing eigenvalues
- the quicksort algorithm for sorting
- the fast Fourier transform
- integer relation detection
- the fast multipole method

Guest editors of IEEE Computing in Science & Engineering 2000

# Ten Algorithms with the greatest influence on science and engg. in the 20th century

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# The Fortran Optimizing Compiler

**1957:** John Backus leads a team at IBM in developing the **Fortran optimizing compiler**.

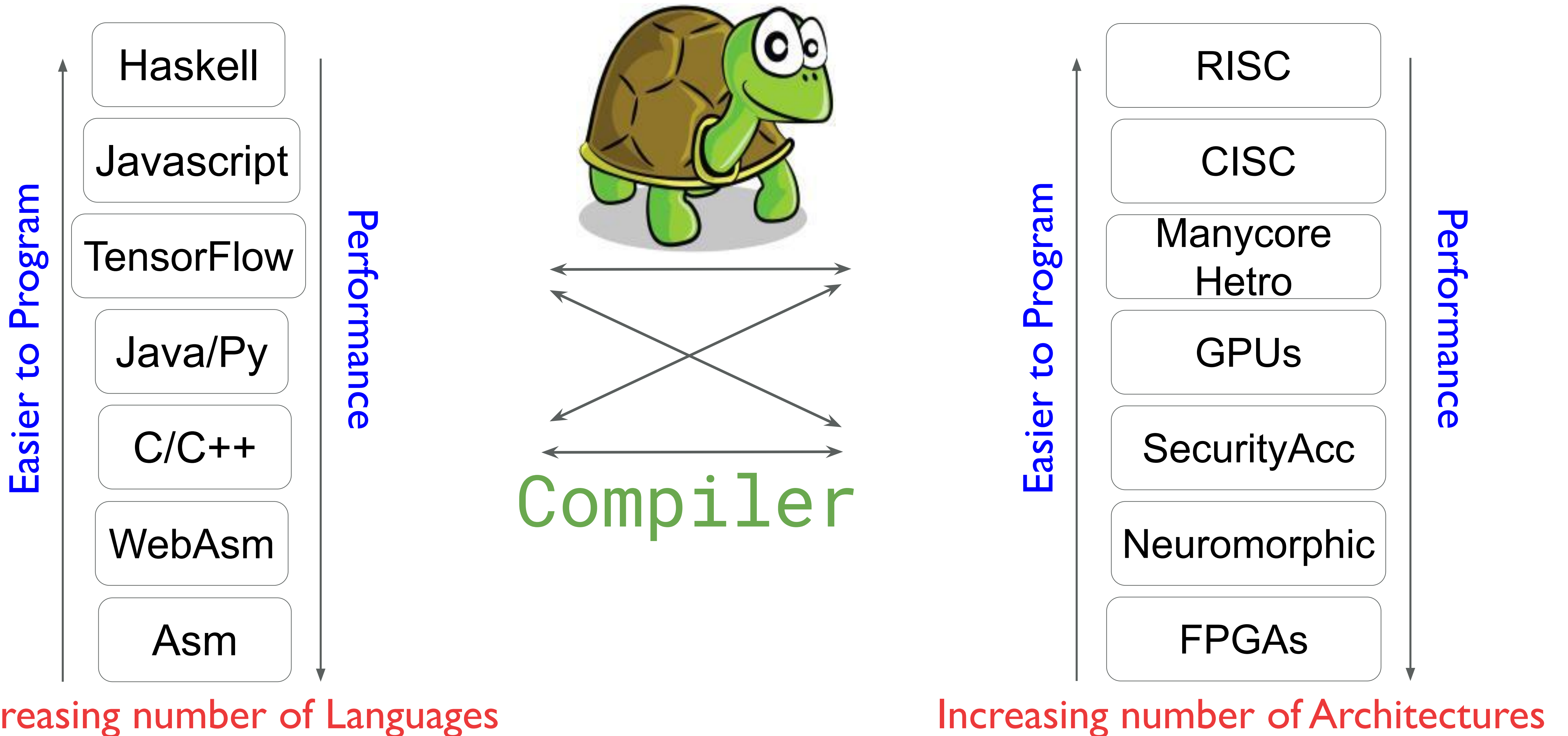
The creation of Fortran may rank as the single most important event in the history of computer programming: Finally, scientists

---

(and others) could tell the computer what they wanted it to do, without having to descend into the netherworld of machine code. Although modest by modern compiler standards—Fortran I consisted of a mere 23,500 assembly-language instructions—the early compiler was nonetheless capable of surprisingly sophisticated computations. As Backus himself recalls in a recent history of Fortran I, II, and III, published in 1998 in the *IEEE Annals of the History of Computing*, the compiler “produced code of such efficiency that its output would startle the programmers who studied it.”

Guest editors of *IEEE Computing in Science & Engineering* 2000

# End of Moore's Law will see...





# Architects and Compilers



Compilers



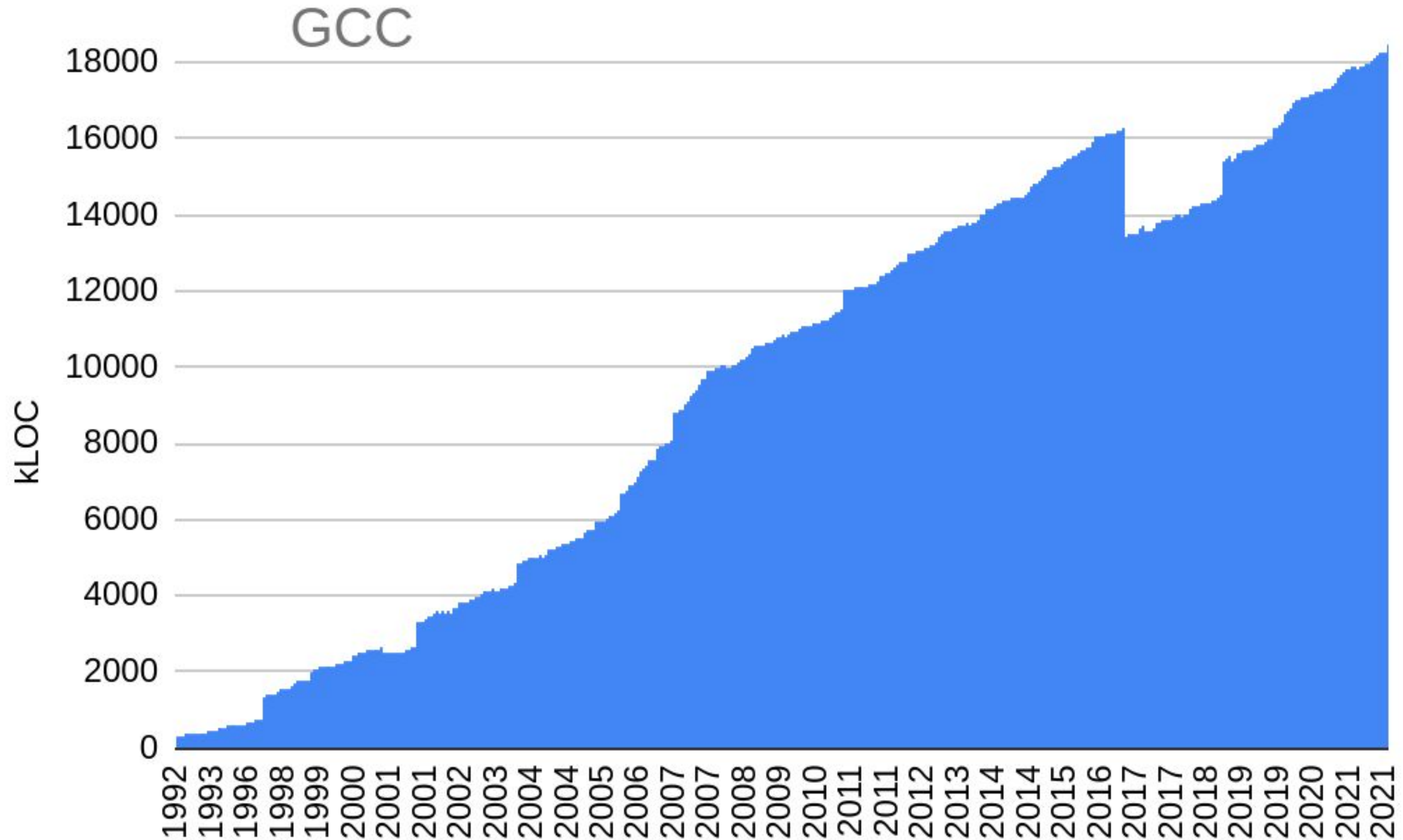
Architects

Image sources:

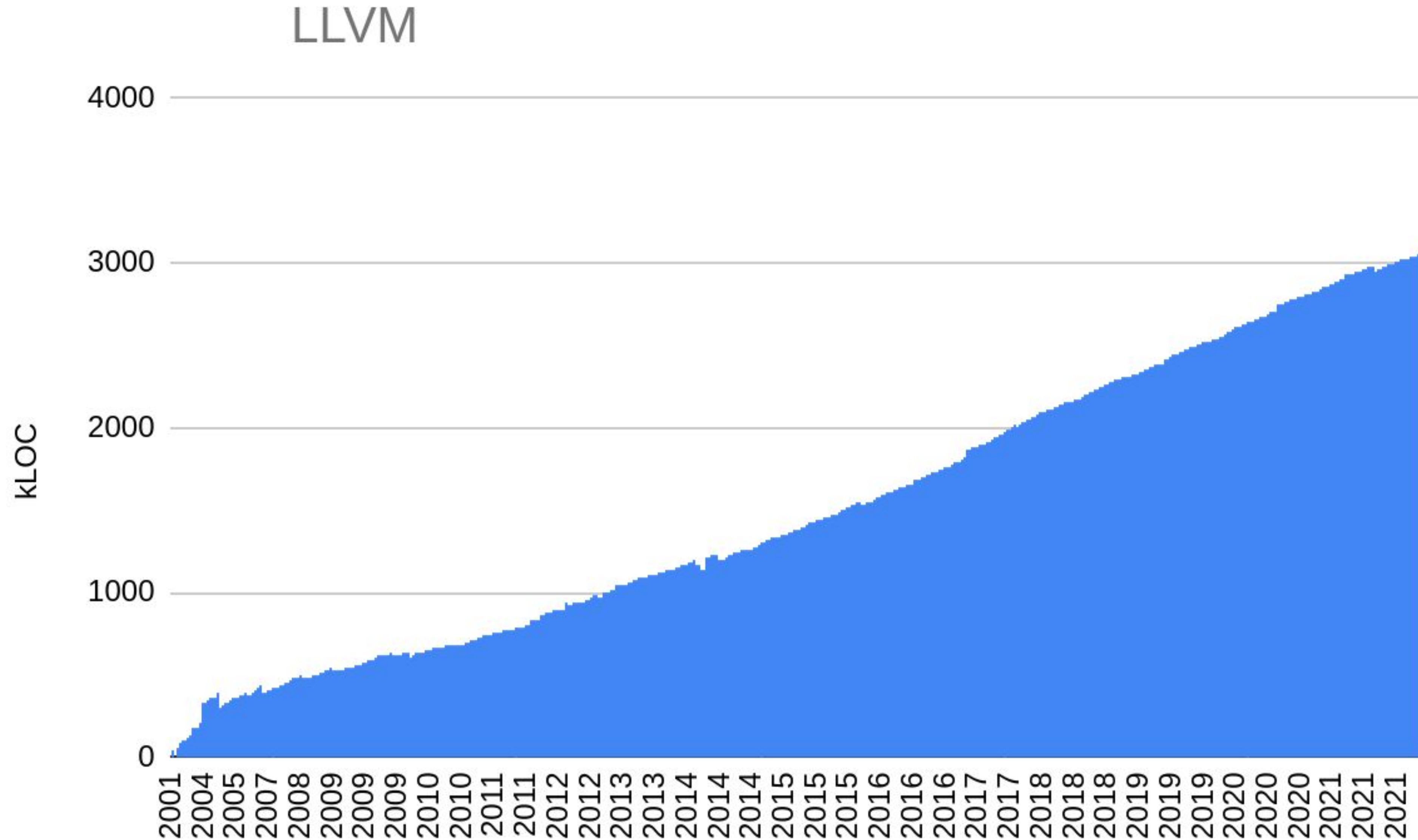
Tortoise: [freeimages.com](http://freeimages.com)

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# Compiler Complexity Growth



# Compiler Complexity Growth





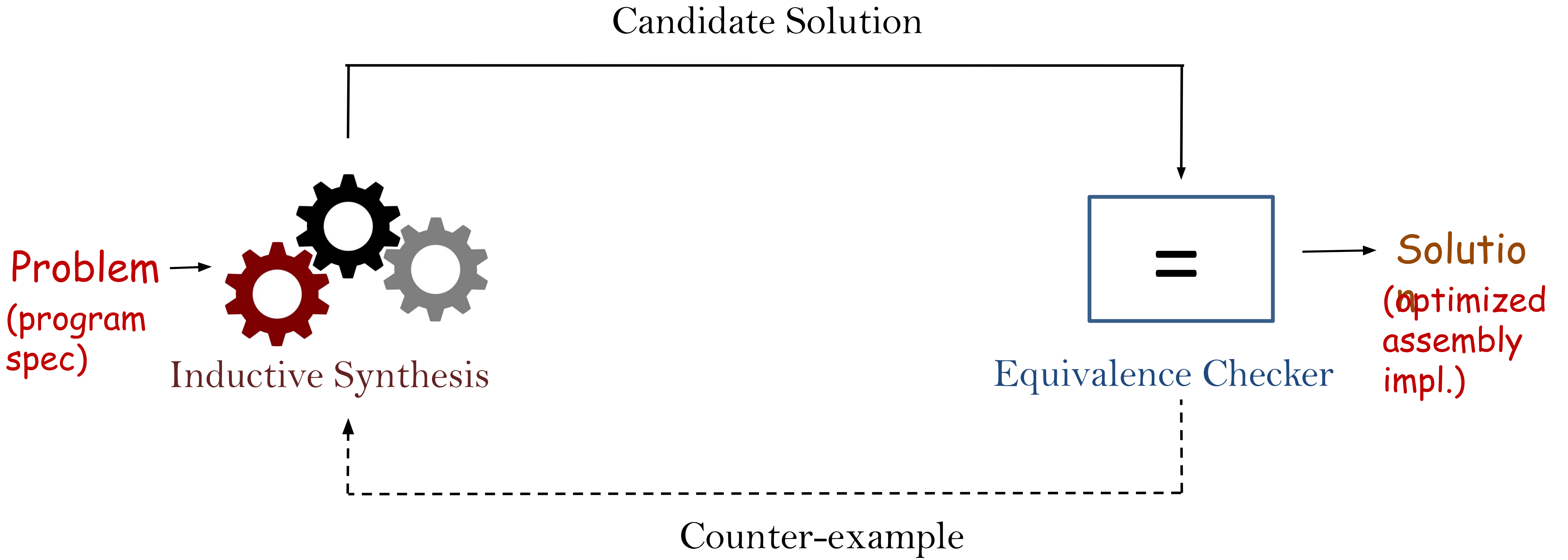
# Superoptimization

Problem  
(program  
spec) →

Compiler Algorithms Carefully Developed by  
Expert Programmers

→ Solution  
(optimized  
assembly  
impl.)

# Superoptimization

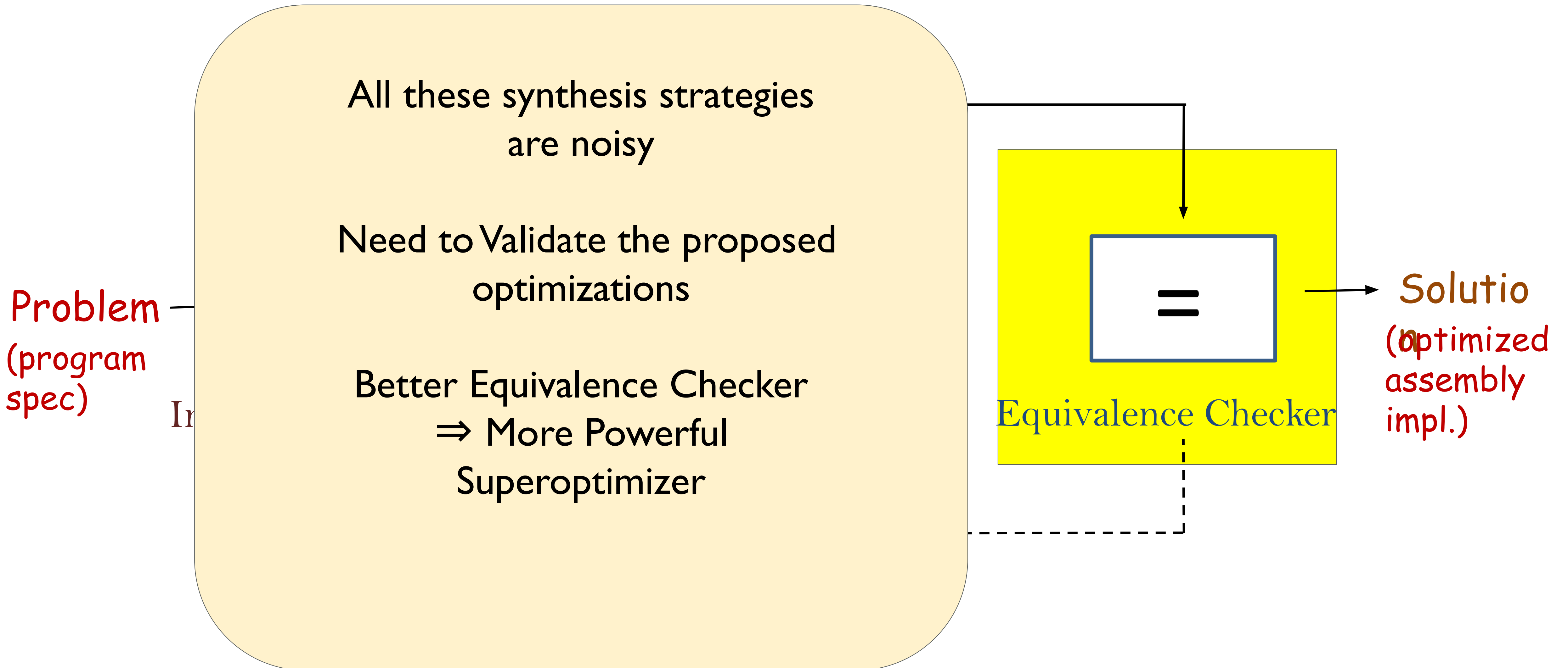


# Superoptimization





# Superoptimization

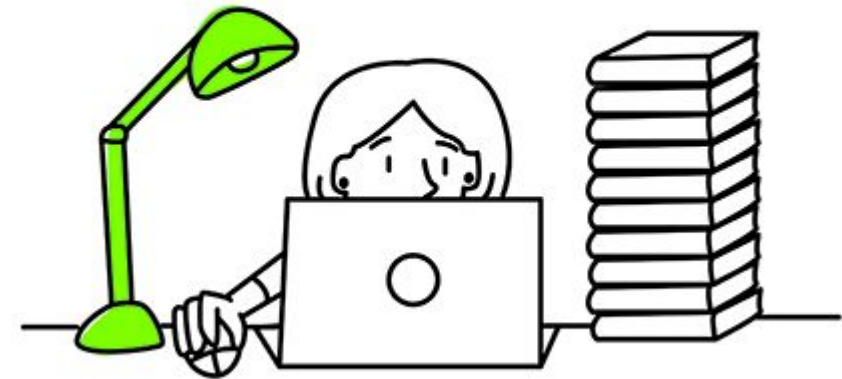


# Traditional Development Model for a Compiler

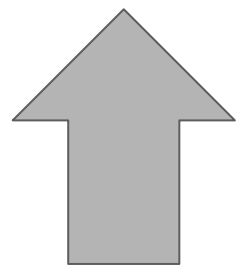


An engineer gets  
an optimization  
idea

# Traditional Development Model for a Compiler



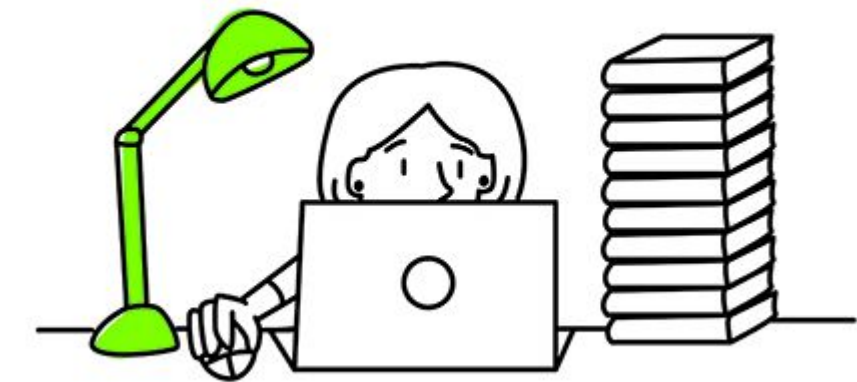
Codes it up



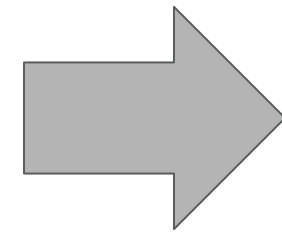
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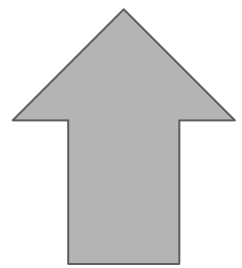
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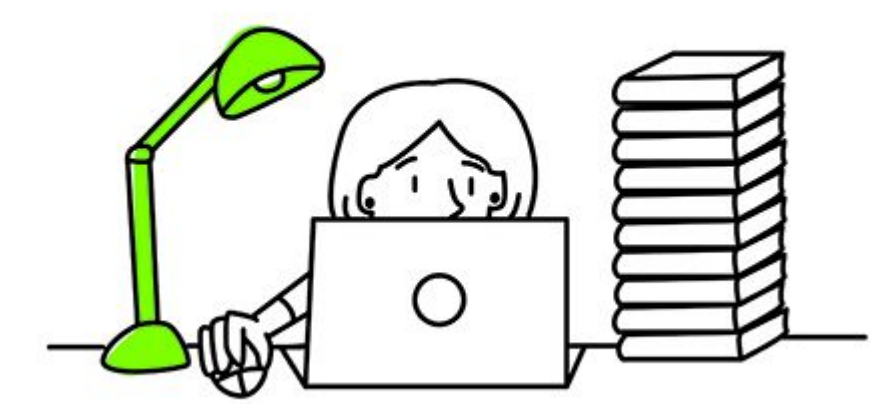


Reviewed by experts

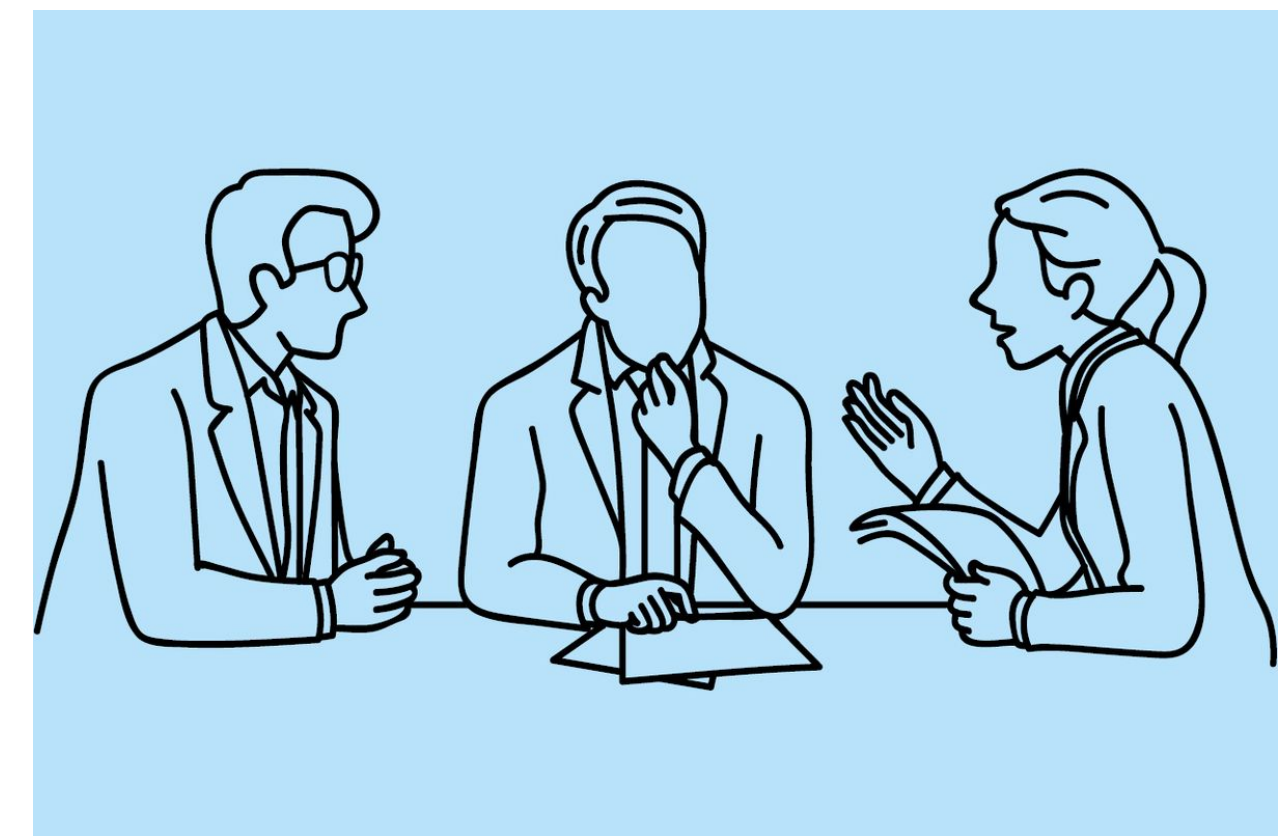
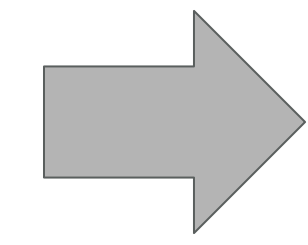


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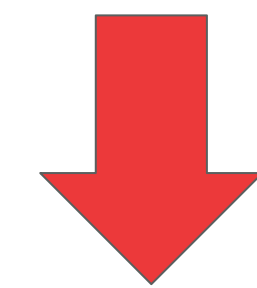
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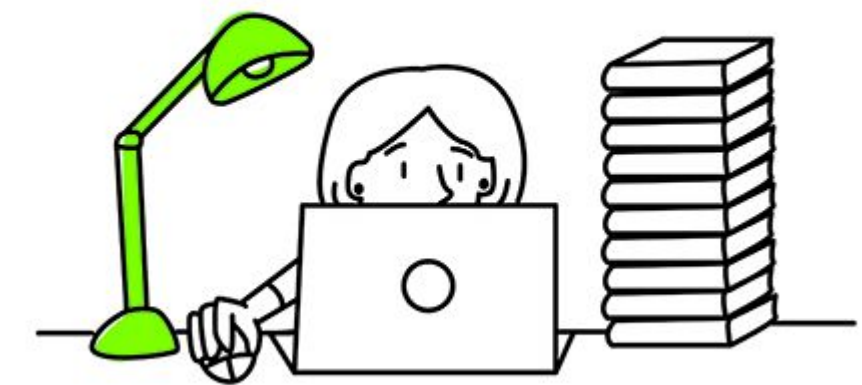
**Reject**



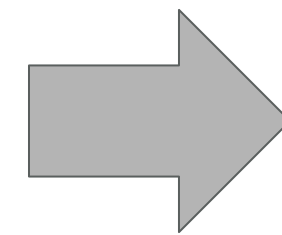
An engineer gets  
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idea

- Too complex compared to the benefit it entails
- Too specific to a certain PL
- Too specific to a certain architecture
- Requires compiler overhaul...

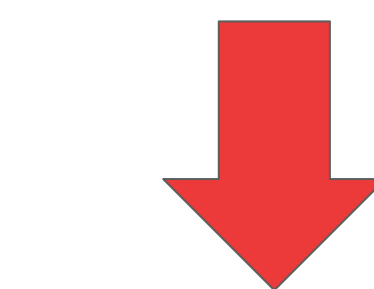
# Traditional Development Model for a Compiler



Codes it up



Reviewed by experts



**Reject**

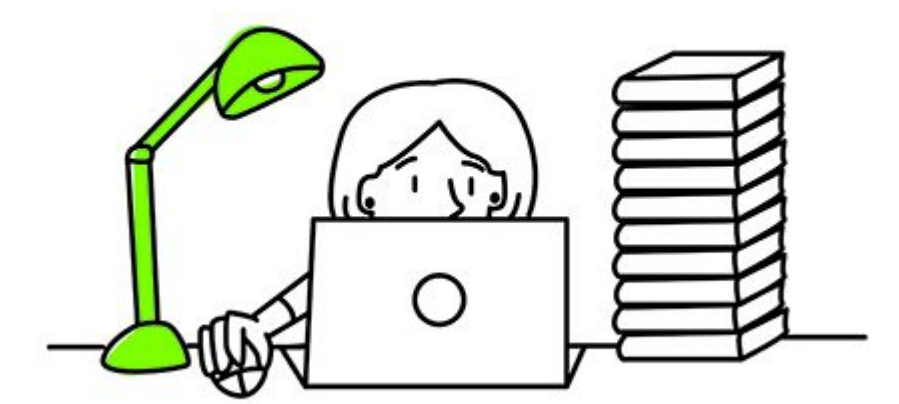
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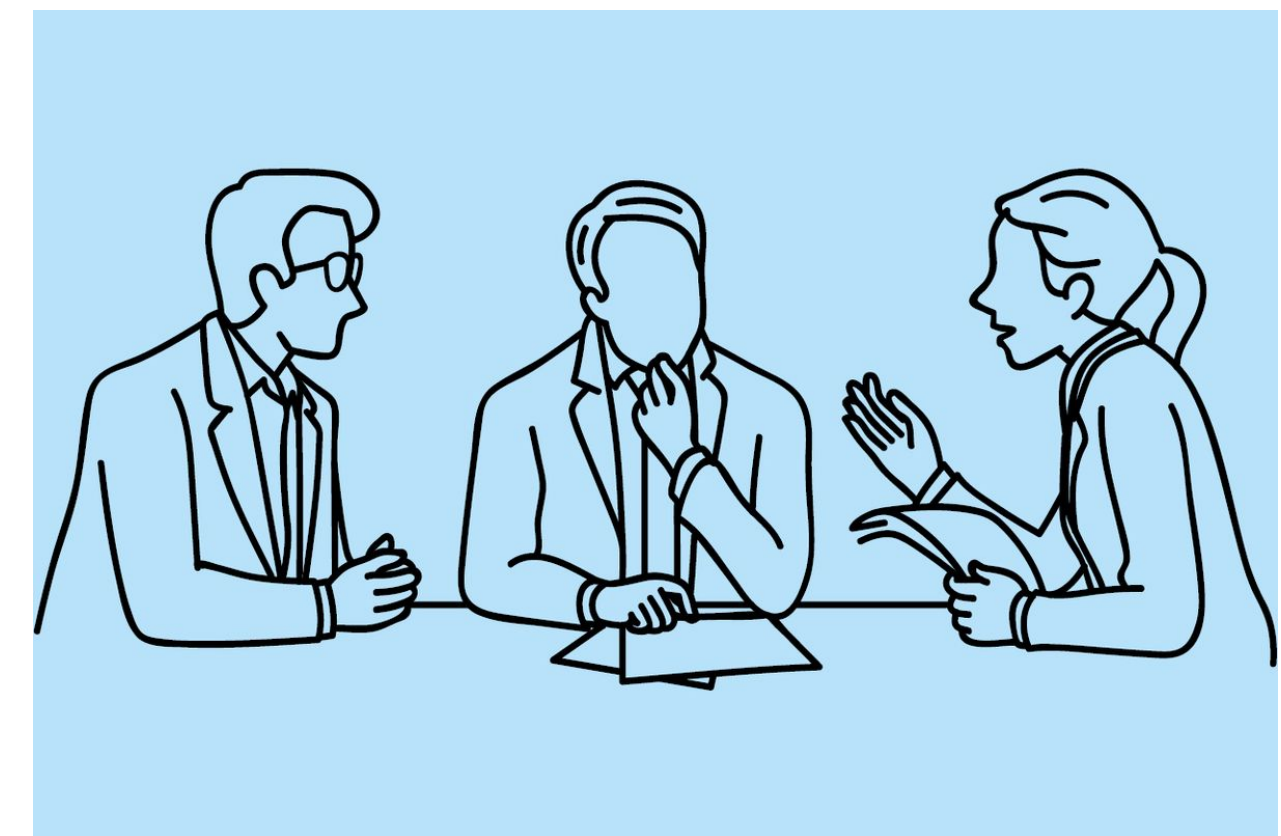
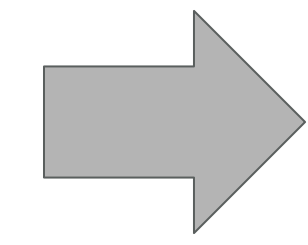
An engineer gets an optimization idea



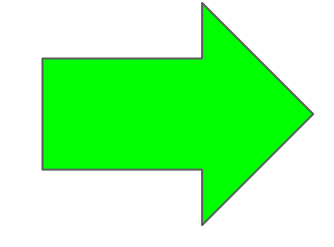
# Traditional Development Model for a Compiler



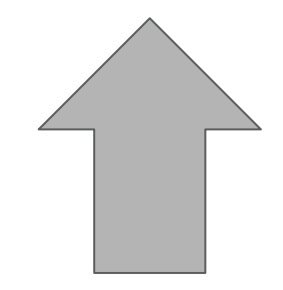
Codes it up



Reviewed by experts

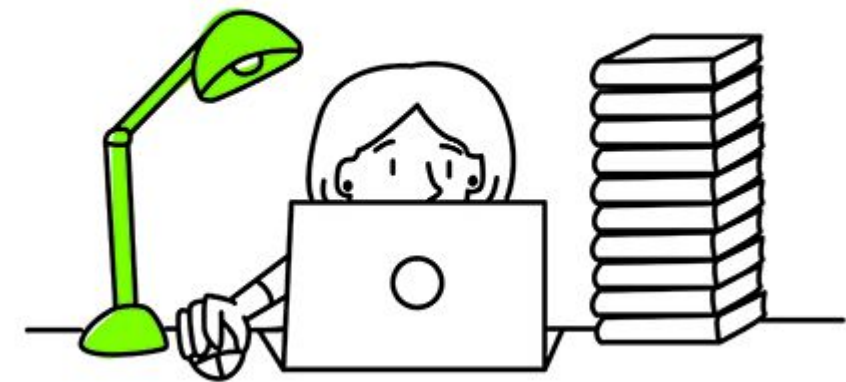


**Accept**

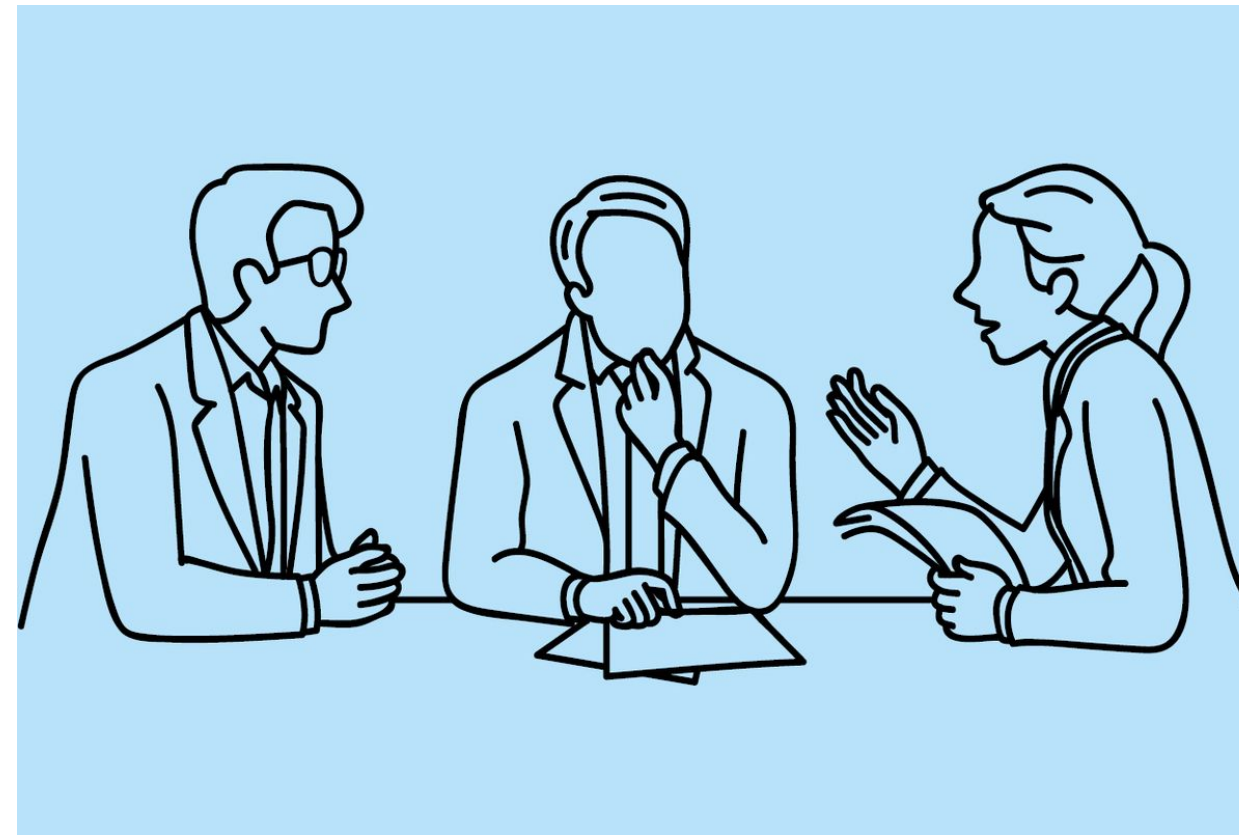
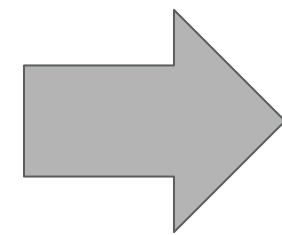


An engineer gets  
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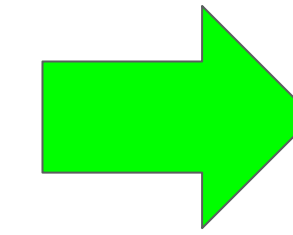
# Traditional Development Model for a Compiler



Codes it up



Reviewed by experts

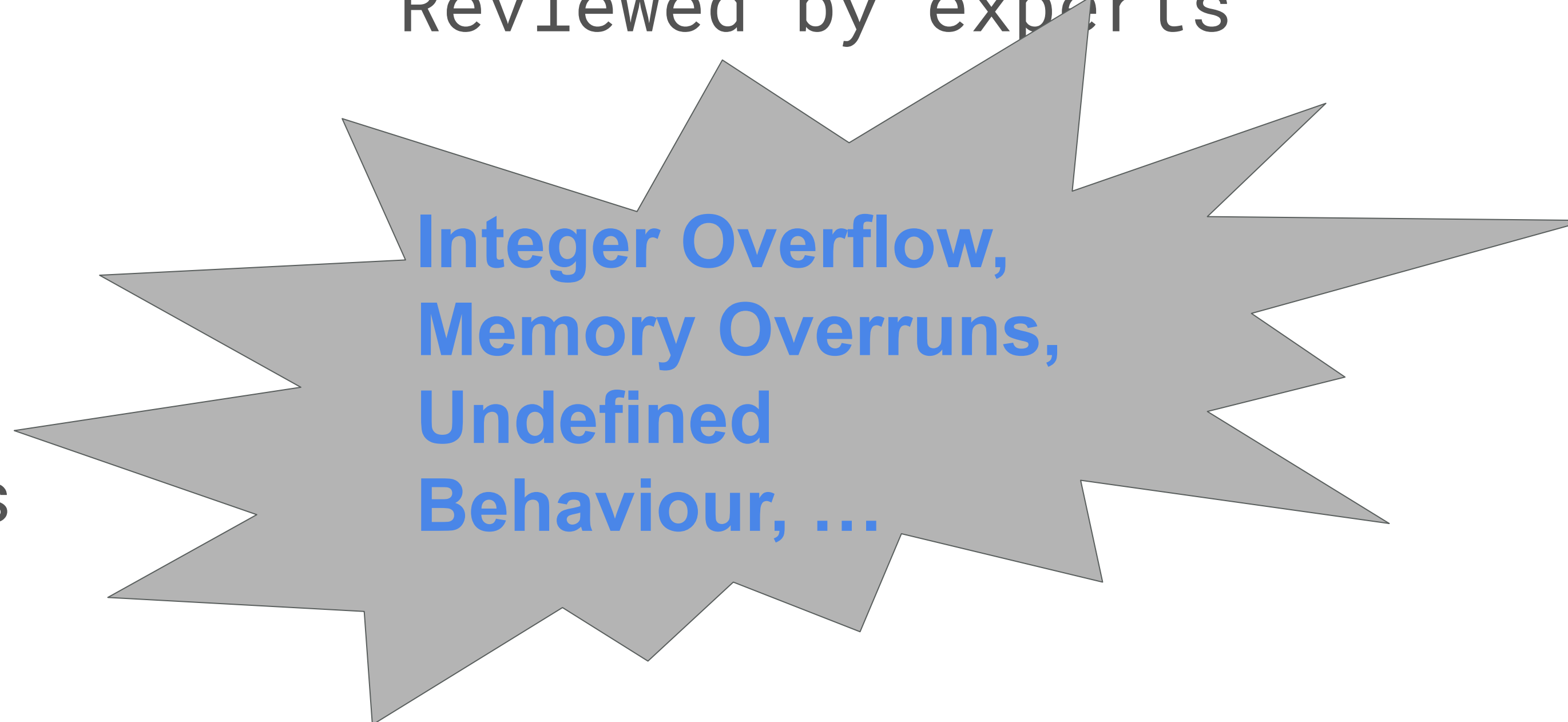
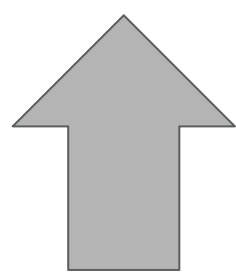


**Accept**

**but  
wait...**



An engineer gets  
an optimization  
idea

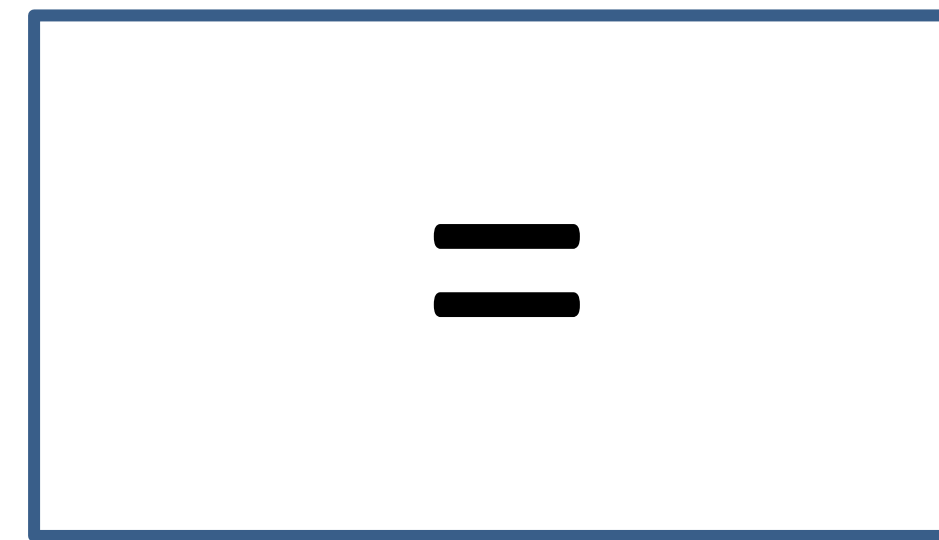


**Integer Overflow,  
Memory Overruns,  
Undefined  
Behaviour, ...**

**compiler  
bugs are  
still  
common**

# Proposed Development Model

Equivalence Checker



**Accept and  
Cache the  
problem-  
solution  
pair as a  
pattern-  
replacement**

**Reject**

**Developers of Inductive  
Synthesis Algorithms**





# Pattern-Replacement Examples

```
int signum(int x) {  
    if (x > 0) return 1;  
    if (x < 0) return -1;  
    else return 0;  
}
```

On Motorola 68020:

```
add.l    d0, d0  
subx.l   d1, d1  
negx.l   d0  
addx.l   d1, d1
```

# Pattern-Replacement Examples

pattern		replacement
load (addr), reg store reg, (addr)	<i>Support for memory accesses</i>	load (addr), reg
mul 2, reg		shl reg
mov r1, r2 mov r3, r1 mov r2,r3  live: r1,r3		xchg r1, r3
sub %eax, %ecx test %ecx, %ecx je .END mov %edx, %ebx .END:	<i>Support for branches</i>	sub %eax, %ecx cmovne %edx, %ebx

# Pattern-Replacement Examples

pattern	replacement
sum += a[i]; sum += a[i+1]; ... sum += a[i+7];	pshbb %mm0, %mm0 psadbw &a[i], %mm0 movd %mm0, sum <i>Use of vector instructions</i>
sub %eax, %ecx mov %ecx, %eax dec %eax live: %eax	not %eax add %ecx, %eax
setg %al movzbl %al, %eax dec %eax and %eax, %esi live: %esi	mov \$0, %eax cmovg %eax, %esi <i>Use of conditional-moves</i>

# Pattern-Replacement Examples

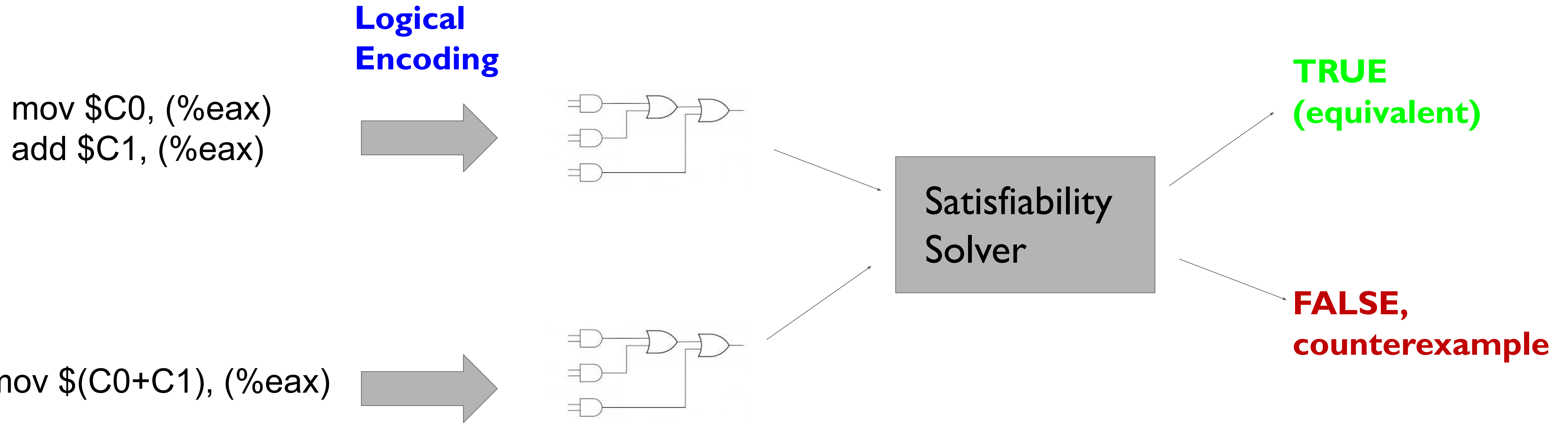
*Support for symbolic constants in pattern and replacement*

pattern	replacement
mov \$C0, %eax dec %eax	mov \$(C0-1), %eax
mov \$C0, (%eax) add \$C1, (%eax)	mov \$(C0+C1), (%eax)

[S. Bansal, A. Aiken. Automatic Generation of Peephole Superoptimizers, ASPLOS 2006]



# Equivalence Checker



[S. Bansal, A. Aiken. Automatic Generation of Peephole Superoptimizers, ASPLOS 2006]

# Important Limitations

- Loops are not supported

pattern

```
for (...) {  
  r = *p;  
  use(r); // *p remains unchanged  
  *p = r;  
}
```

replacement

```
r = *p;  
for (...) {  
  use(r); // *p remains unchanged  
}
```



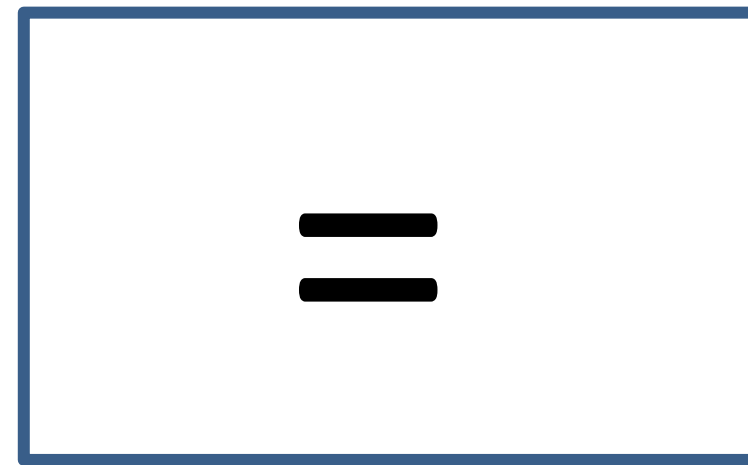
# Important Limitations

- Aliasing information is not captured, e.g., heap access vs. stack access

pattern	replacement
load (stack-addr), reg access (heap-addr) store reg, (stack-addr)	load (stack-addr), reg access (heap-addr)



# Equivalence Checker



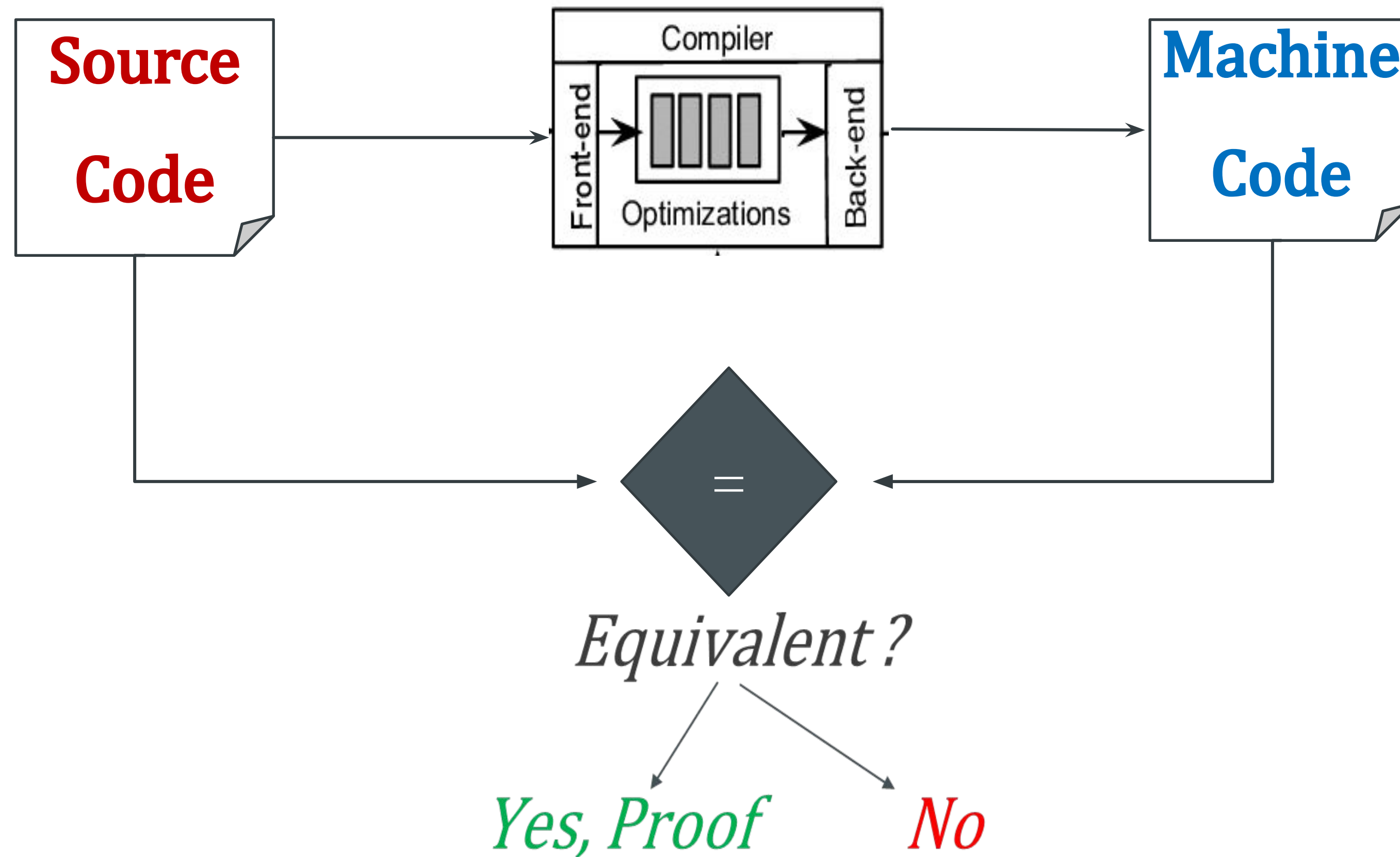
Equivalence Checker

End-to-End, support for loops, aliasing information, function calls, ...

No false-positives (sound)

Minimize false-negatives

# Translation Validation





# Equivalence Checking – Program with loops

```
void divP () {  
    for( int i=0; i < 1024; i++) {  
        a[i] = b[i]/2;  
    }  
}
```

C Program

```
void shiftP () {  
    for(int r1=0; r1 < 1024; r1++) {  
        a[r1] = b[r1] >> 1;  
    }  
}
```

(abstracted) Assembly

# Equivalence Checking – Program with loops

Given,  $\text{Input}_C == \text{Input}_A$

$\text{Memory}_C == \text{Memory}_A$

```
void divP () {
```

```
  for( int i=0; i < 1024; i++) {
```

```
    a[i] = b[i]/2;
```

```
  }
```

```
}
```

C Program



```
void shiftP () {
```

```
  for(int r1=0; r1 < 1024; r1++) {
```

```
    a[r1] = b[r1] >> 1;
```

```
  }
```

```
}
```

(abstracted) Assembly

# Equivalence Checking – Program with loops

Given,  $\text{Input}_C == \text{Input}_A$

$\text{Memory}_C == \text{Memory}_A$

```
void divP () {
```

```
  for( int i=0; i < 1024; i++) {
```

```
    a[i] = b[i]/2;
```

```
  }
```

```
}
```

C Program

```
void shiftP () {
```

```
  for(int r1=0; r1 < 1024; r1++) {
```

```
    a[r1] = b[r1] >> 1;
```

```
  }
```

```
}
```

(abstracted) Assembly

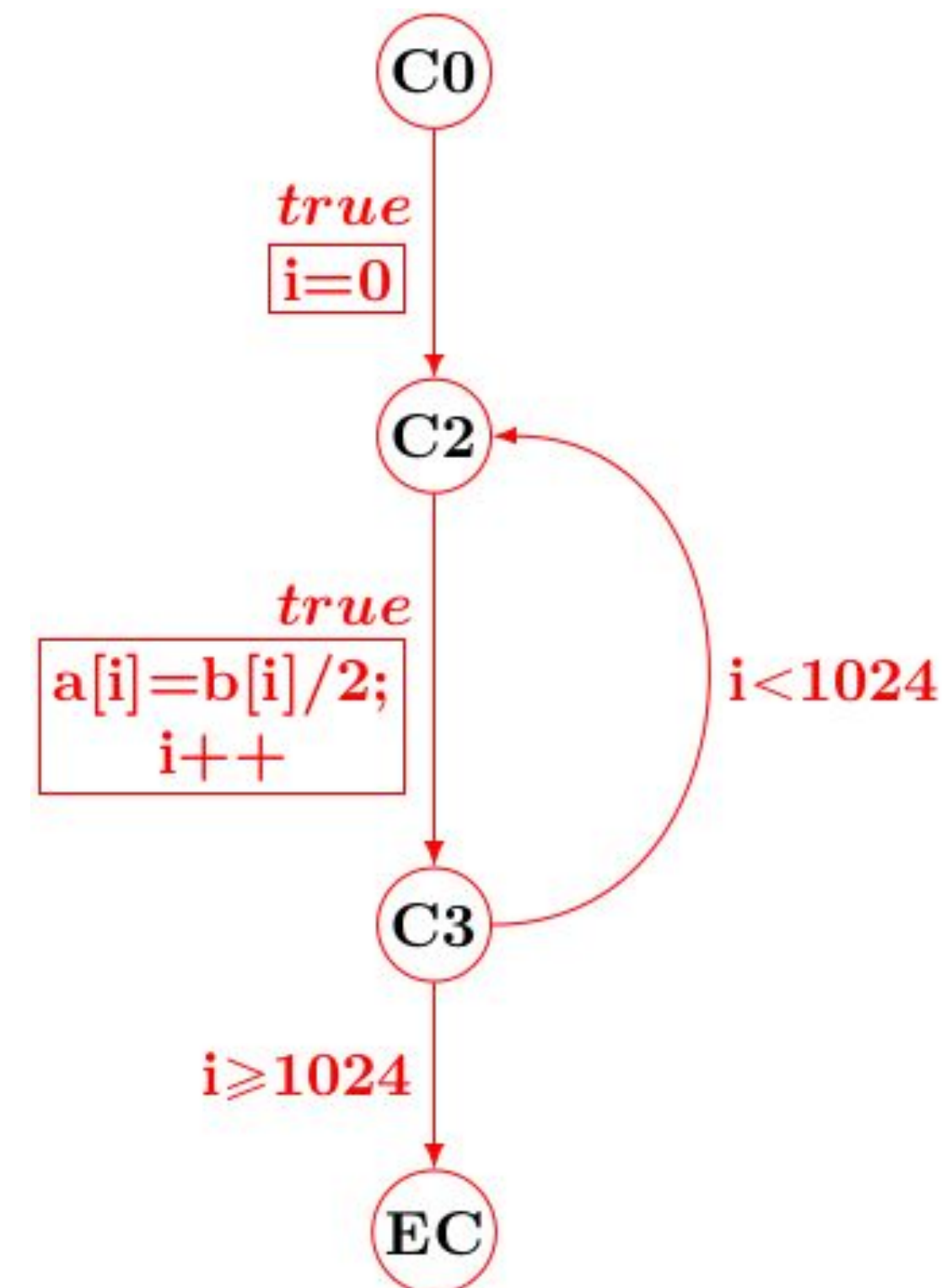
$\text{Return}_C == \text{Return}_A$

$\text{Memory}_C == \text{Memory}_A ?$

# Control Flow Graph (CFG)

```
C0: void divP ( ) {  
C1:   for( int i=0; i < 1024; ) {  
C2:     a[i] = b[i]/2; i++;  
C3:   }  
EC: }
```

C Program



Nodes are PCs

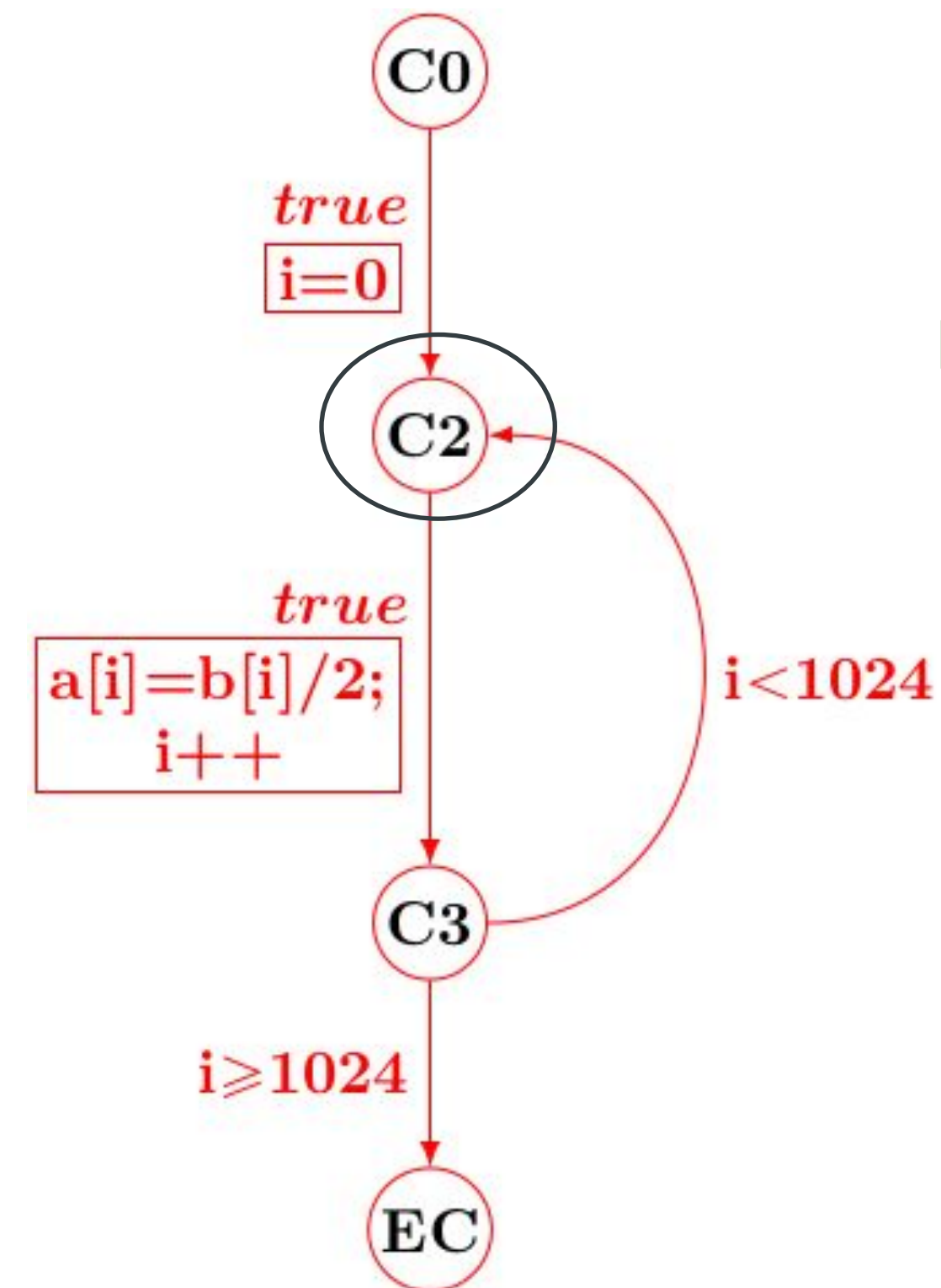
Edges involve transfer functions



# Control Flow Graph (CFG)

```
C0: void divP ( ) {  
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```

C Program



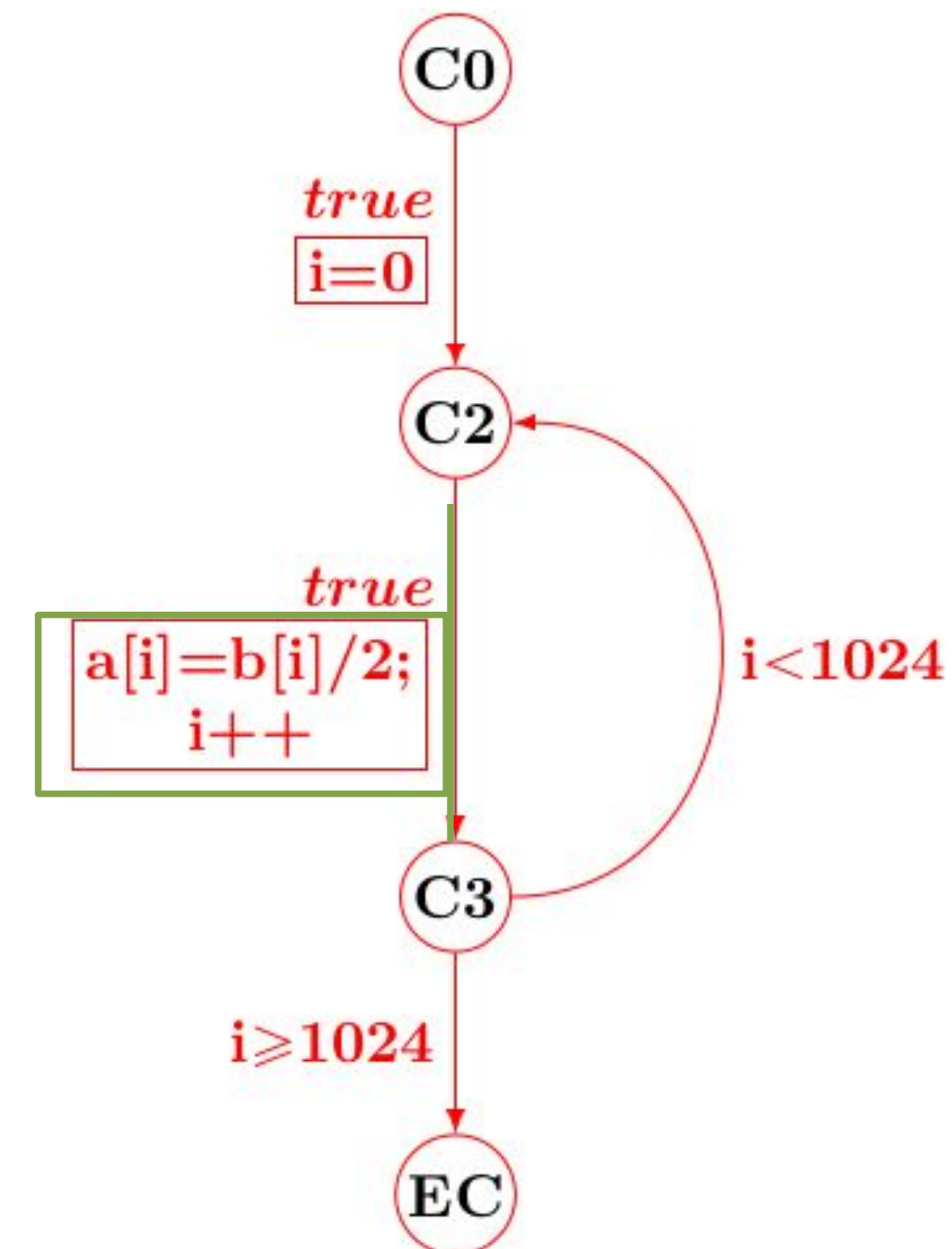
Node C2  
represents a PC

# Control Flow Graph (CFG)

```
C0: void divP ( ) {  
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EC: }
```

## C Program

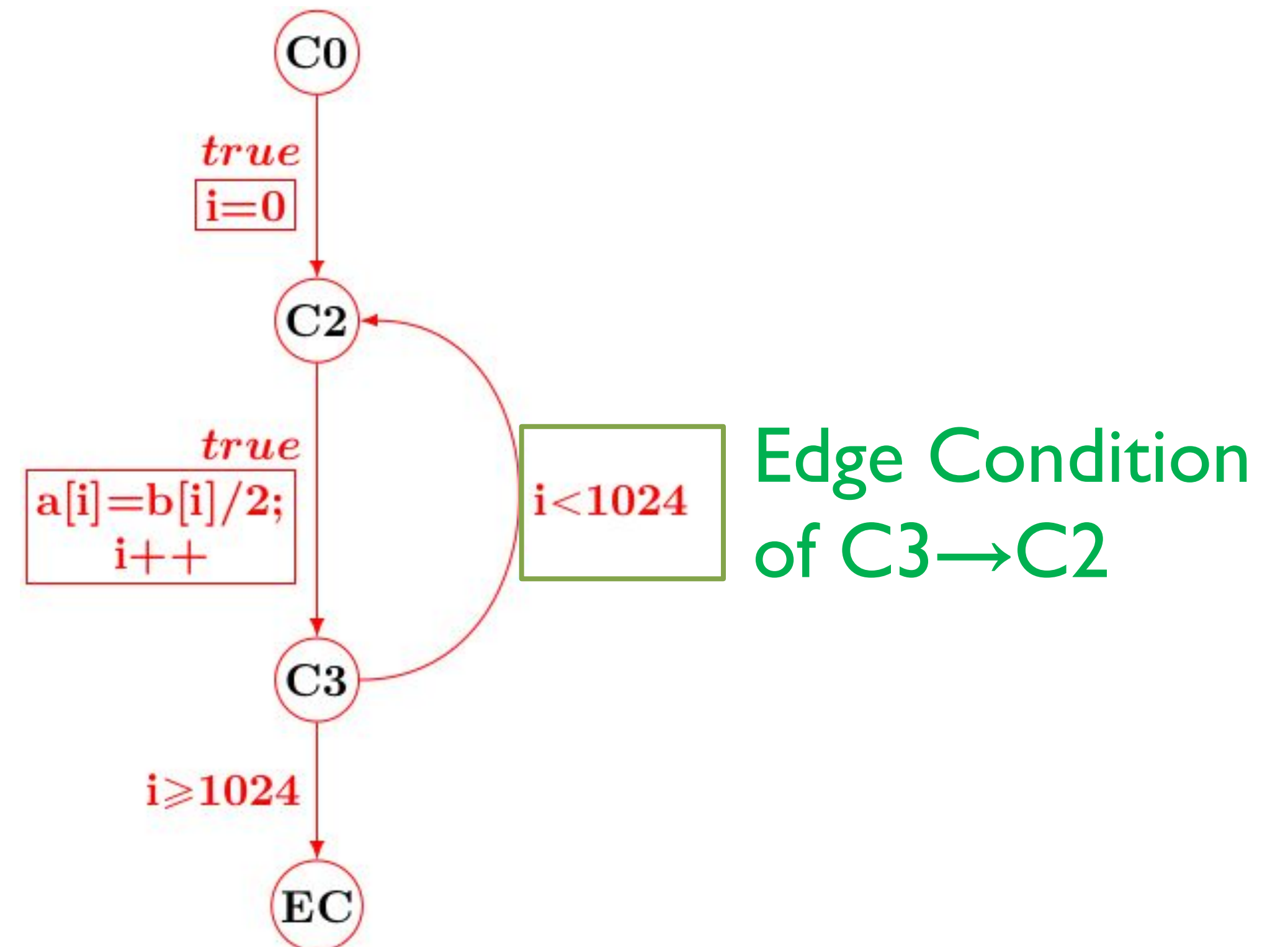
Transfer function  
of  $C2 \rightarrow C3$



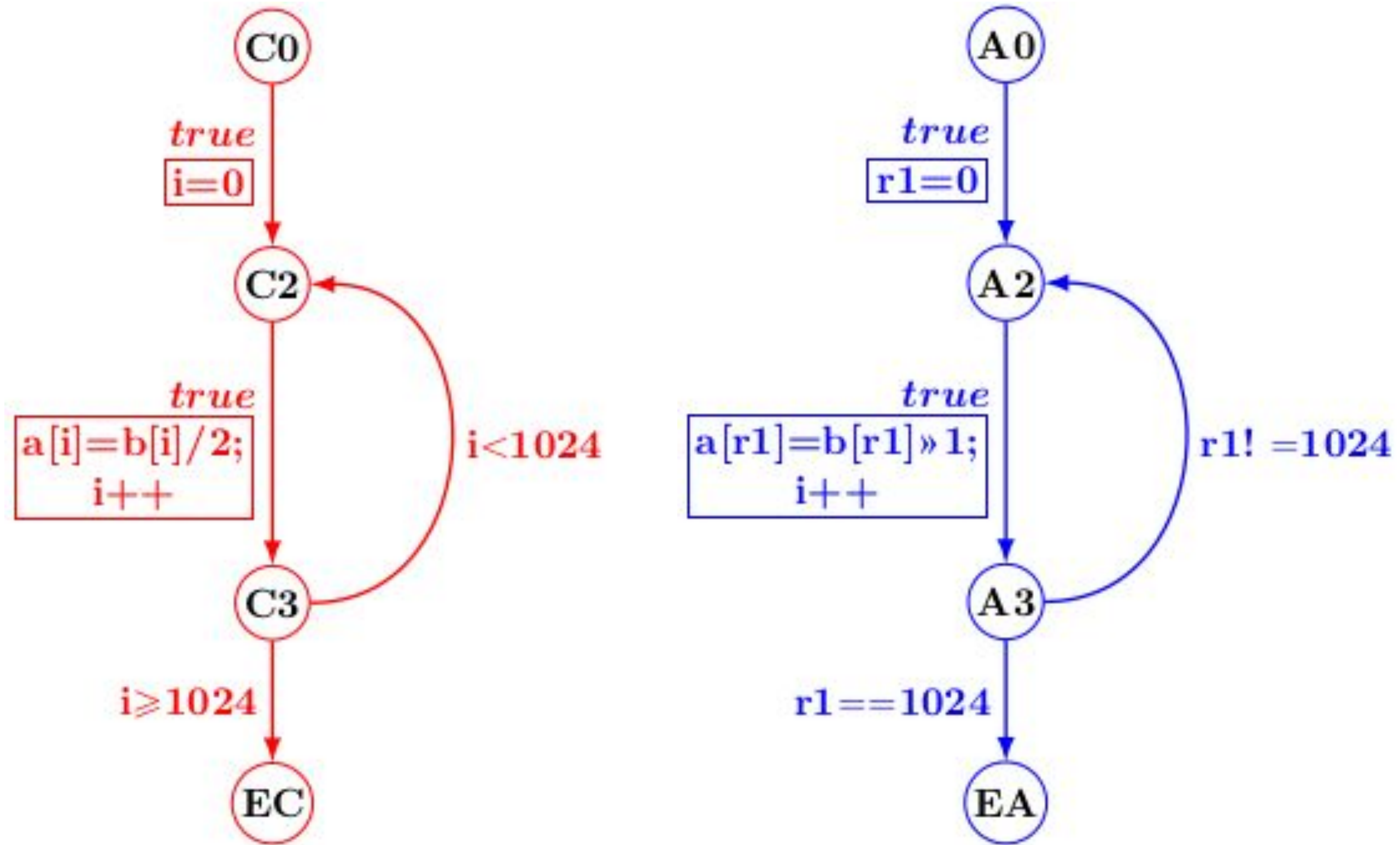
# Control Flow Graph (CFG)

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```

## C Program



# Product Program Construction

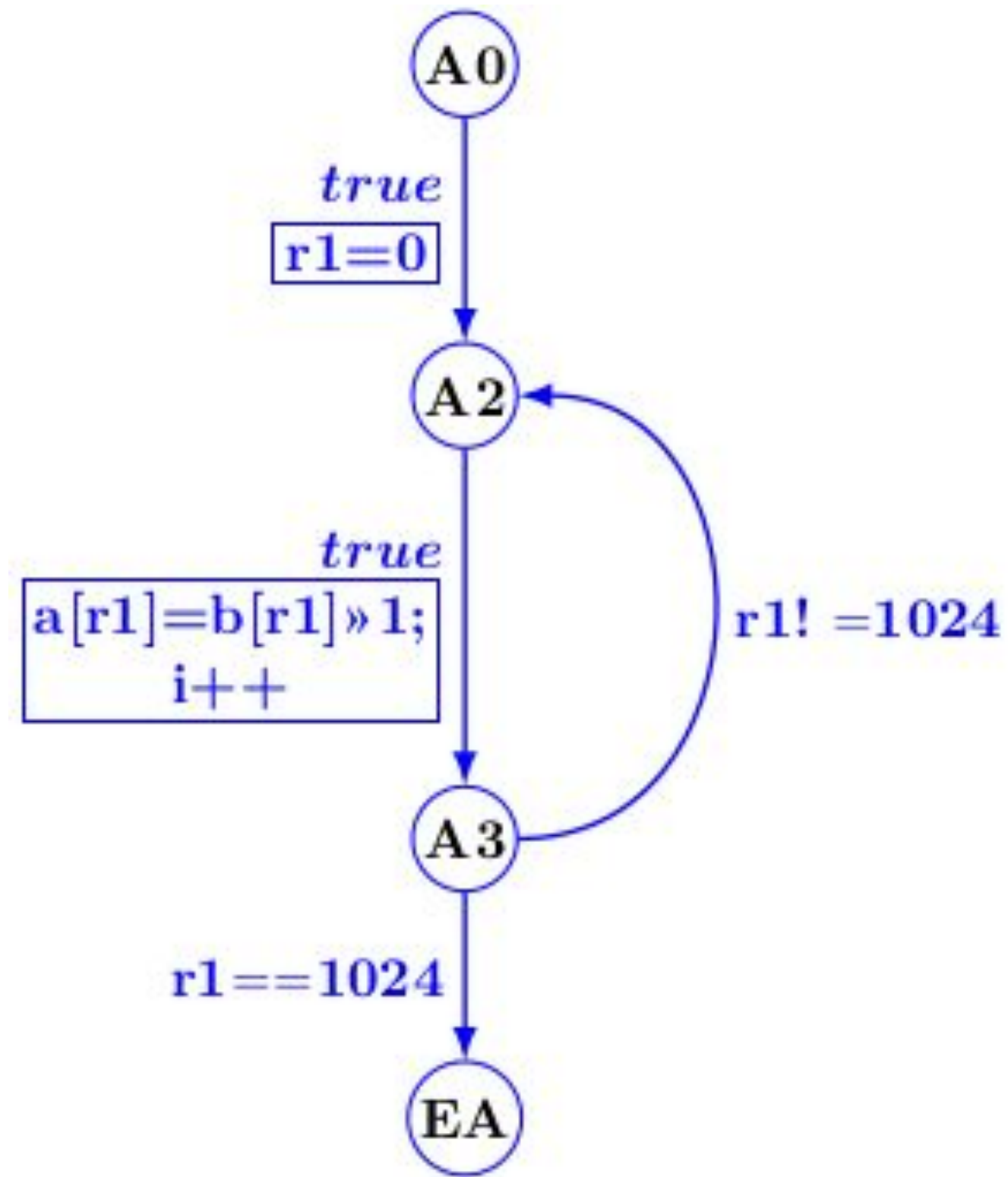
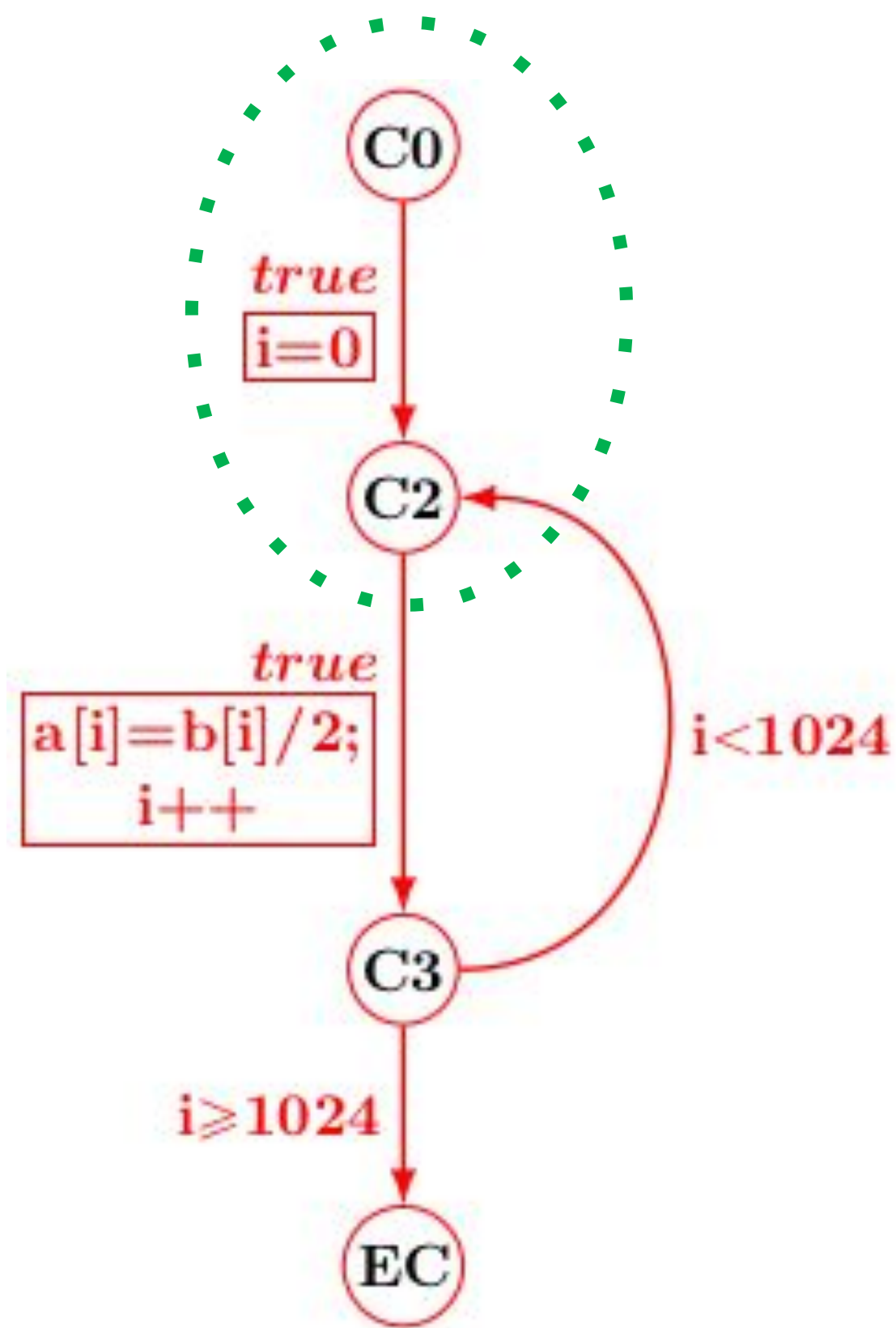


**Goal:** Construct a **Product Program** that executes both programs in lockstep

such that the two programs' states always remain related.



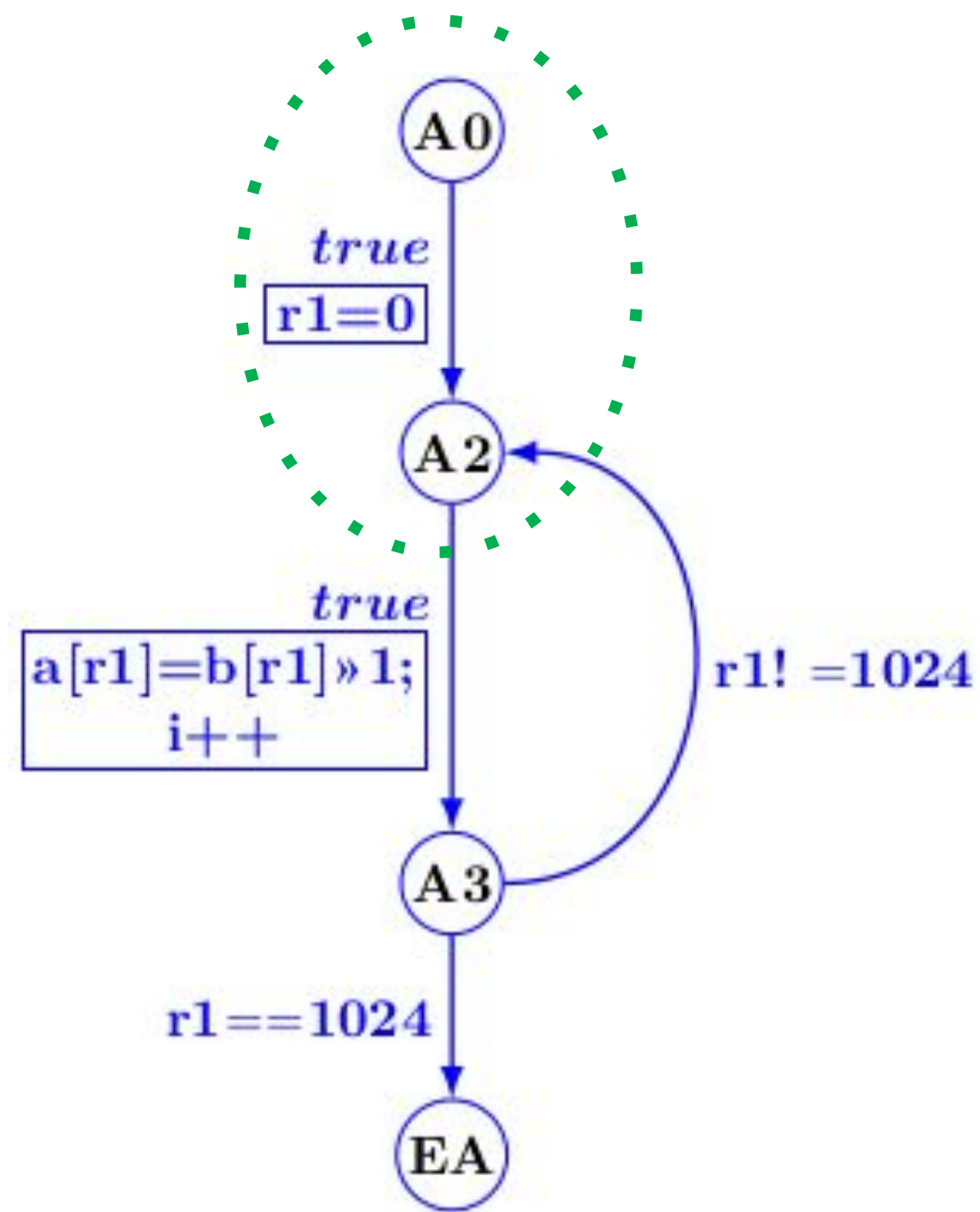
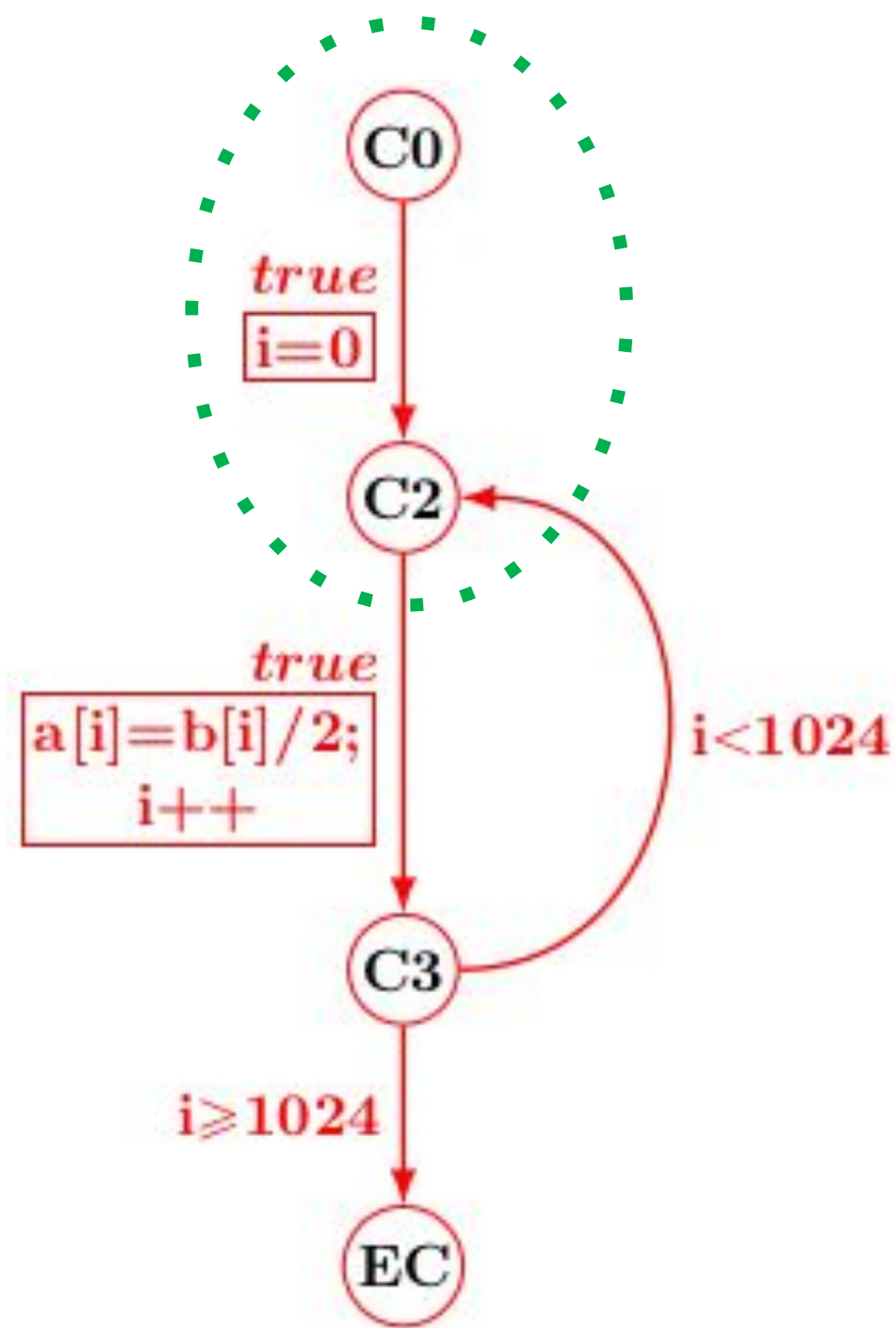
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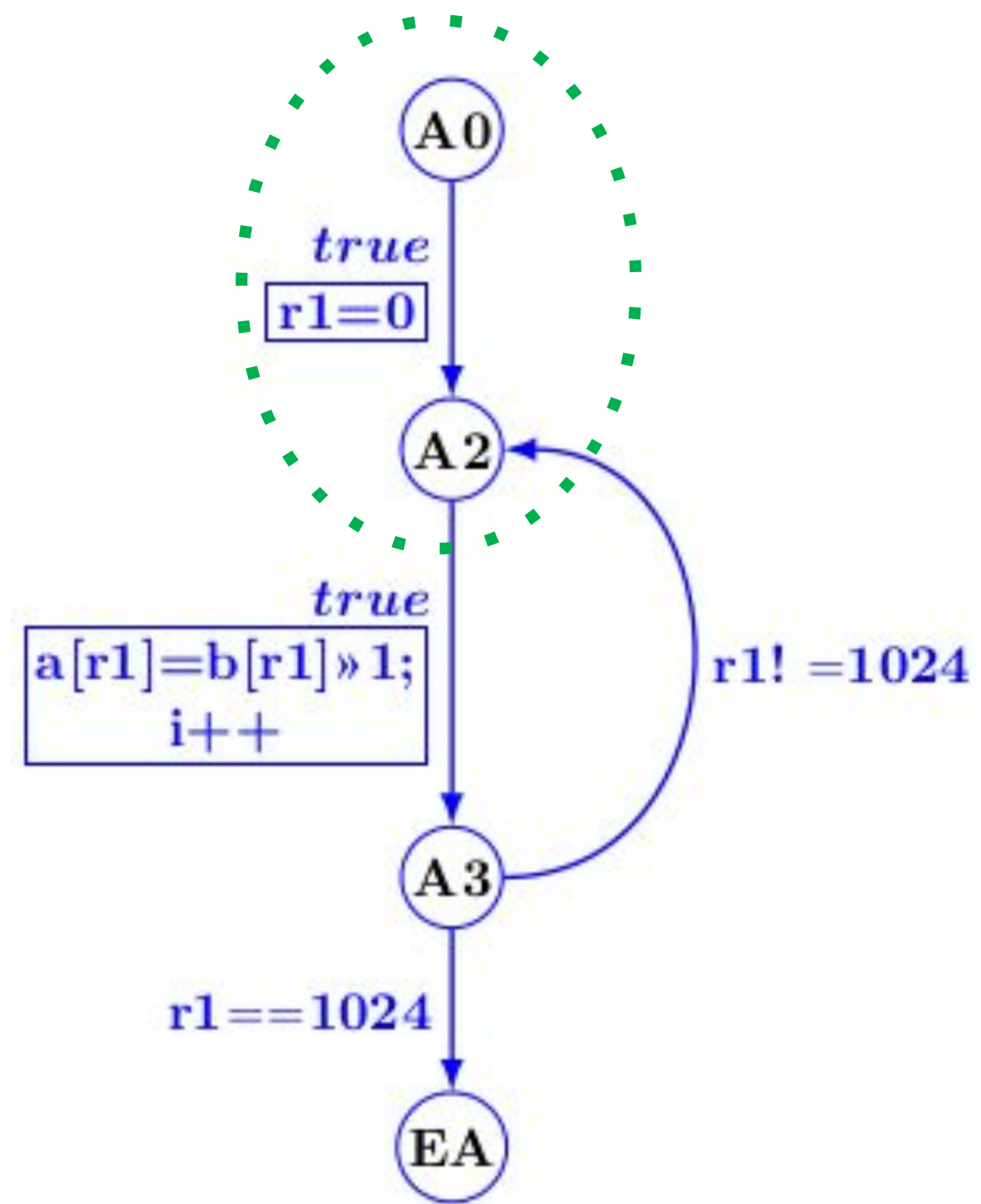
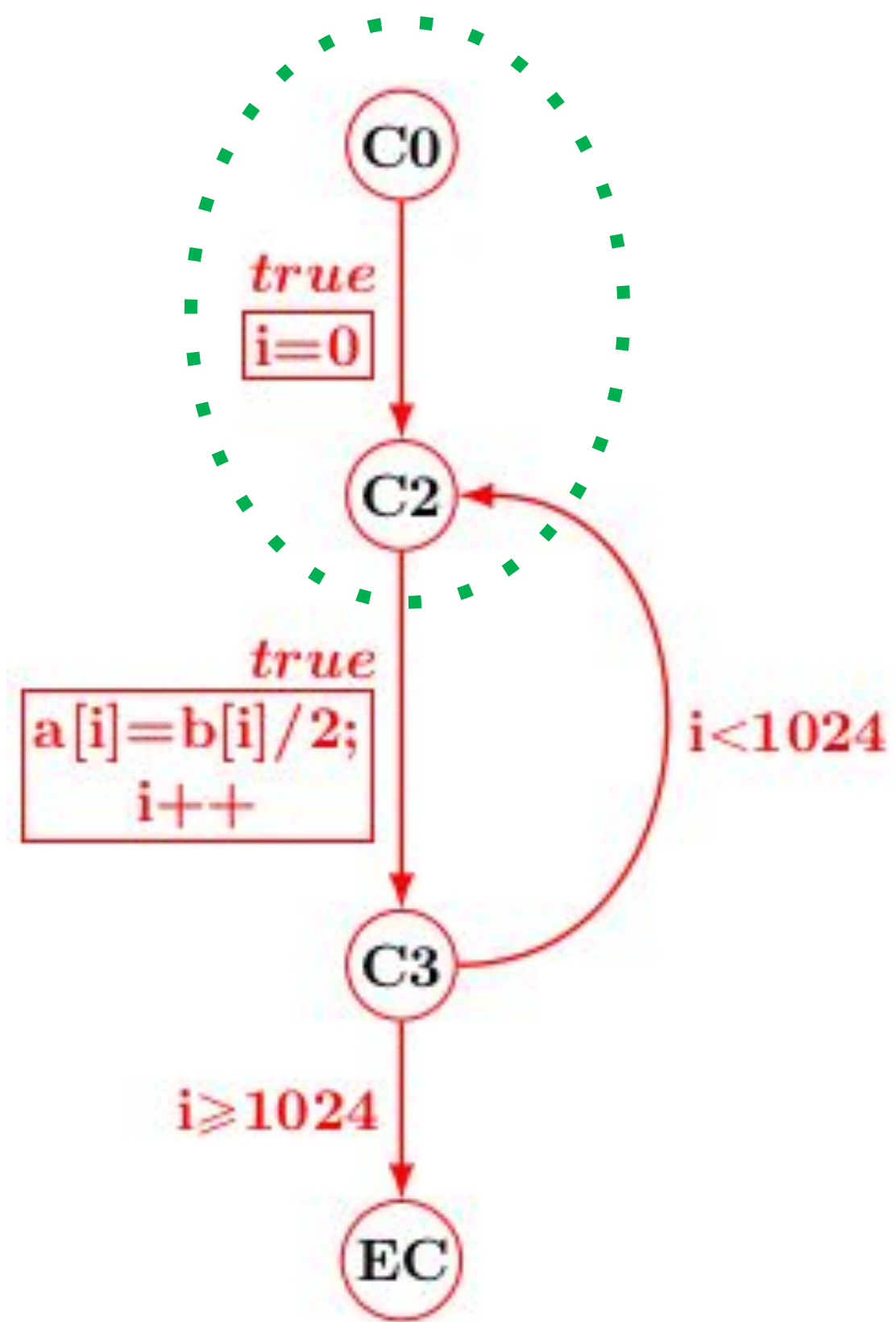
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# Product Program Construction

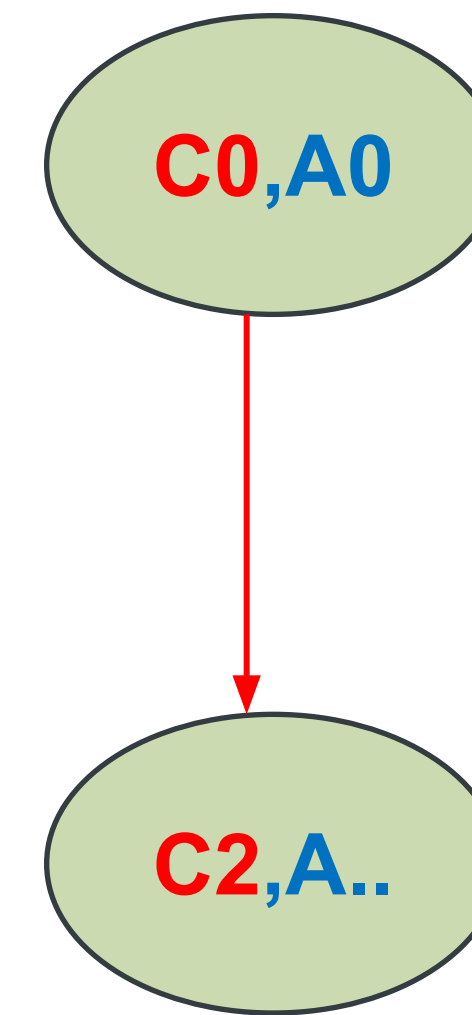
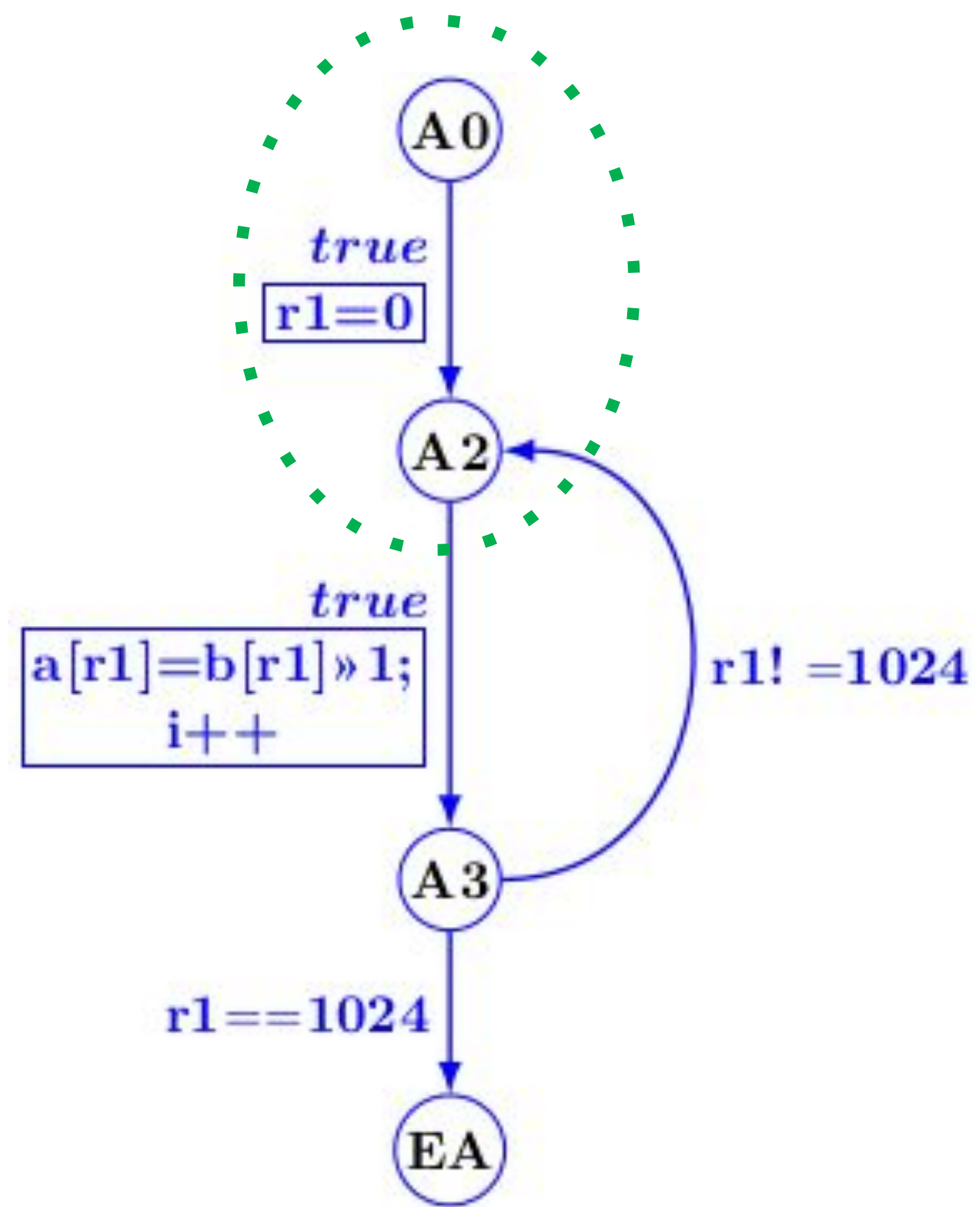
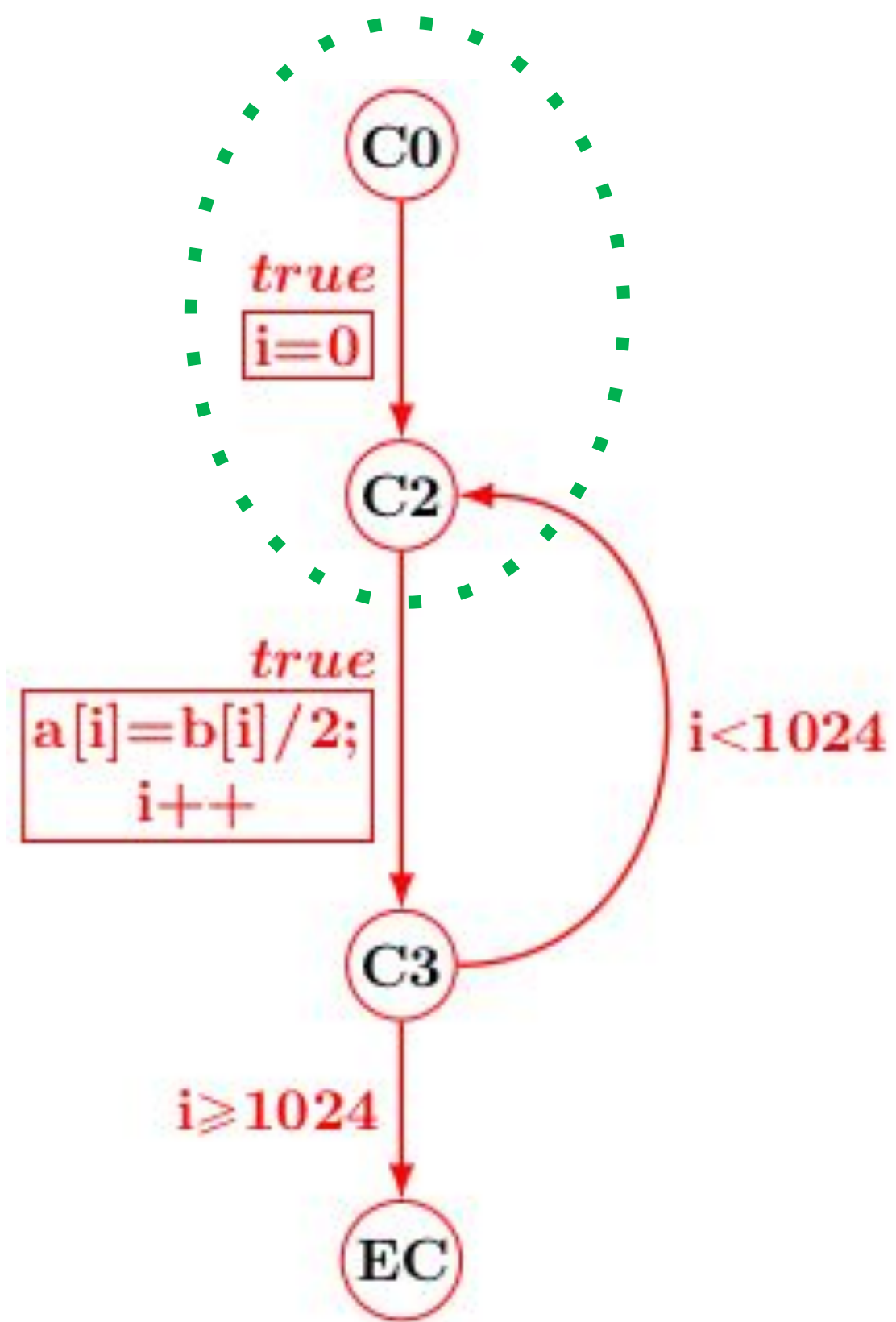


**C0,A0**

Product CFG



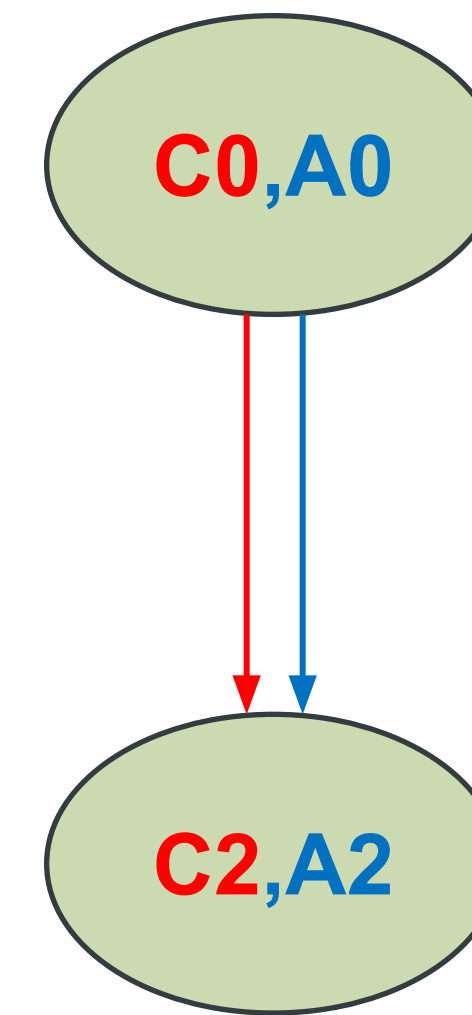
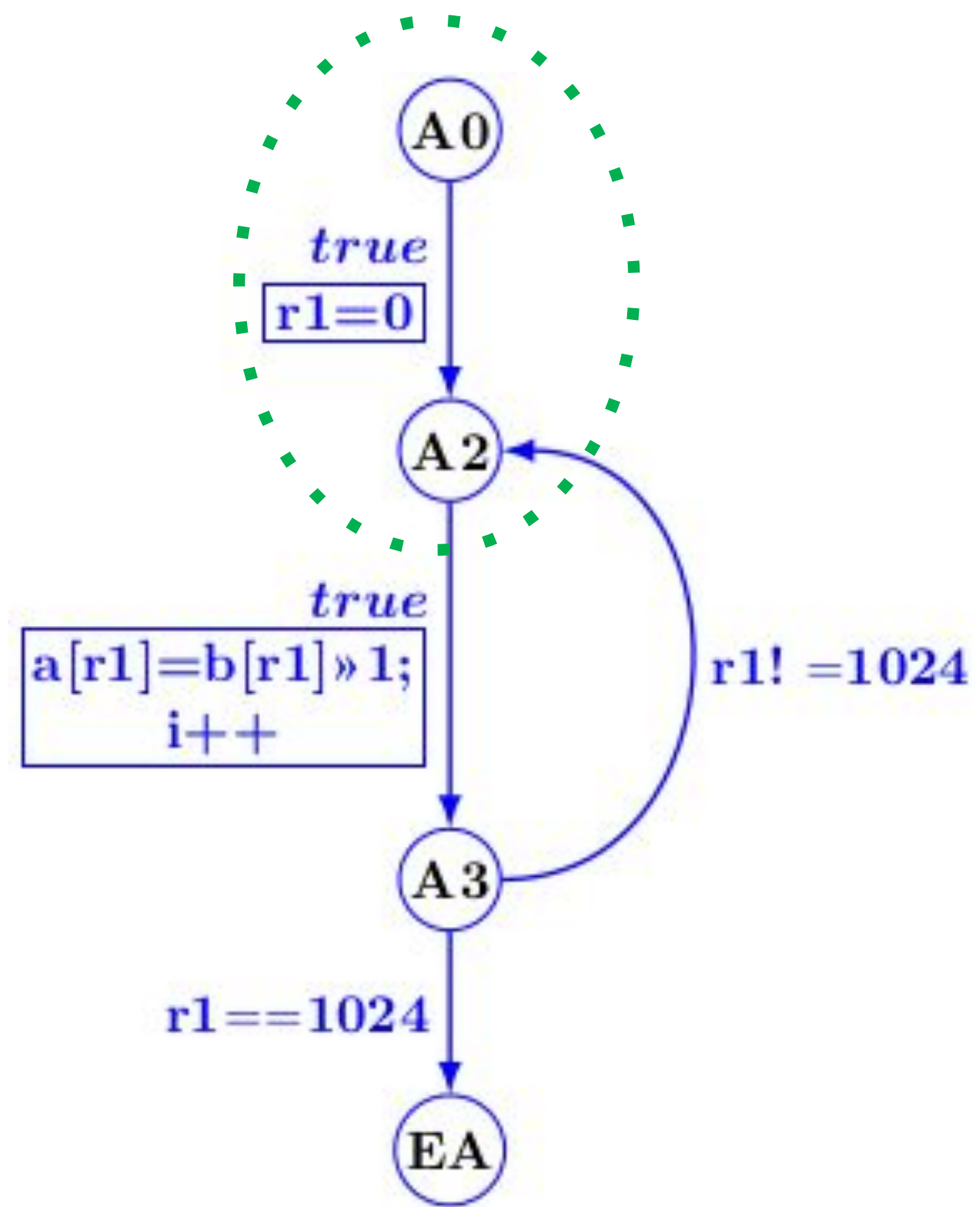
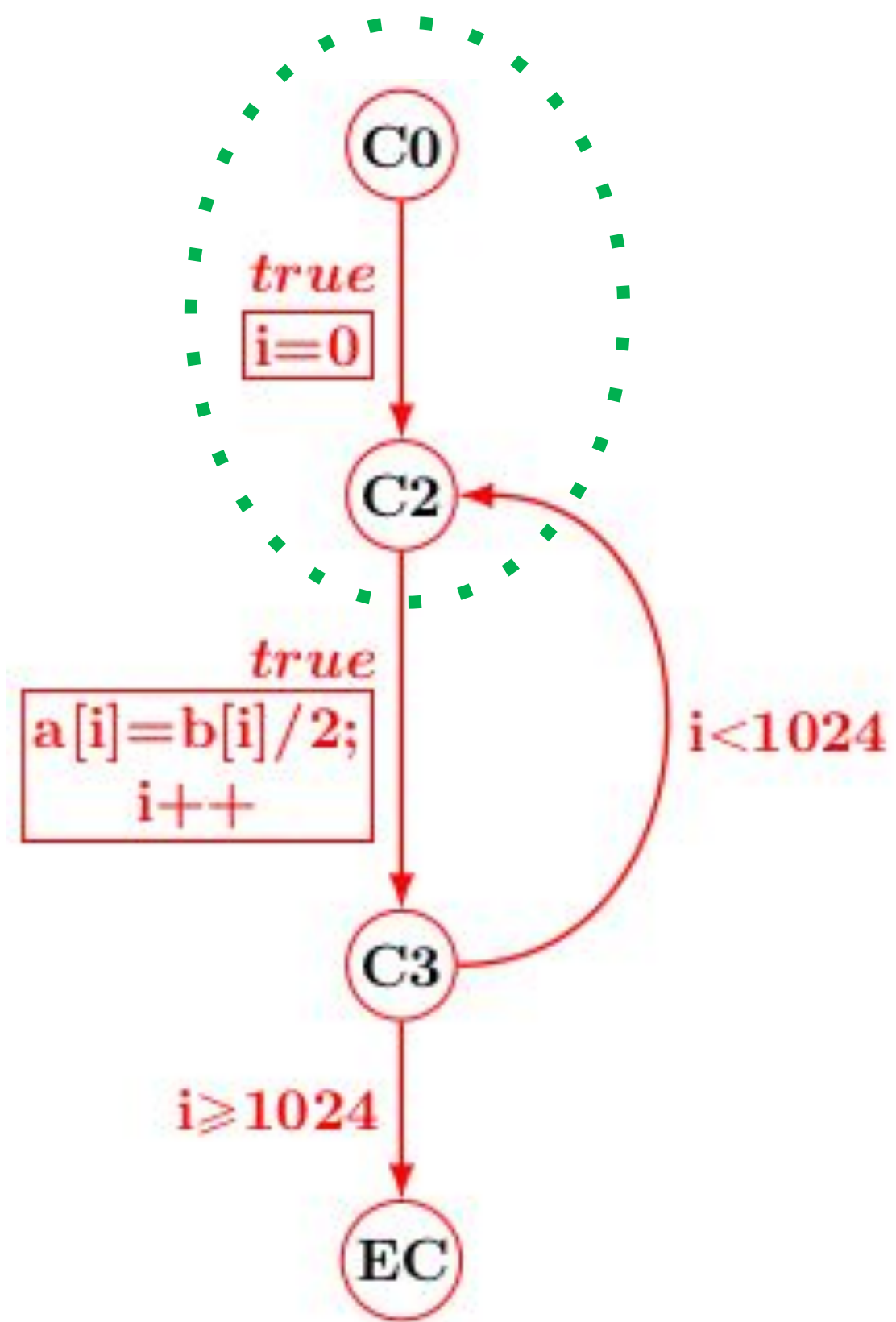
# Product Program Construction



Product CFG



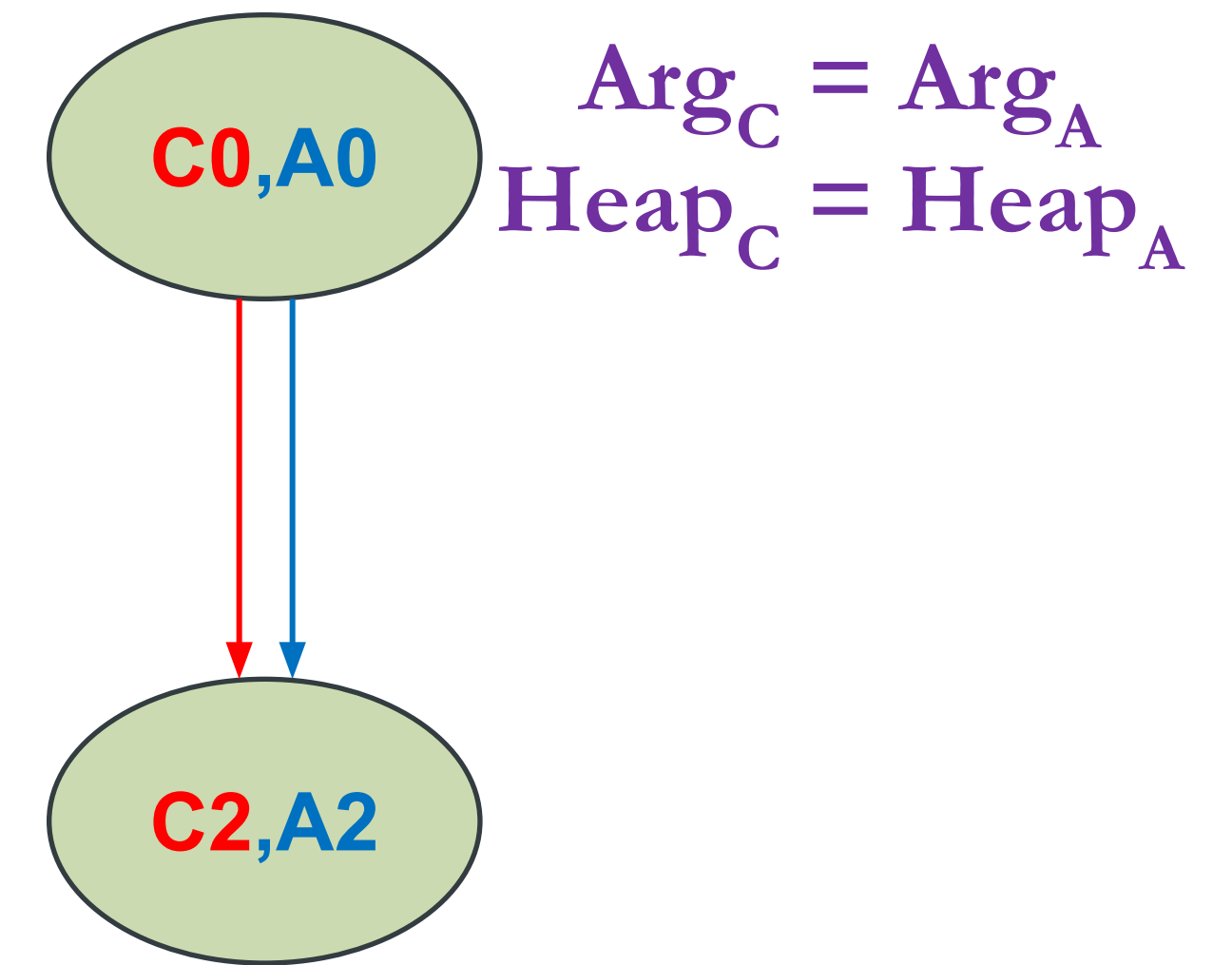
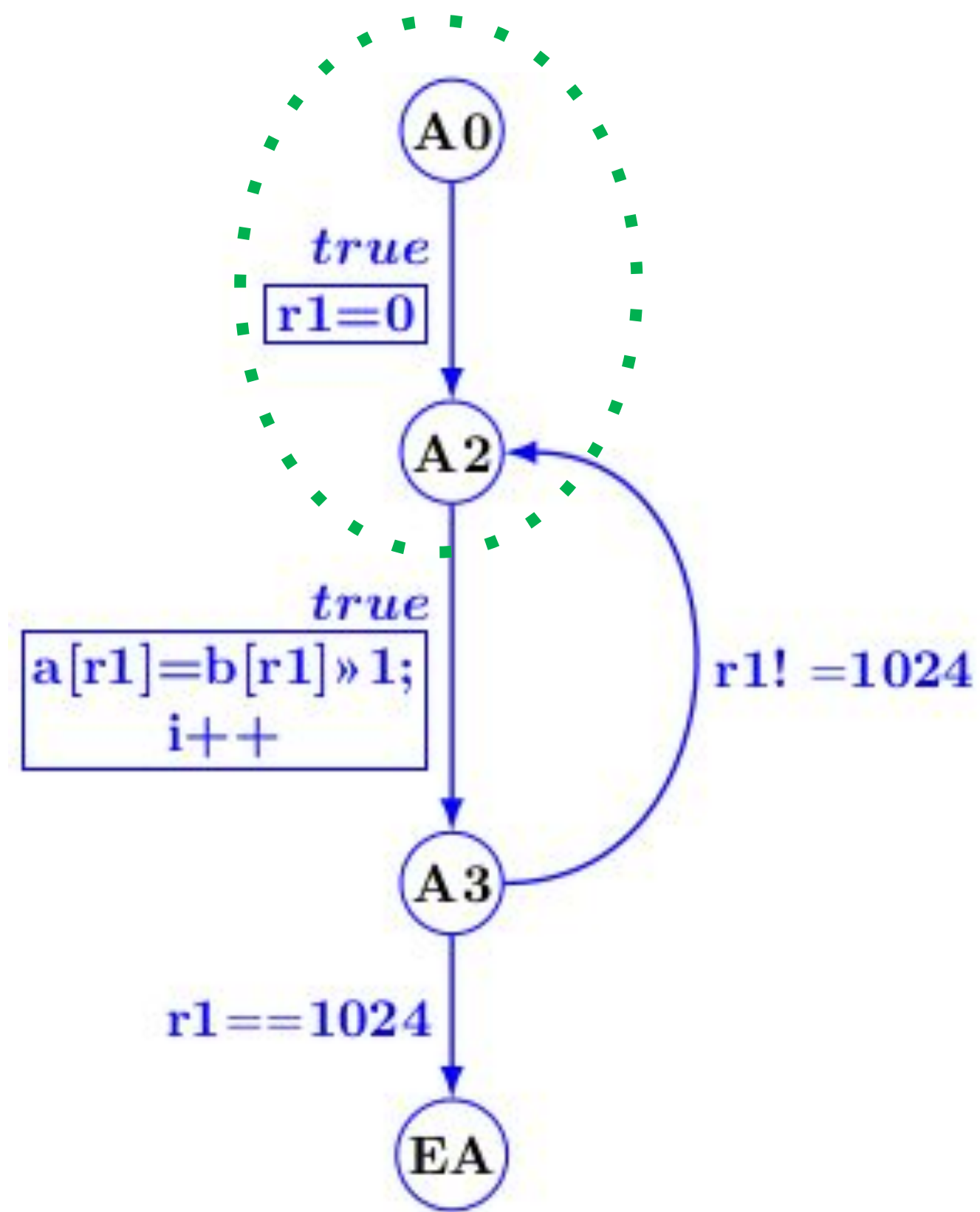
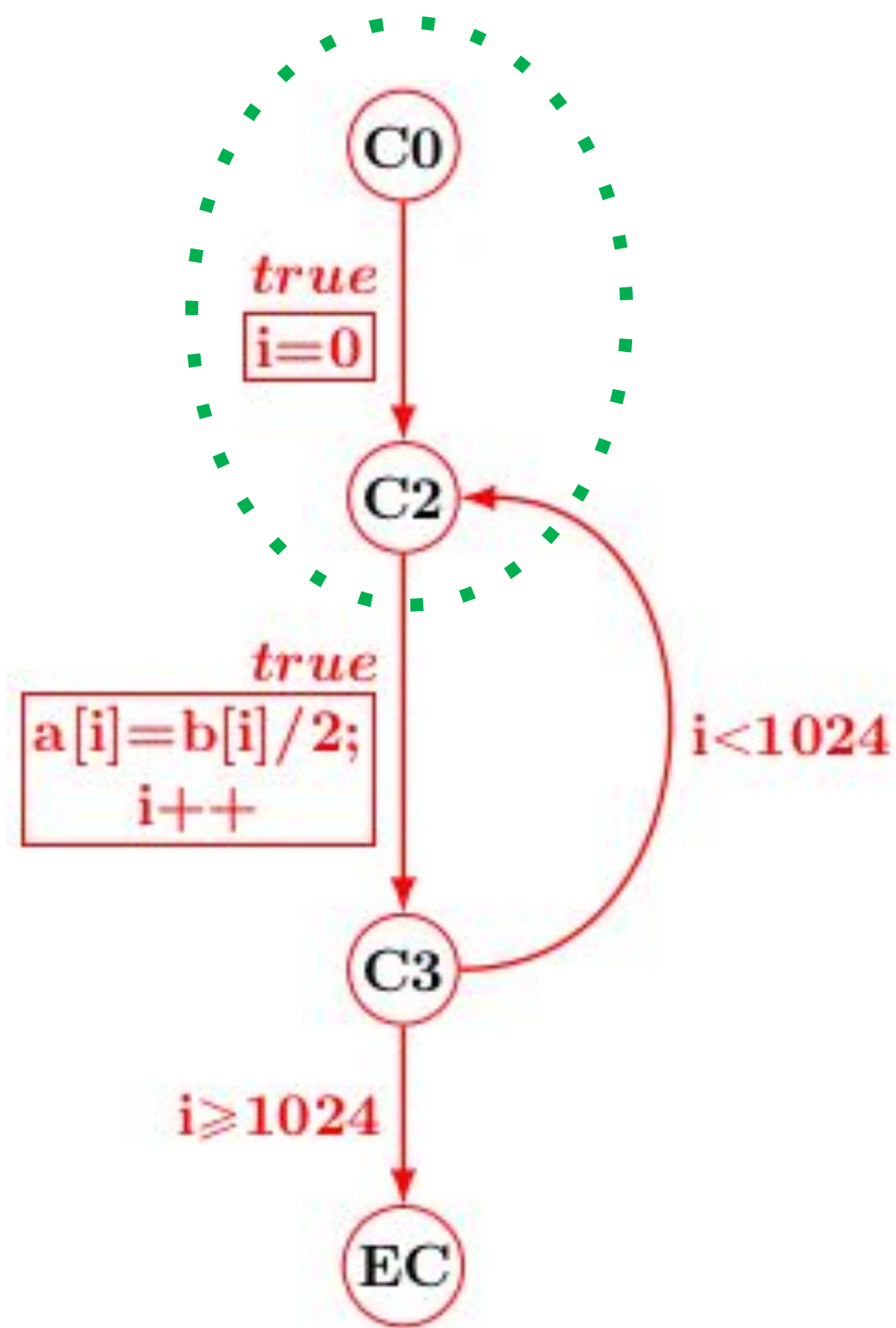
# Product Program Construction



Product CFG

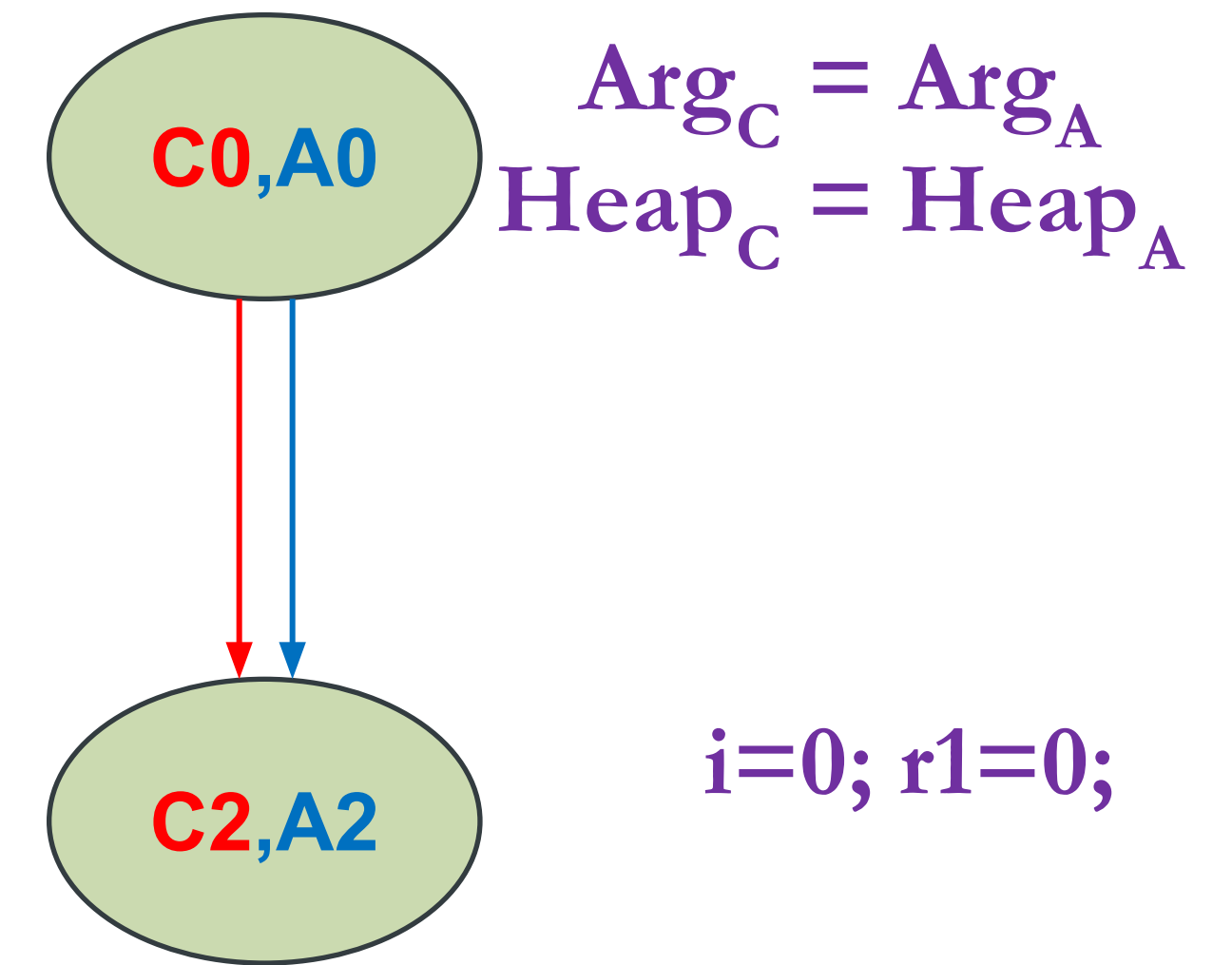
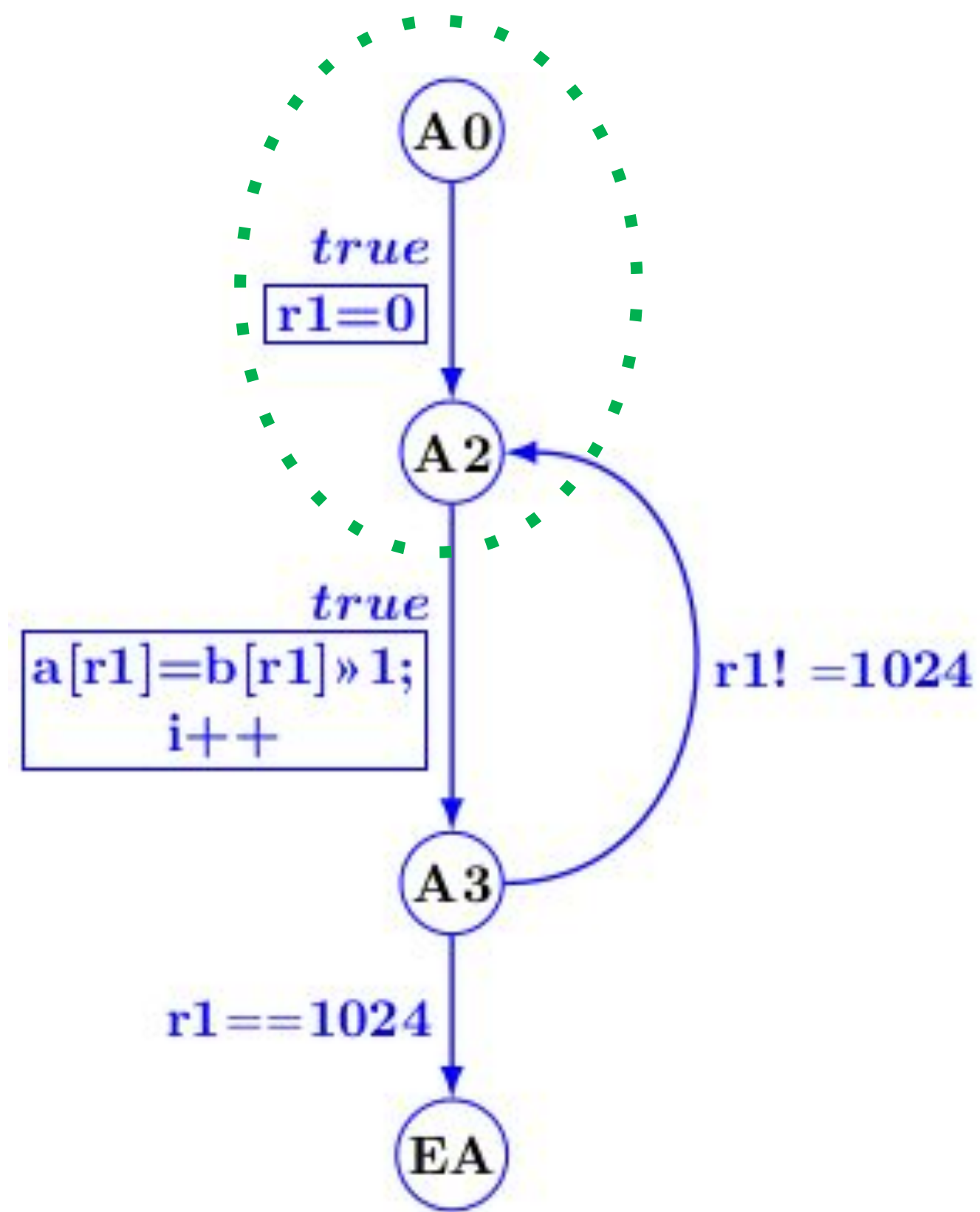
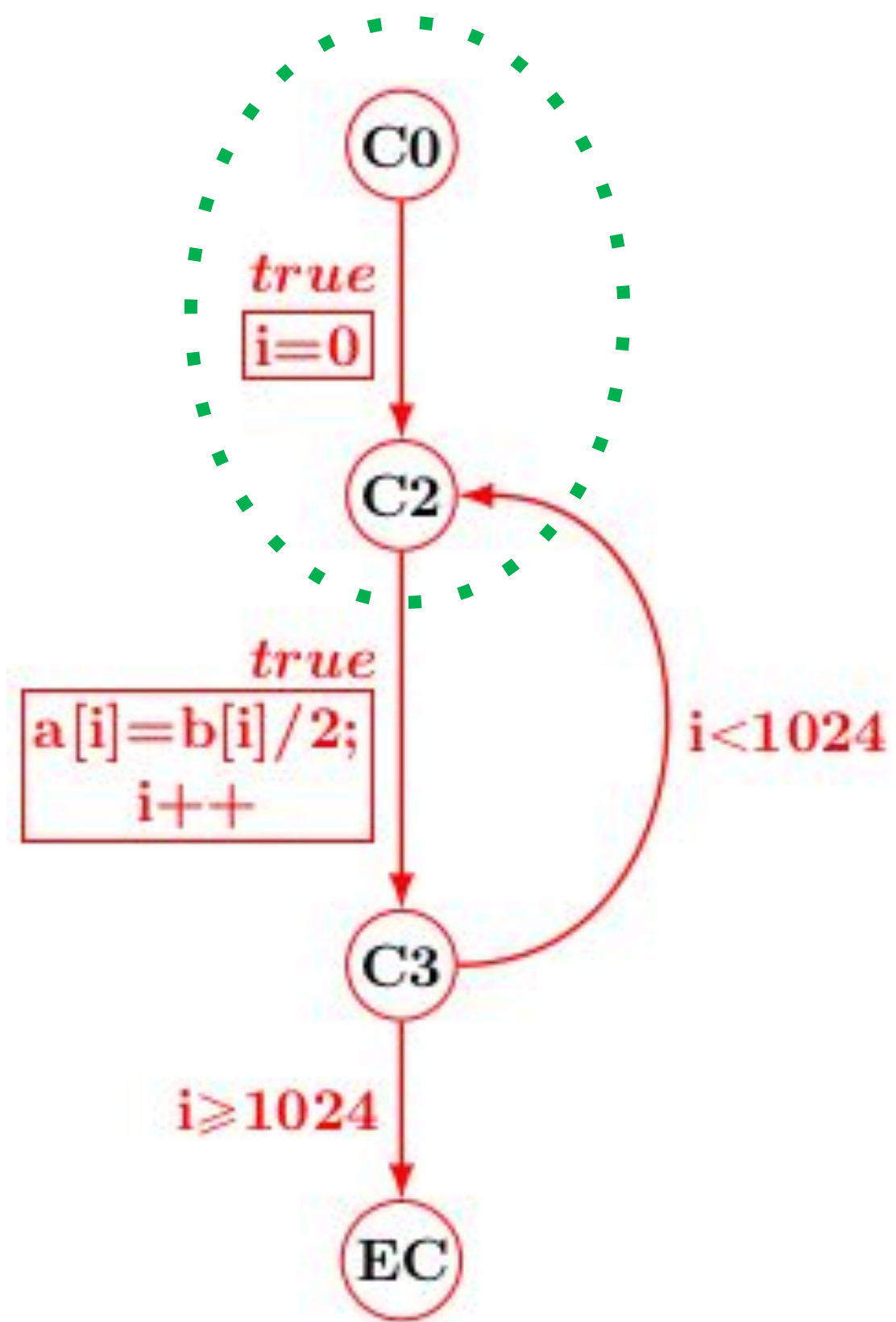
# Product Program Construction

Product CFG



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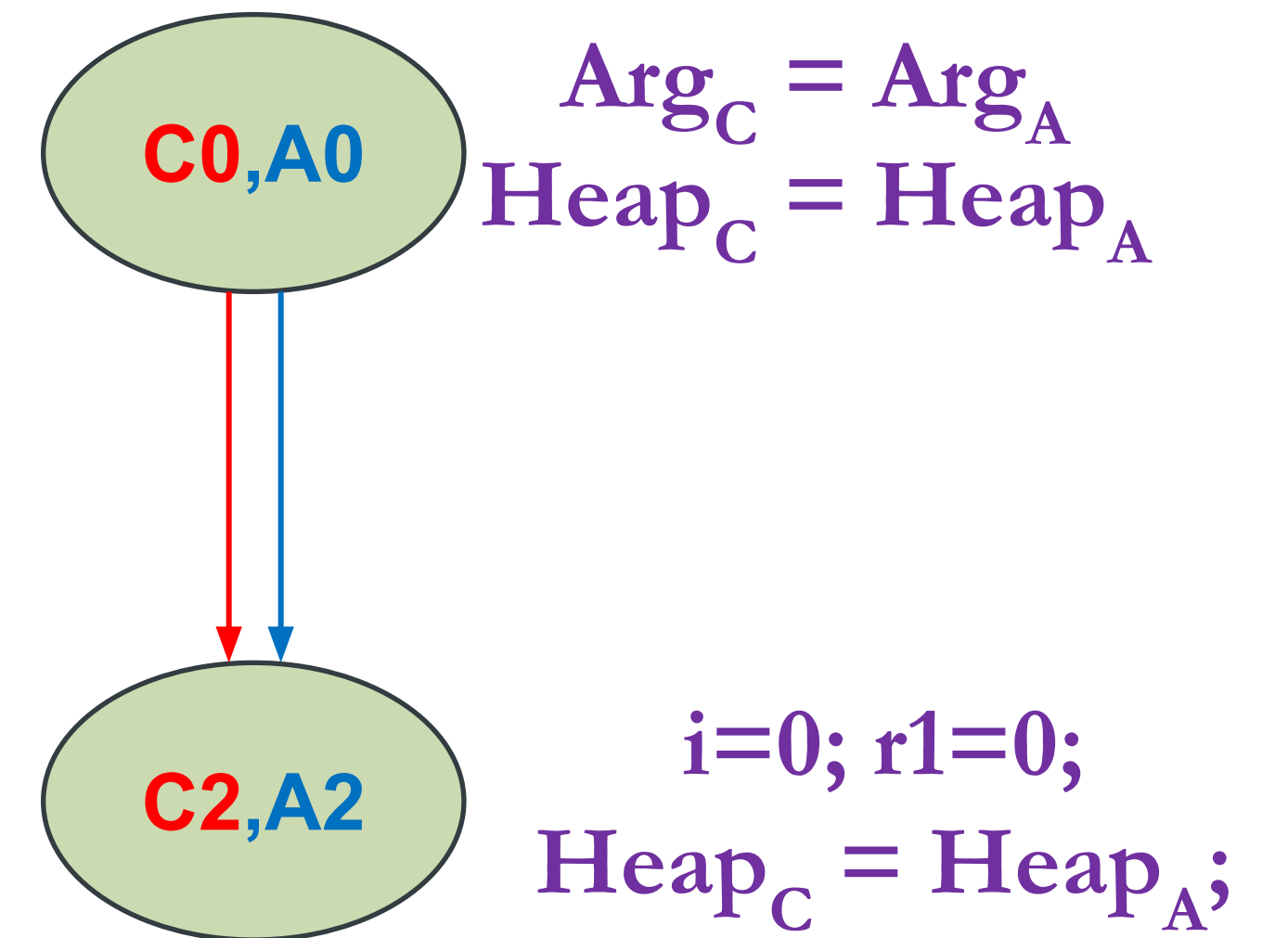
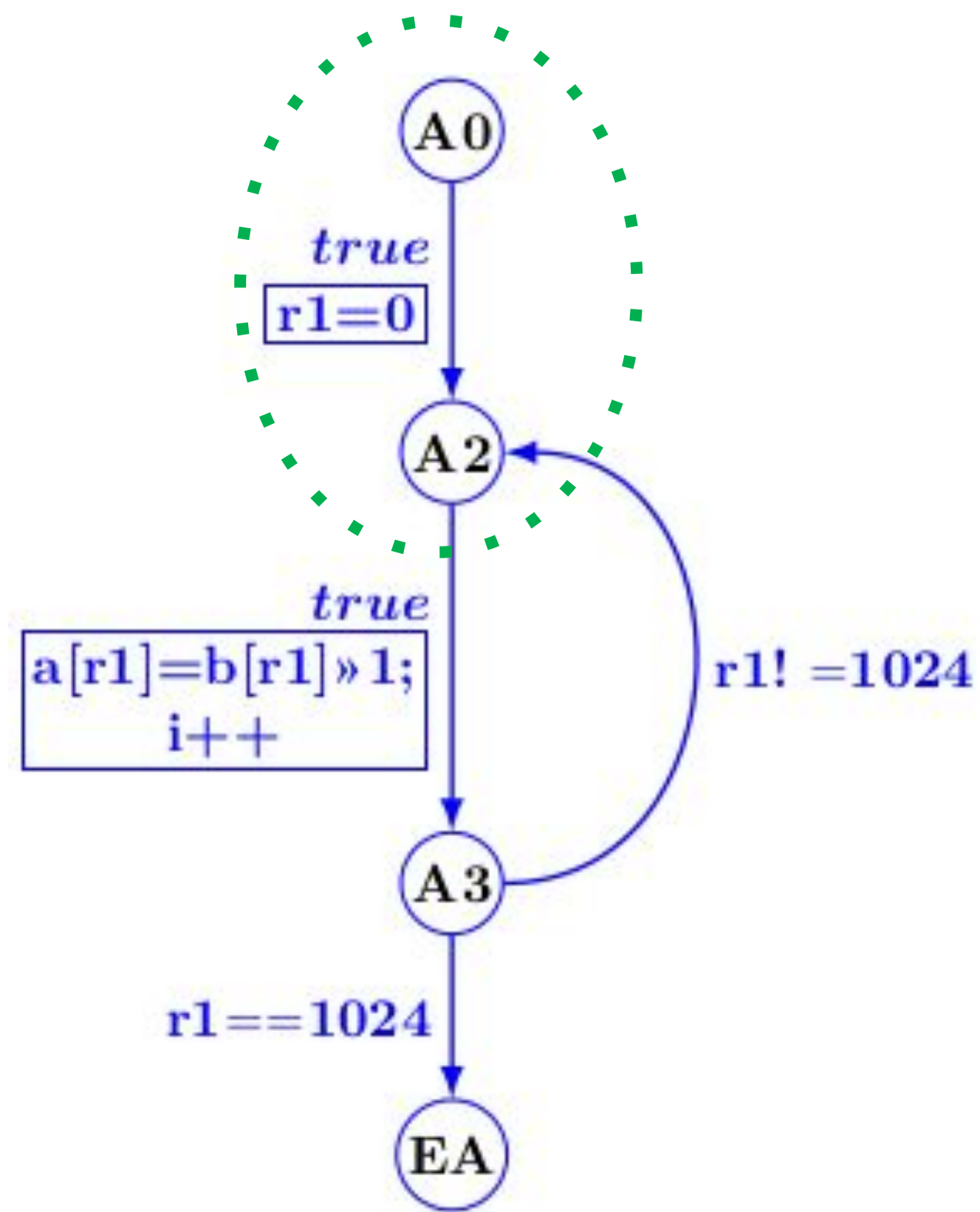
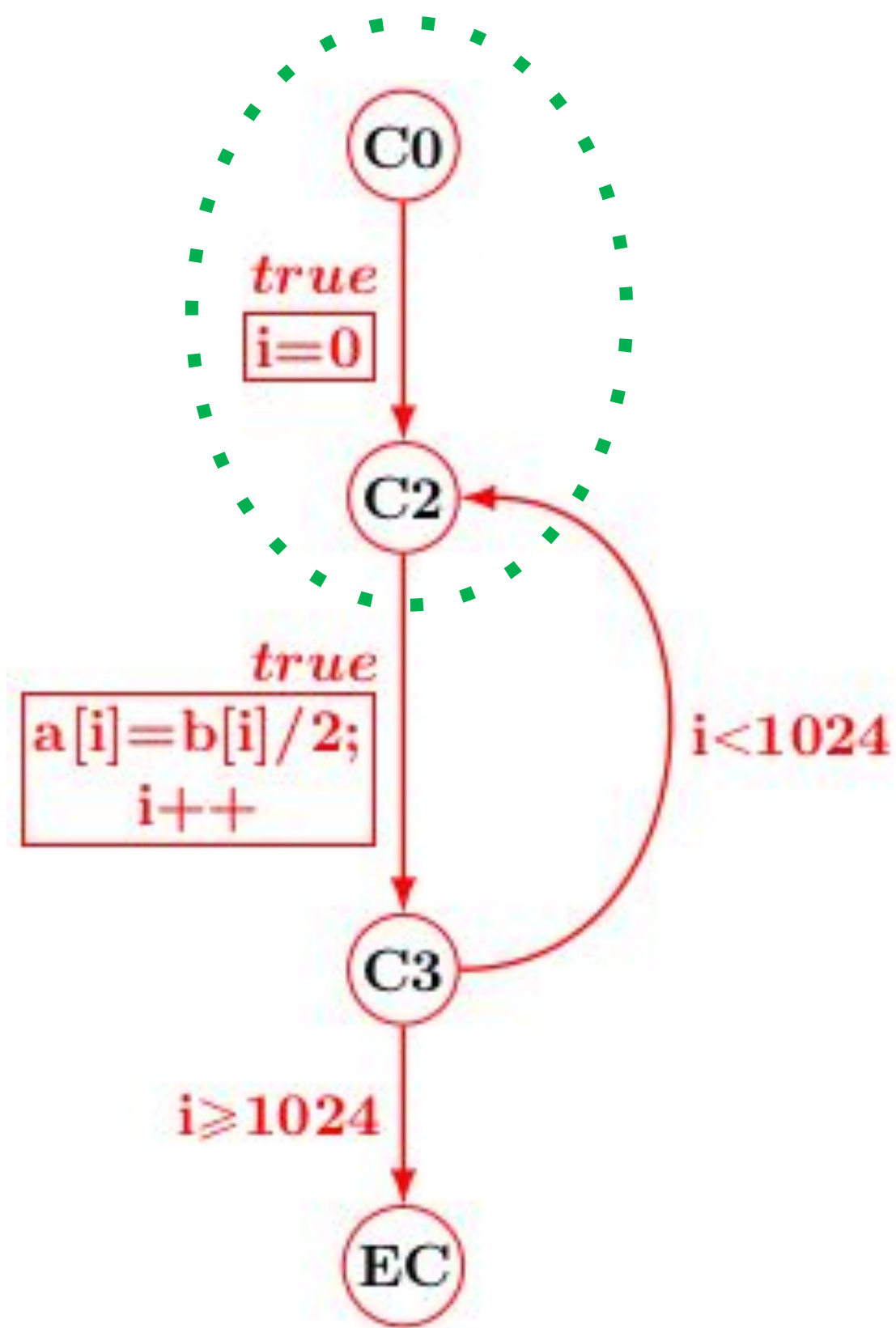
Product CFG





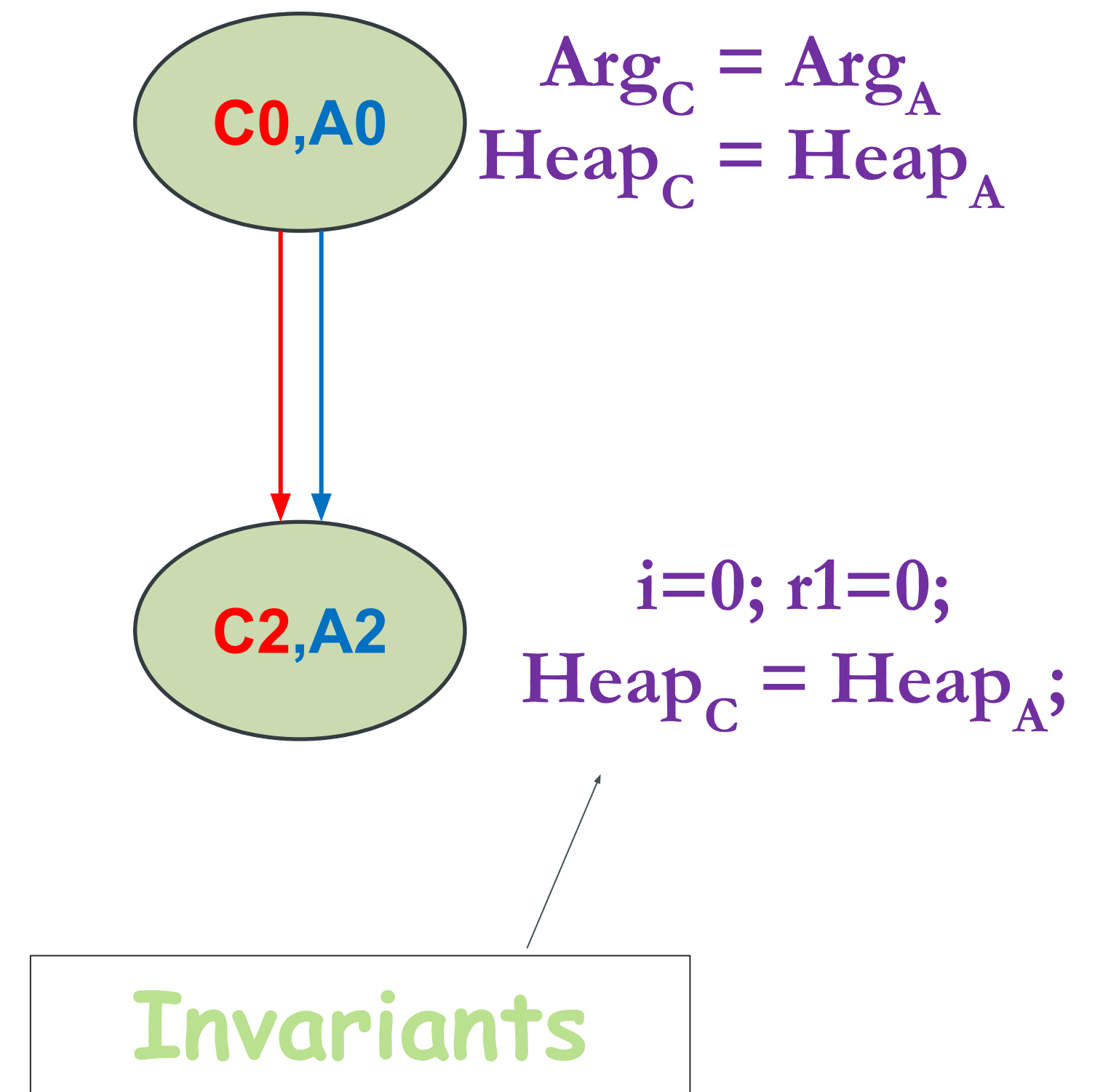
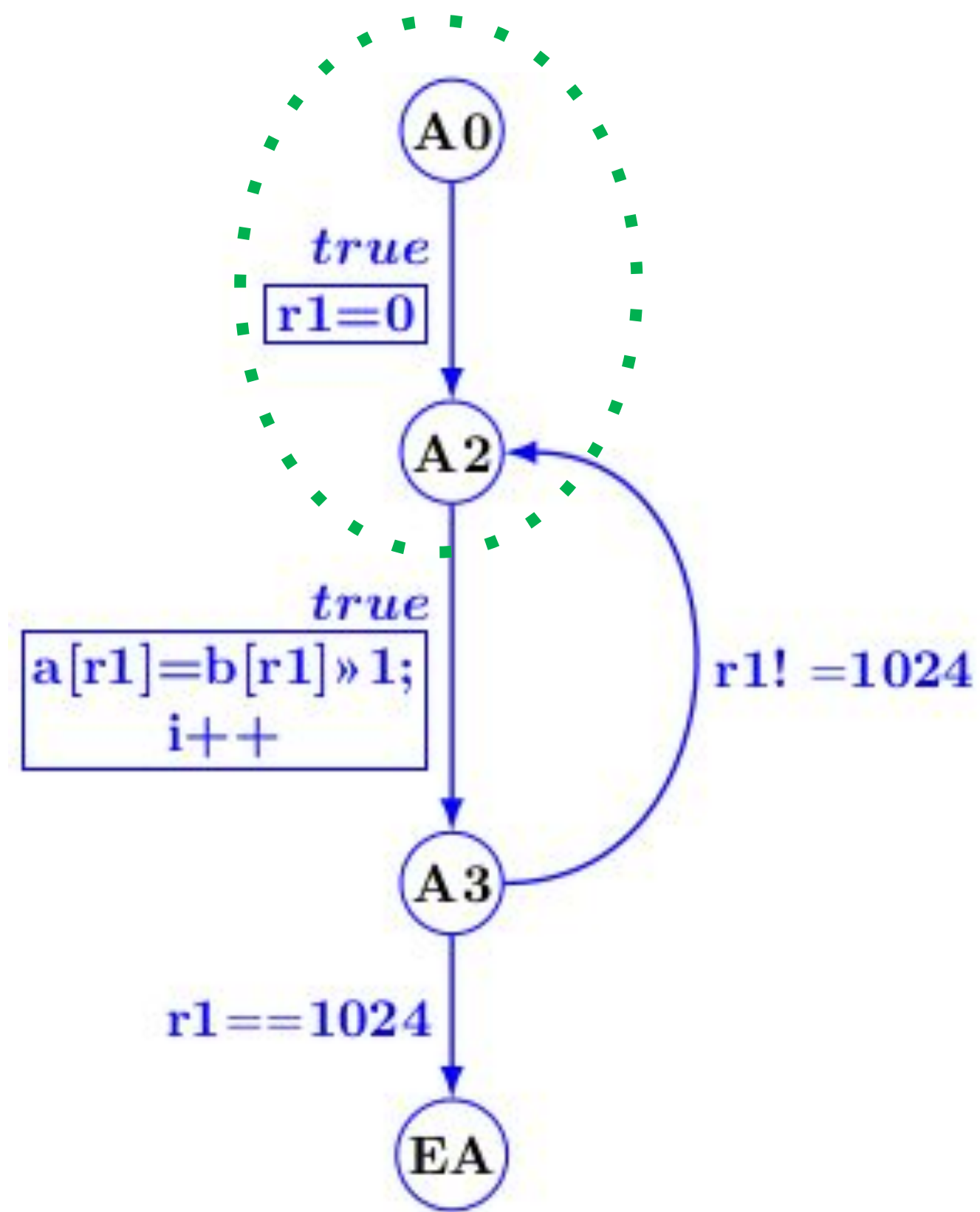
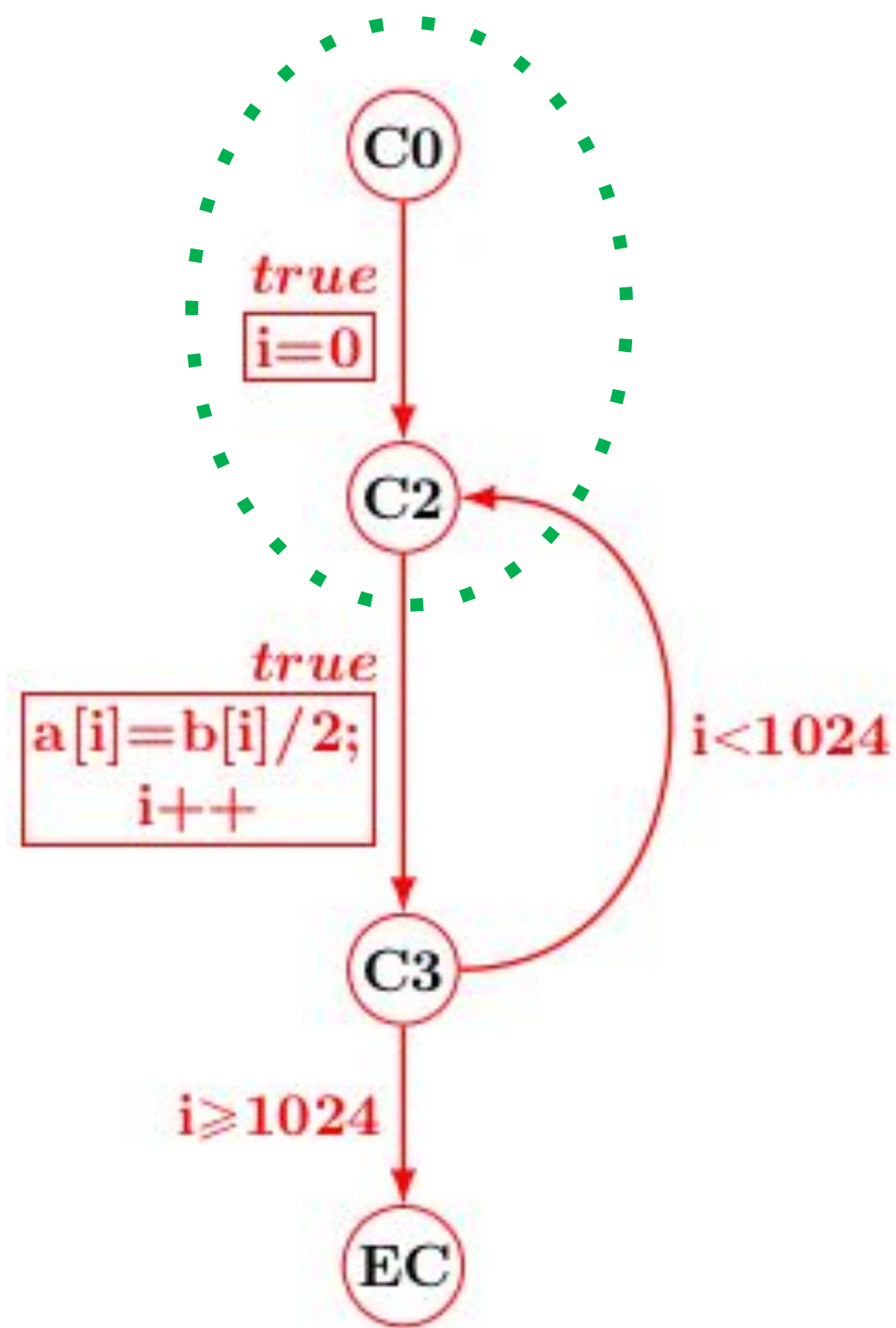
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Product CFG



# Product Program Construction

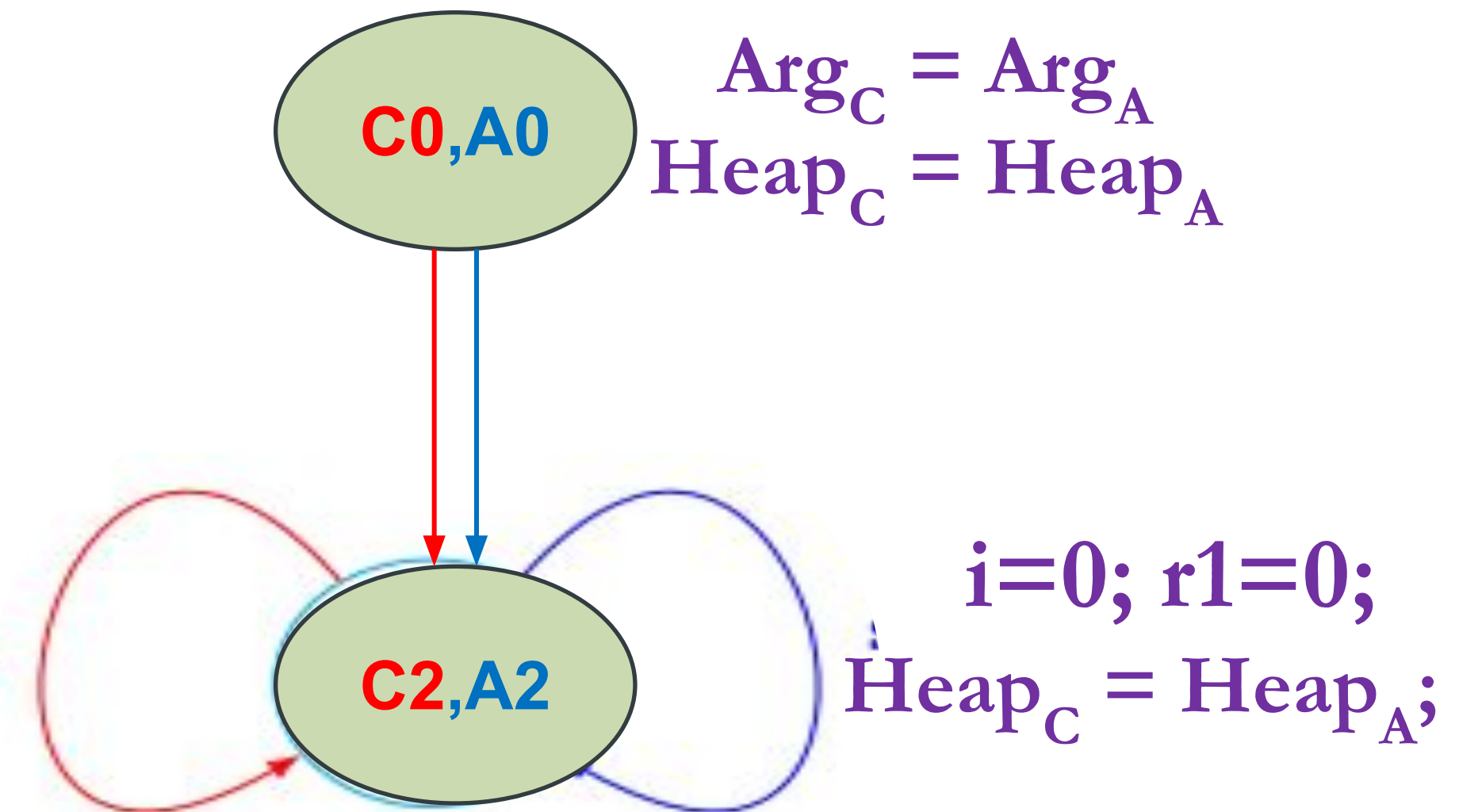
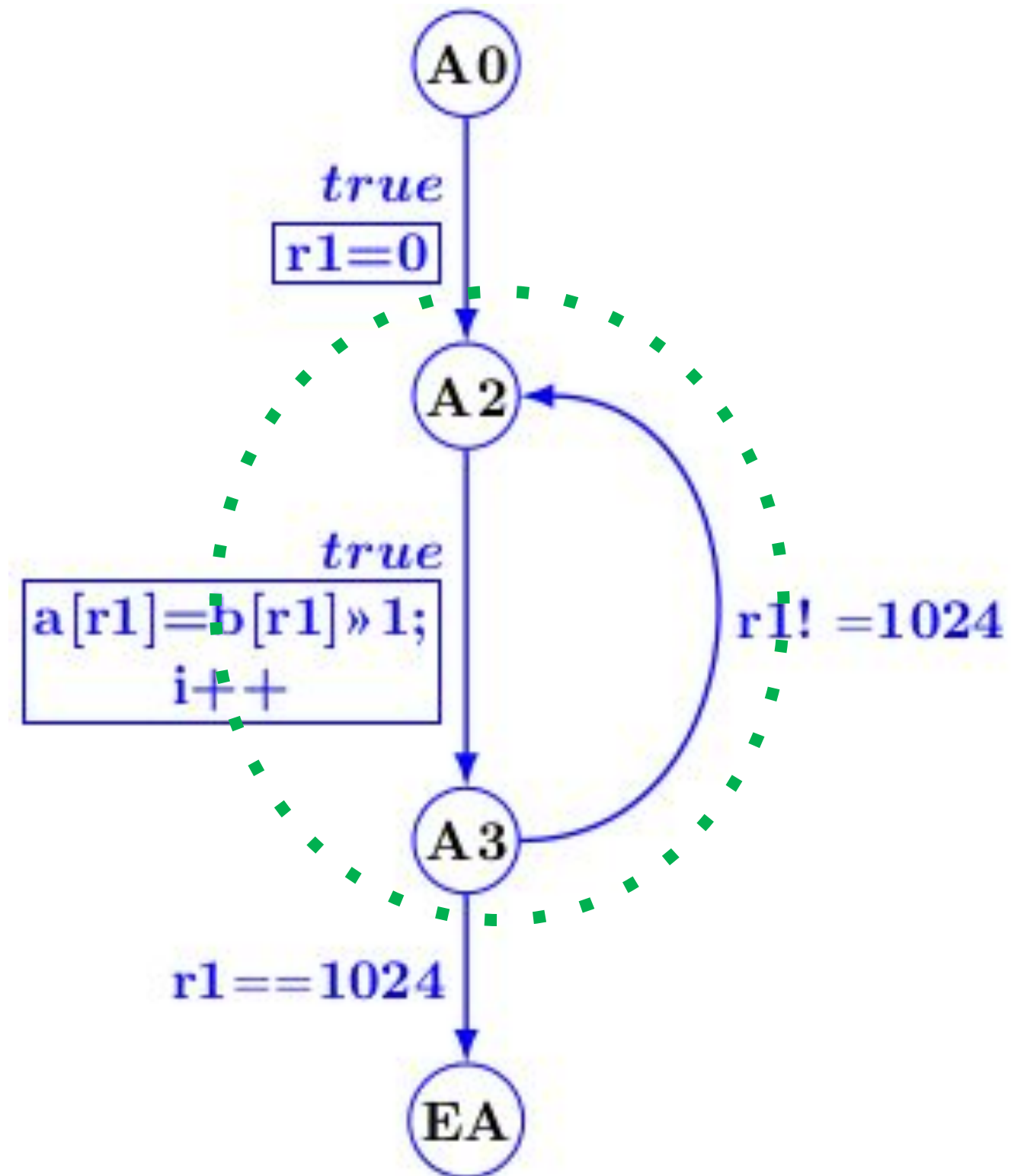
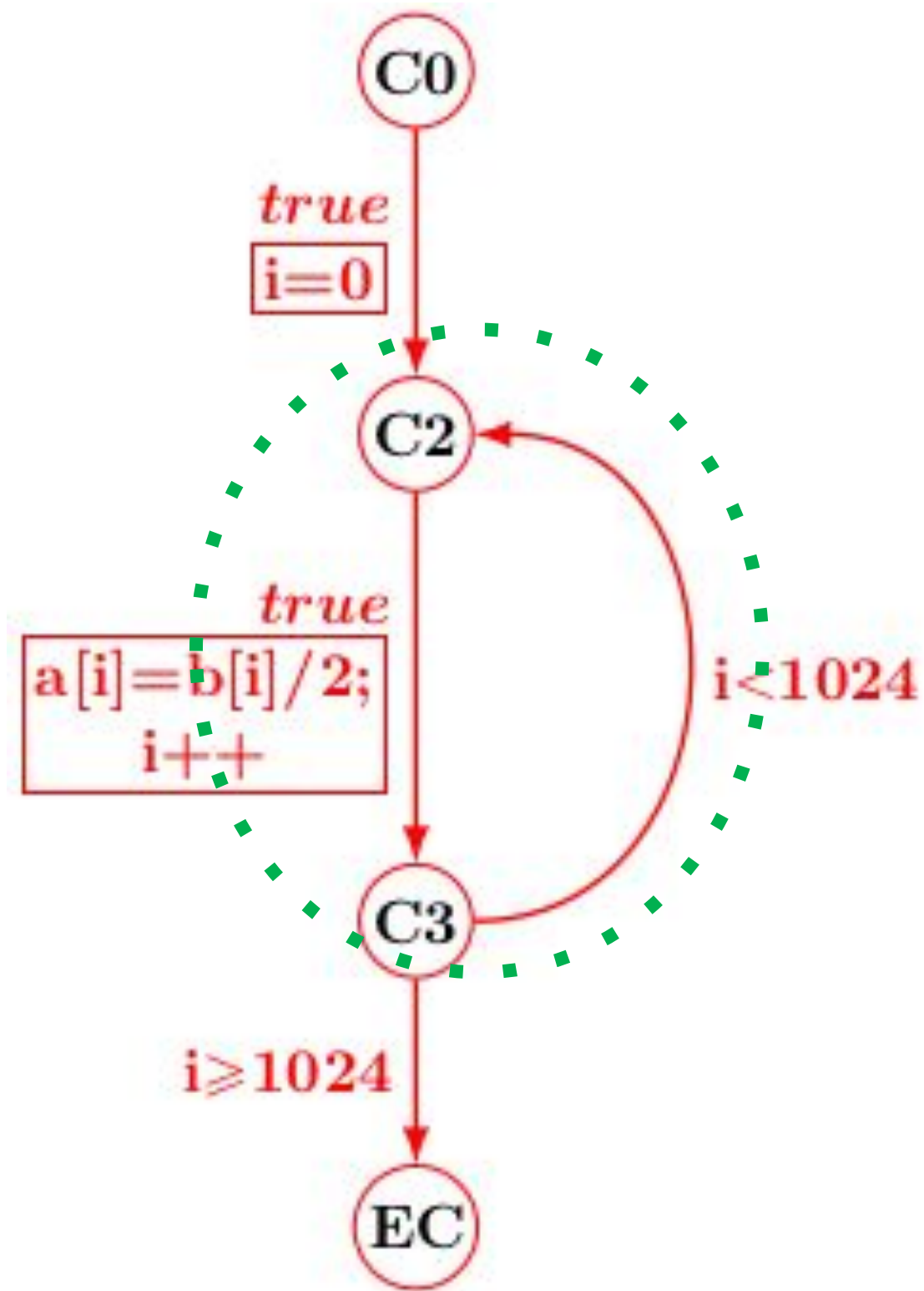
Product CFG





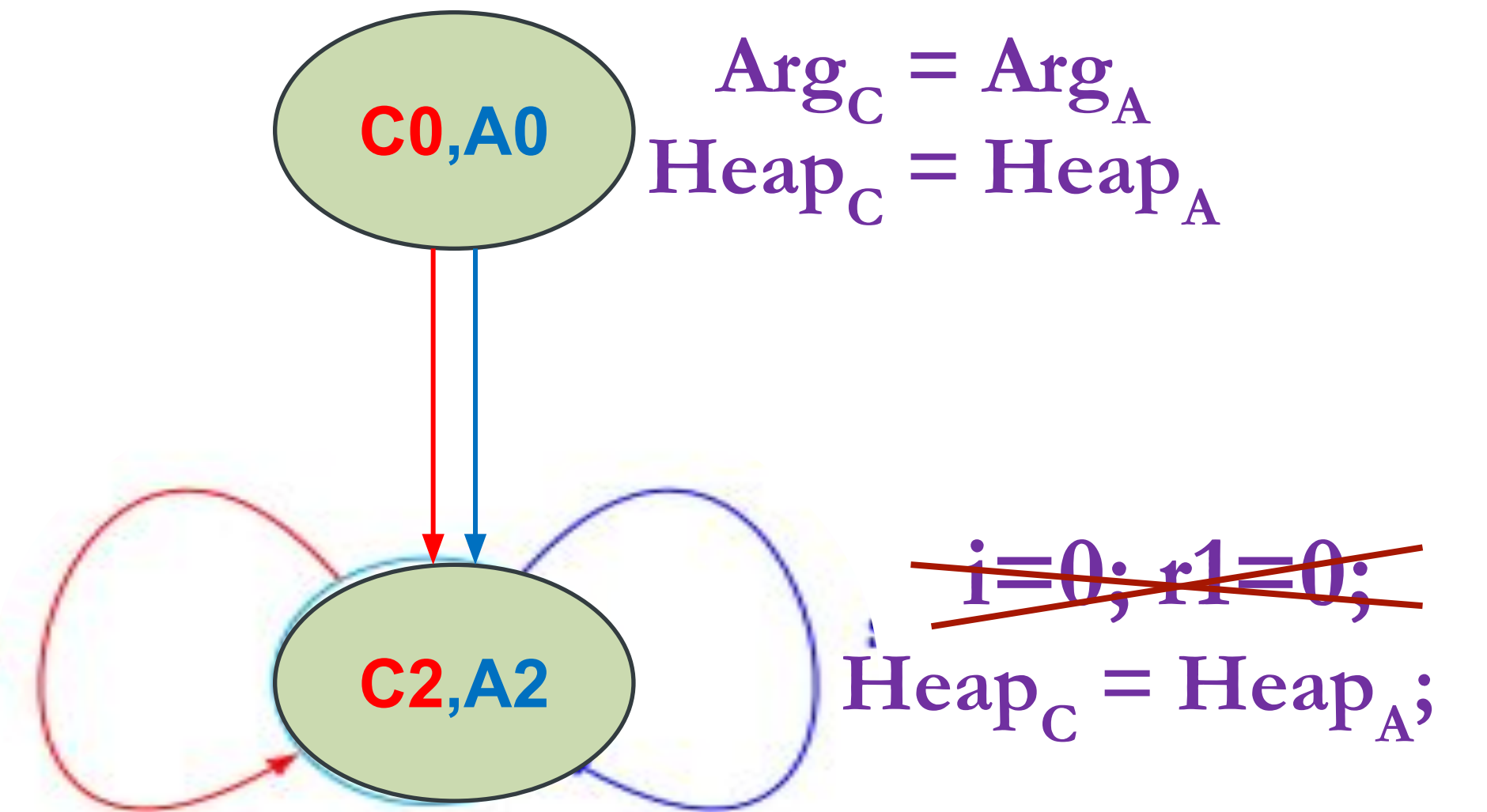
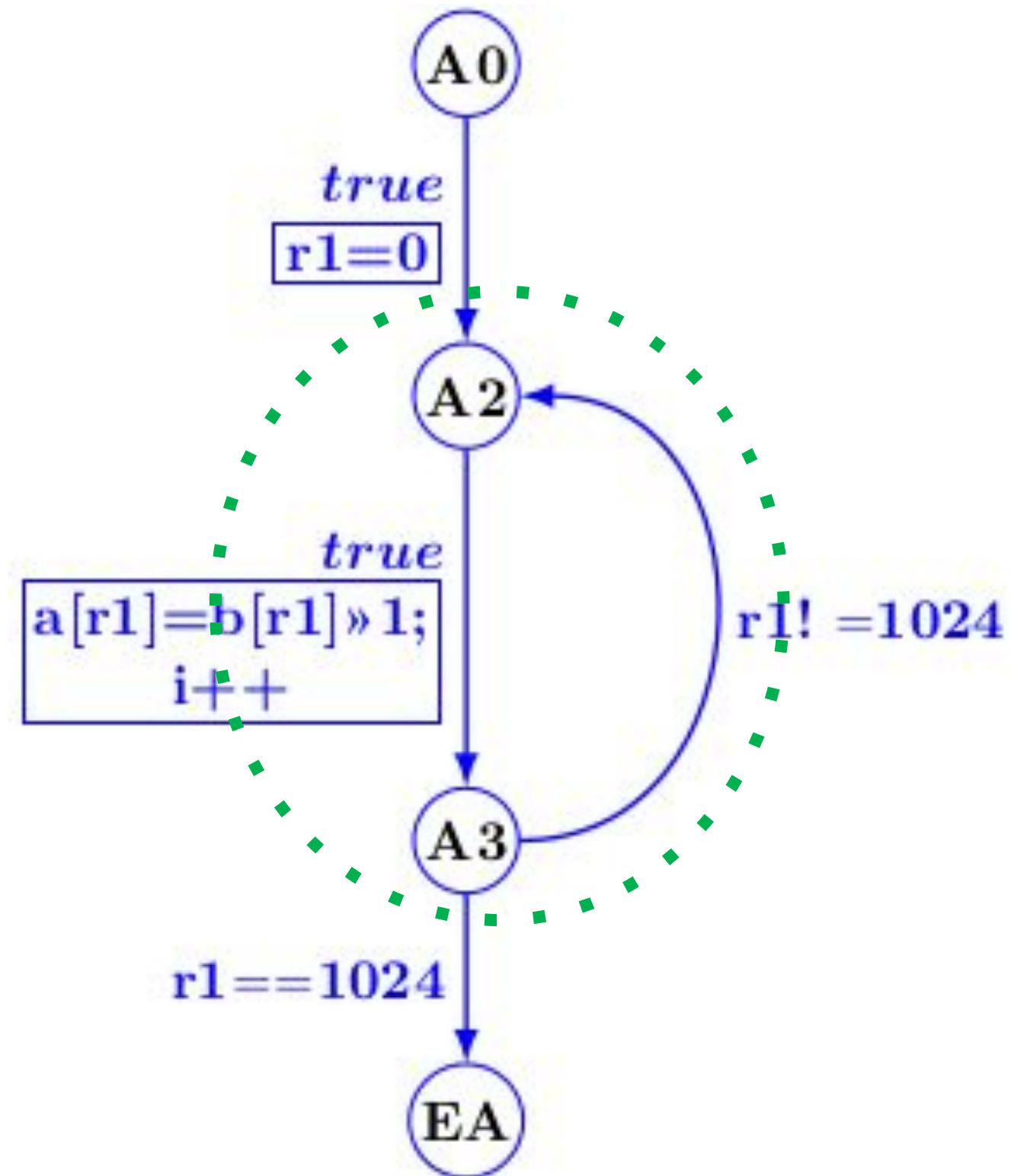
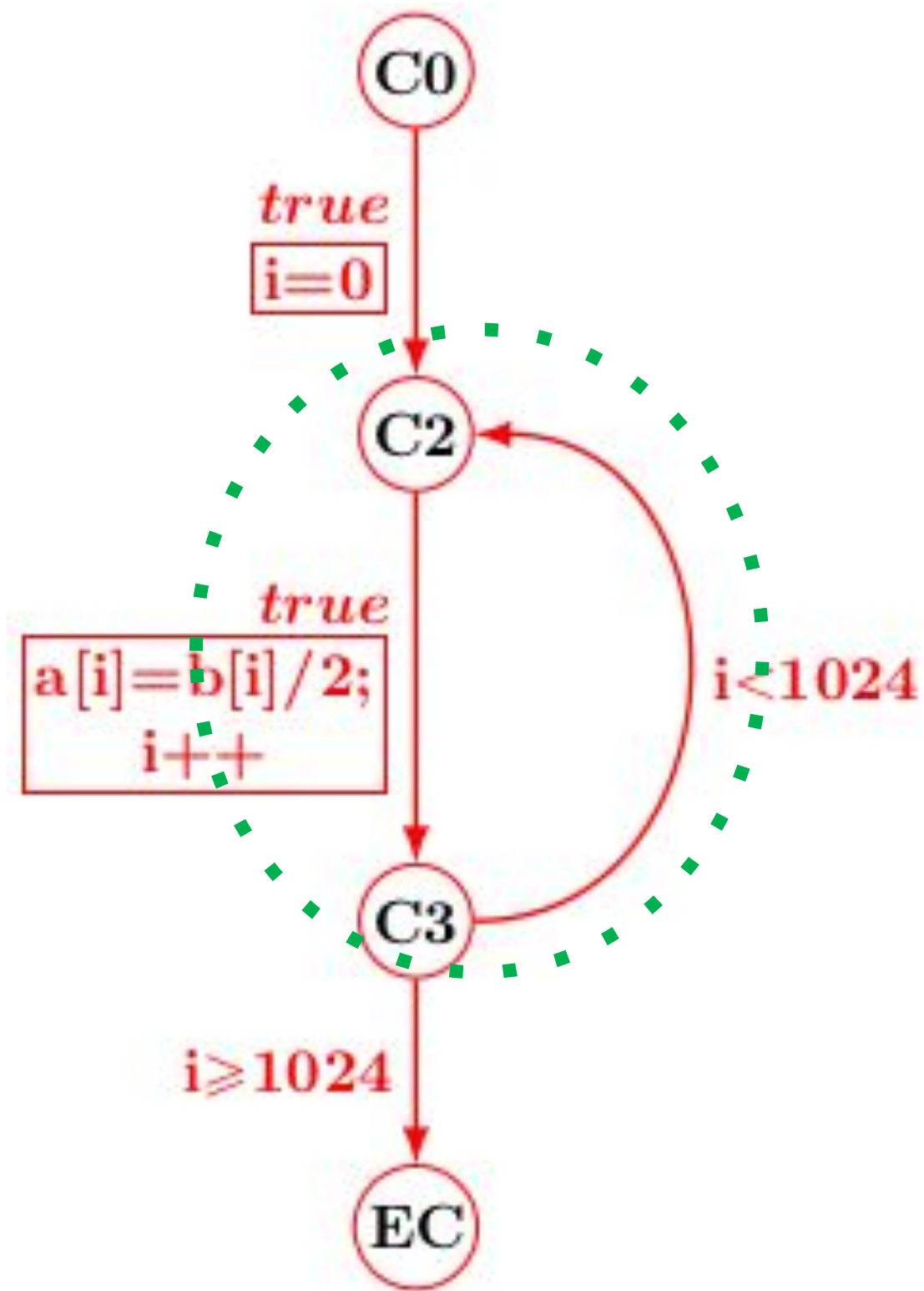
# Product Program Construction

Product CFG



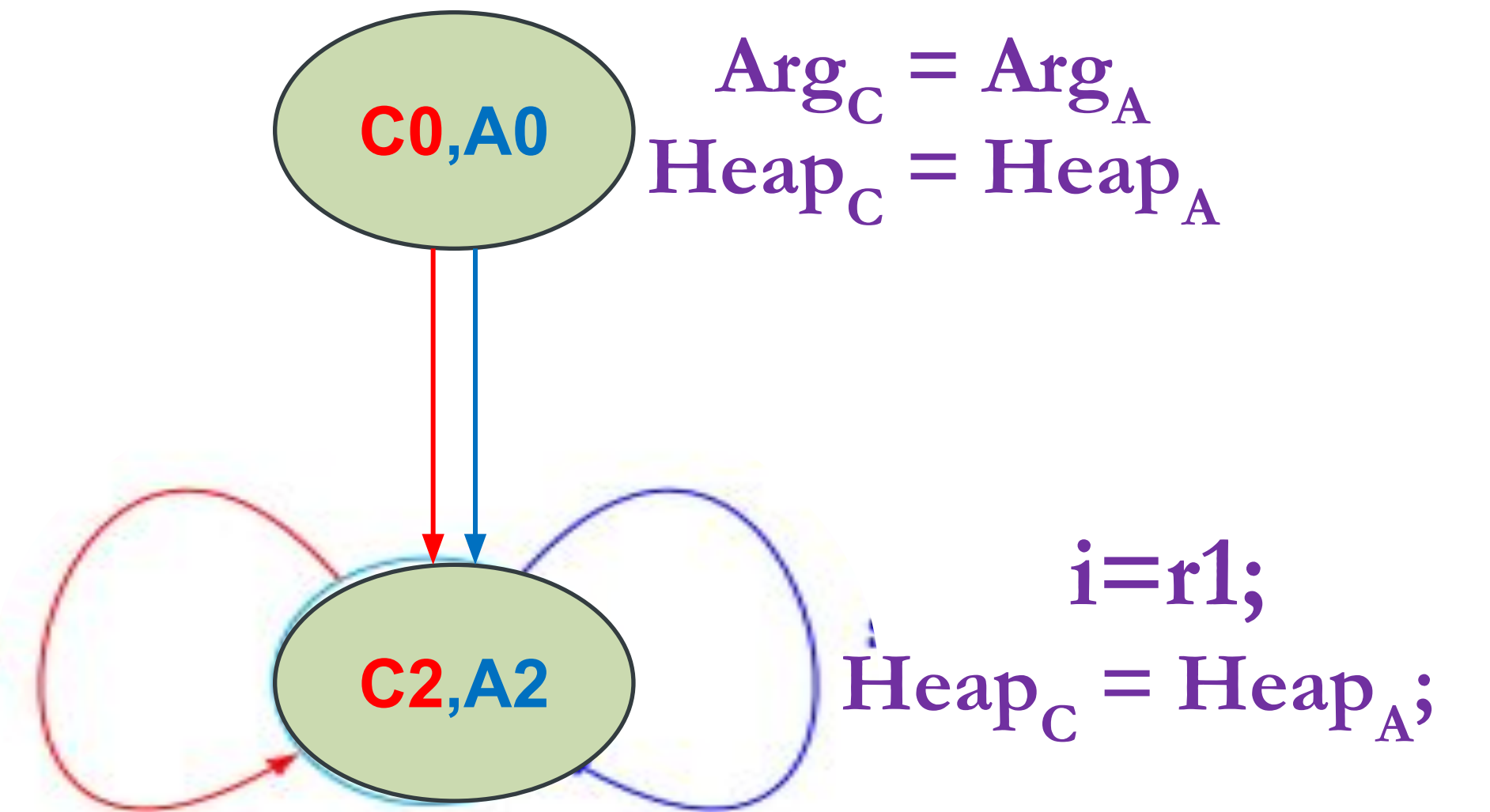
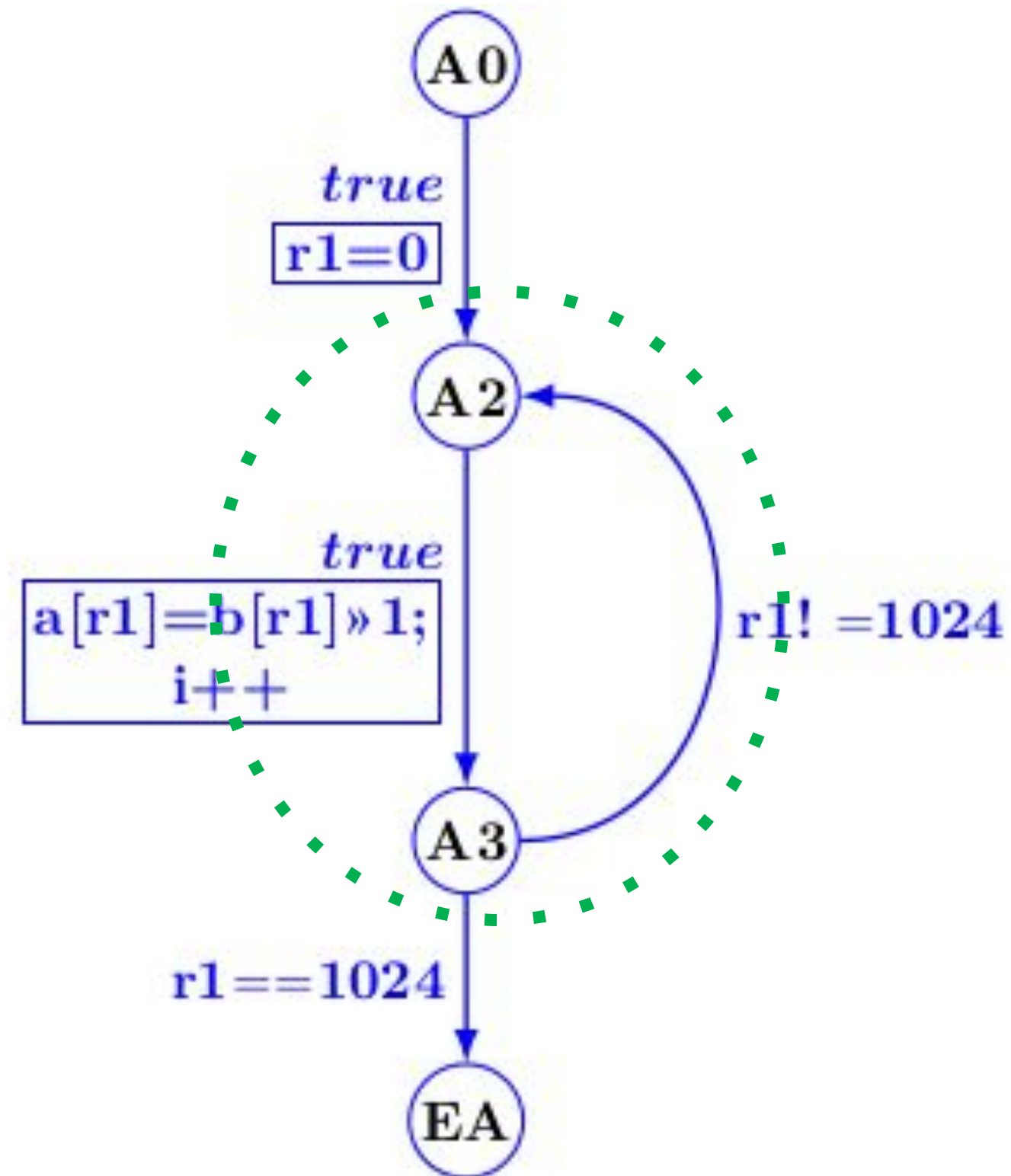
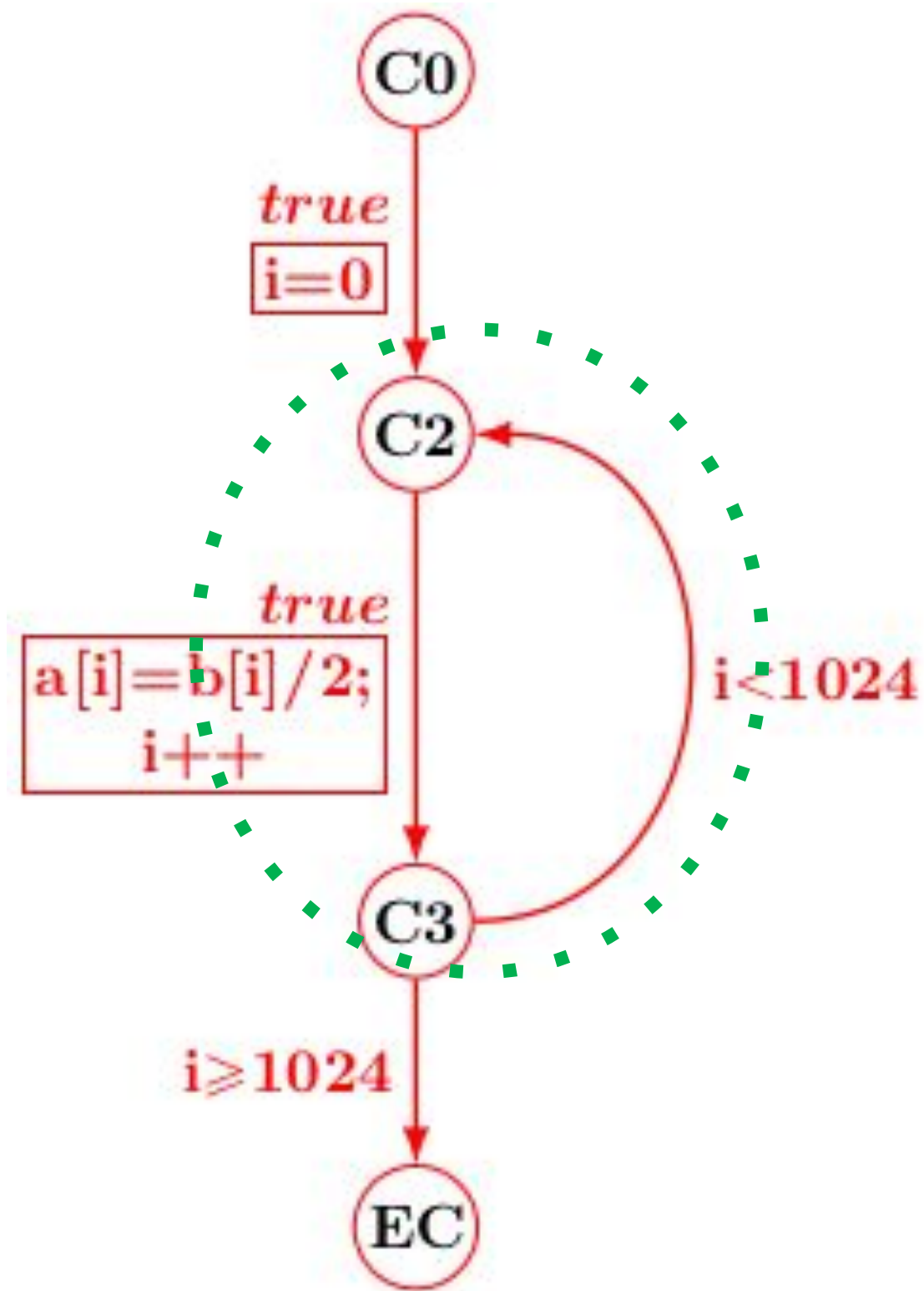
# Product Program Construction

Product CFG



# Product Program Construction

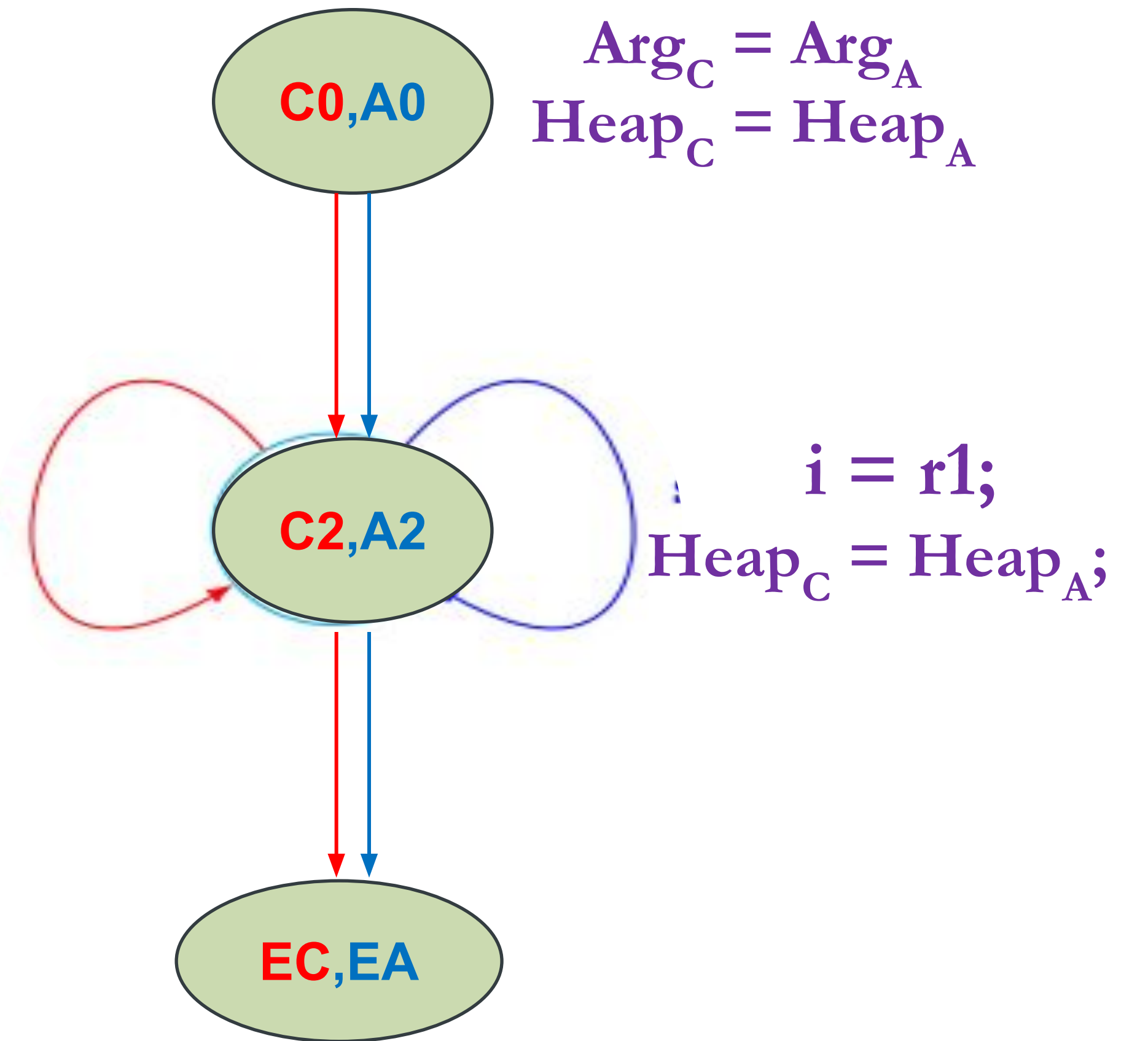
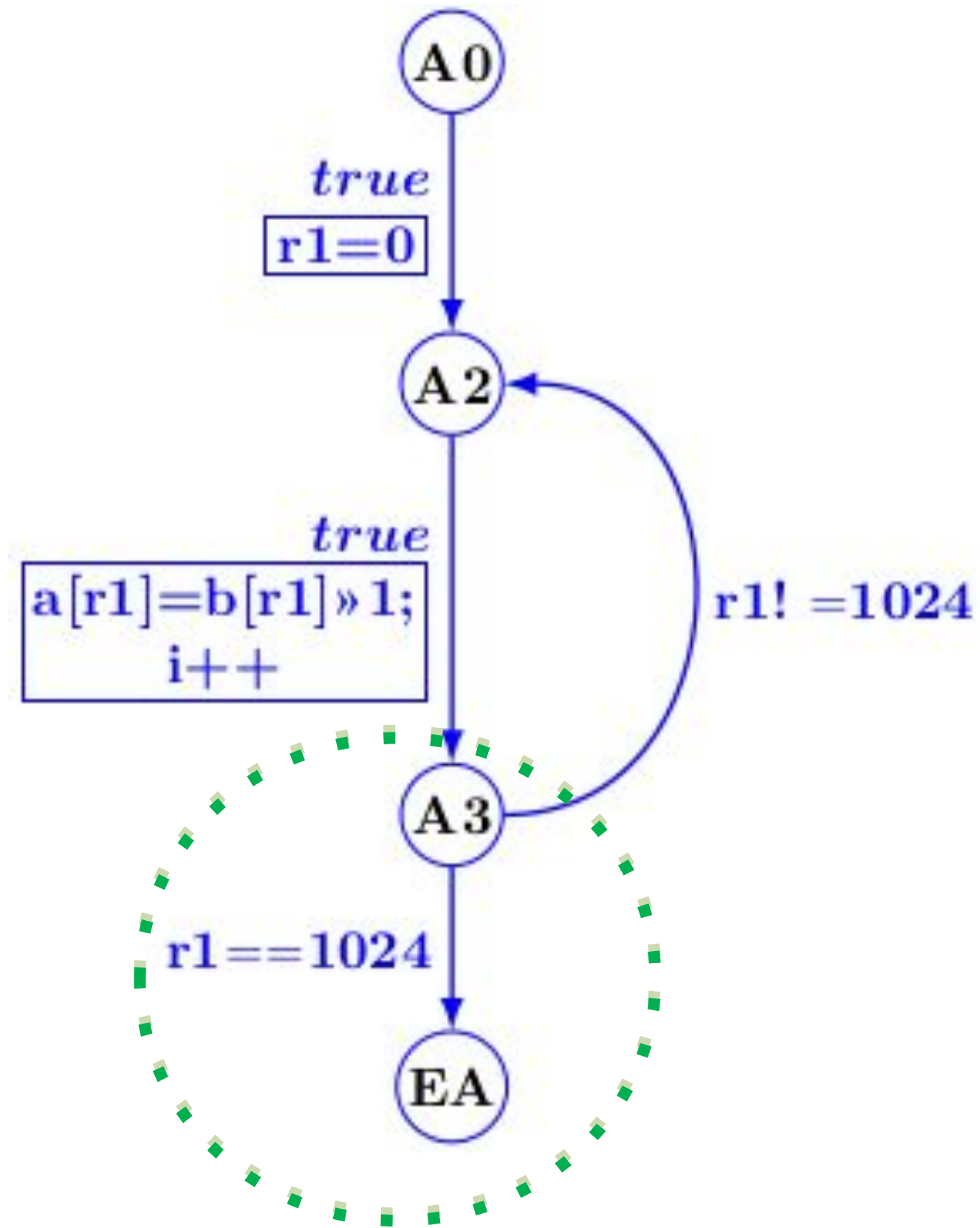
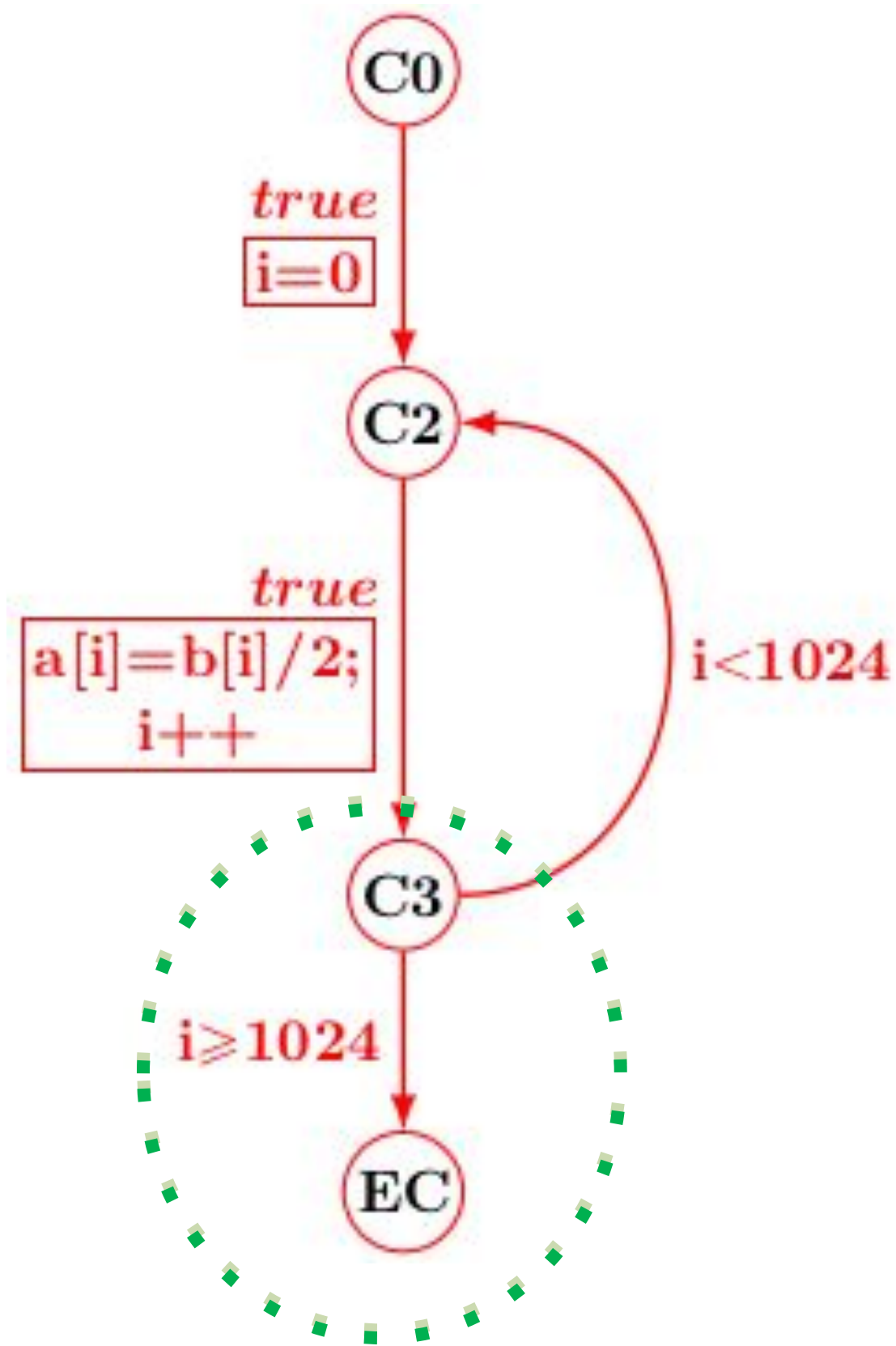
Product CFG



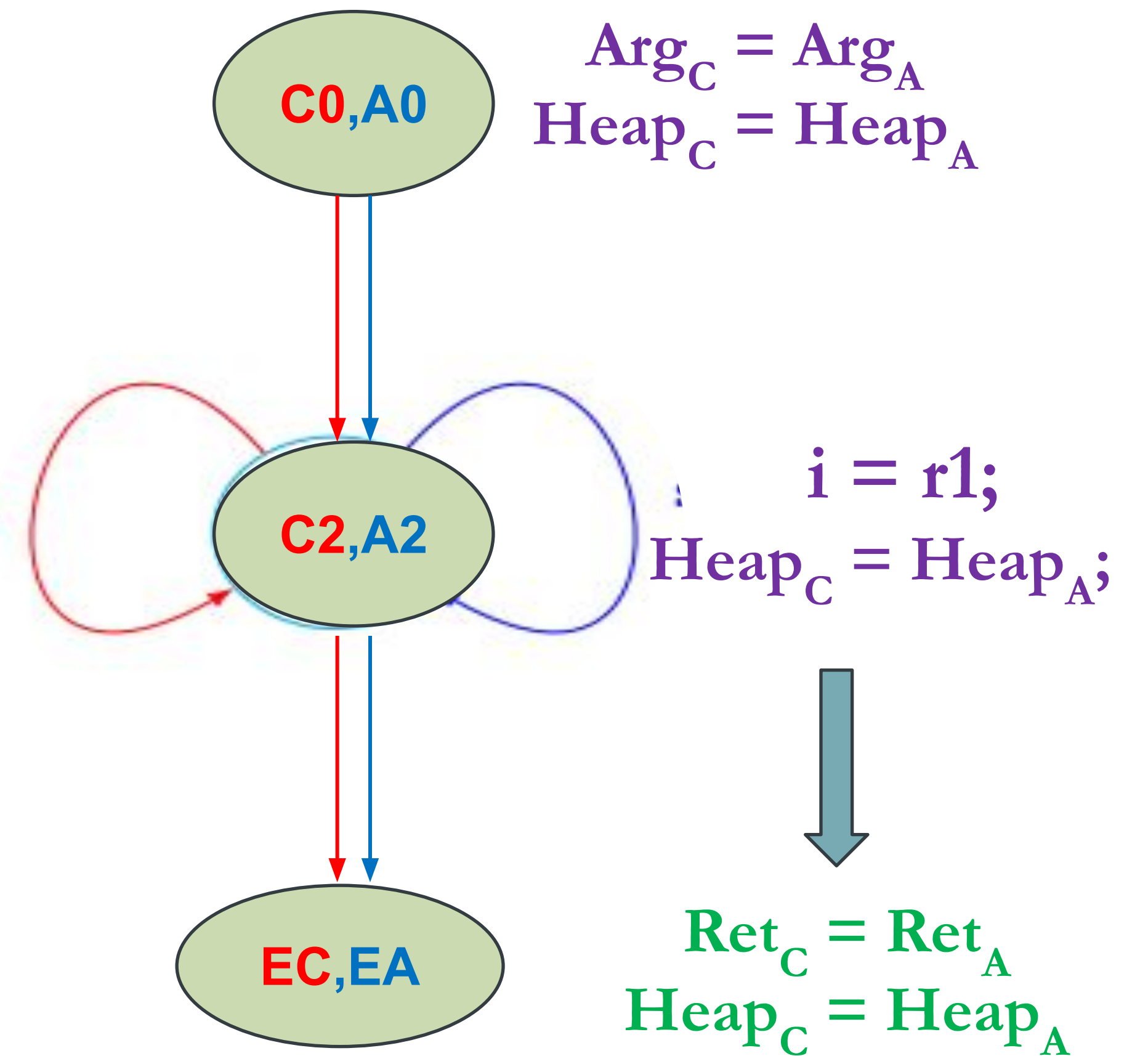
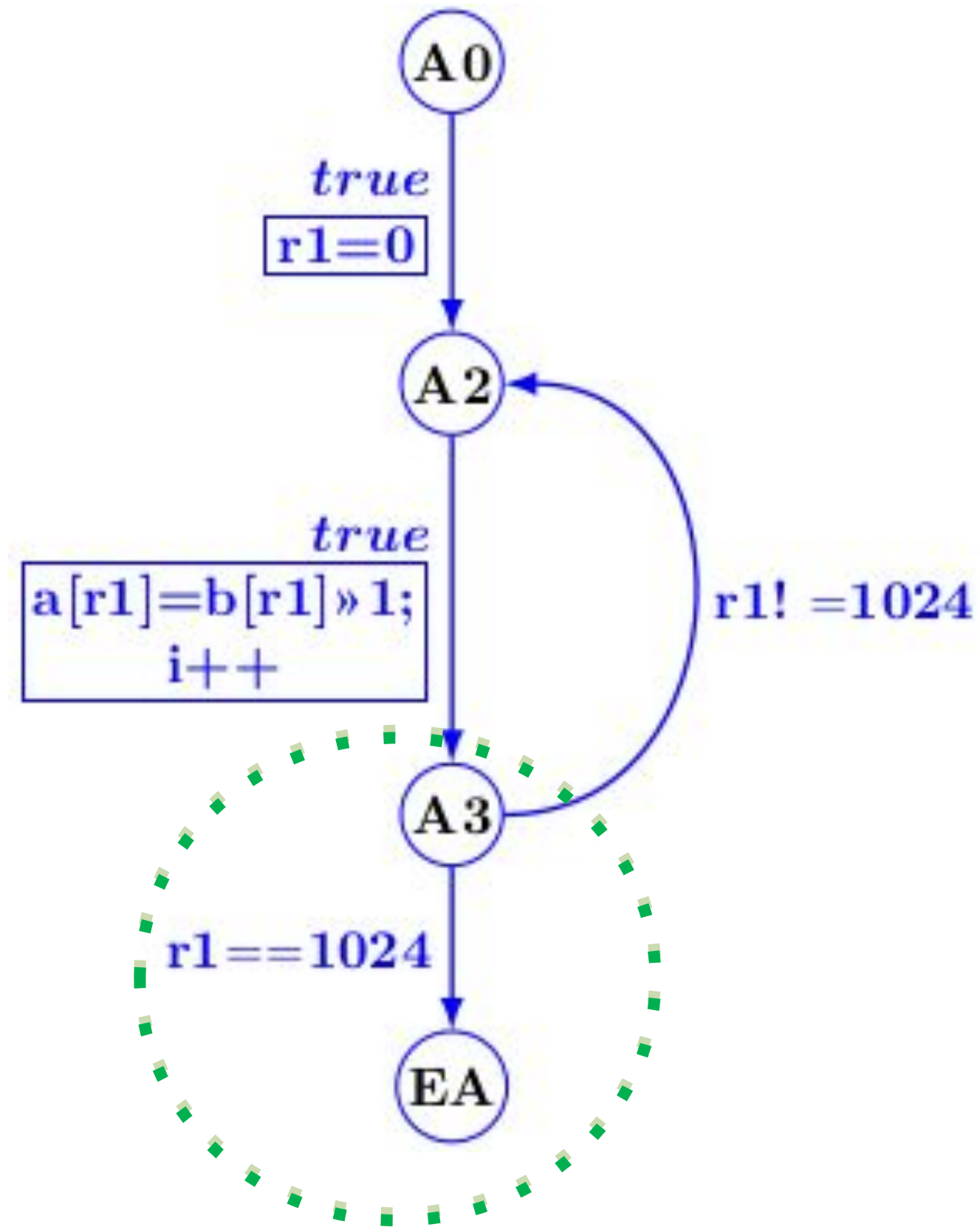
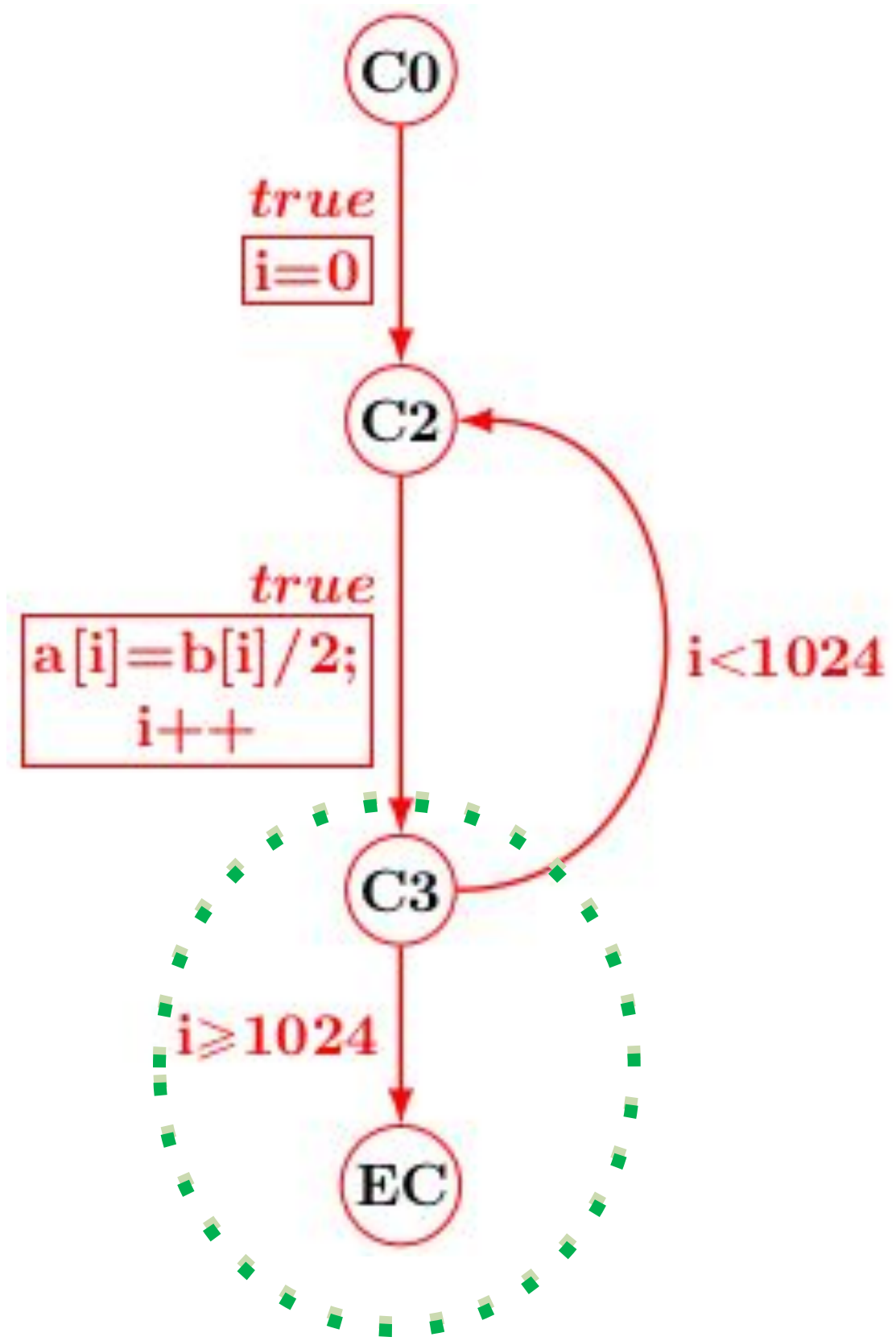


# Product Program Construction

Product CFG

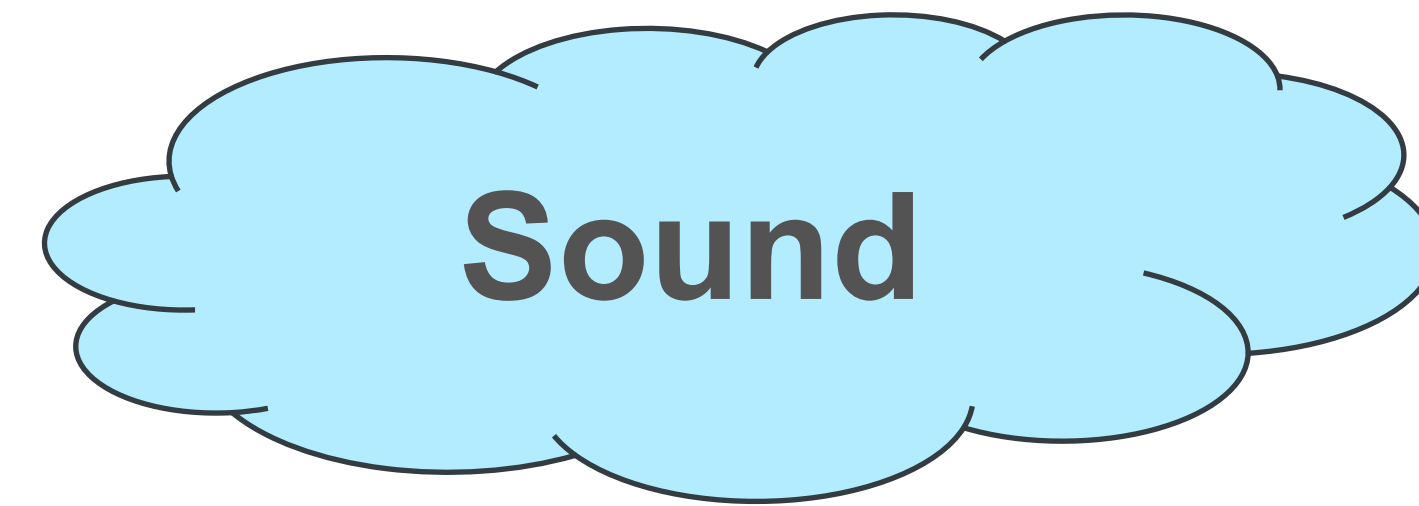
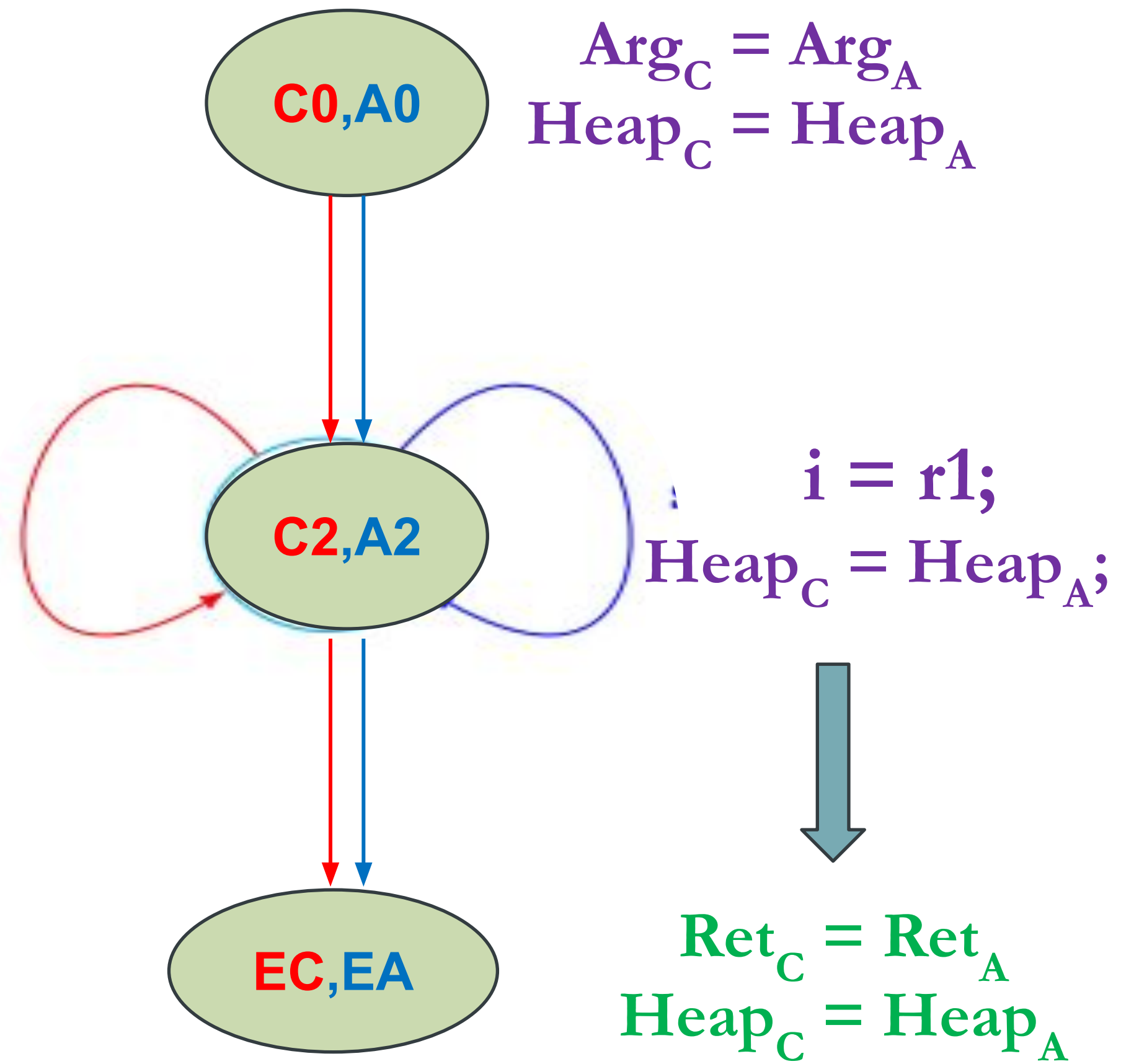


# Prove at exit points

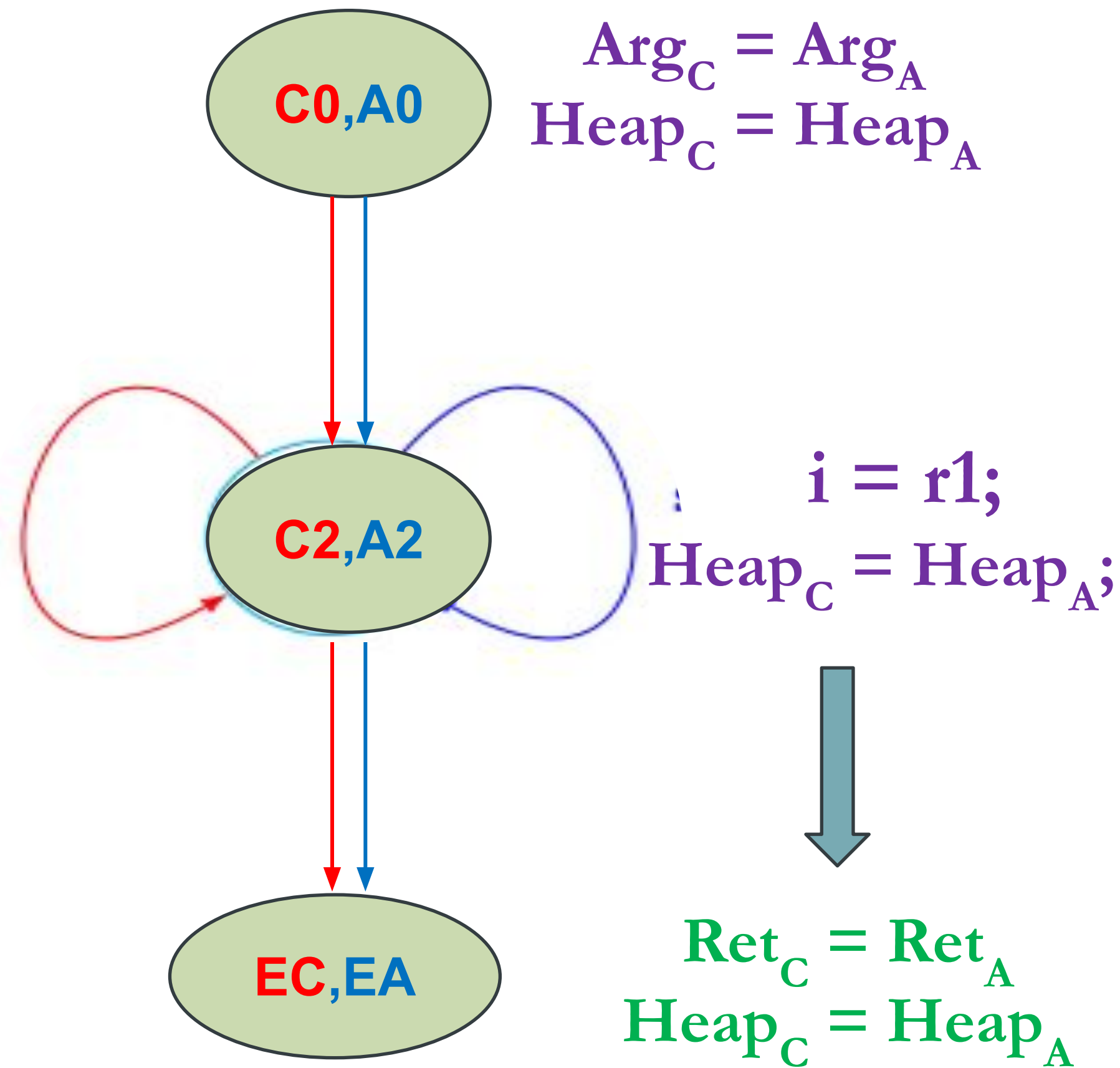




# Equivalence Checking



# Equivalence Checking



Undecidable

*Identifying the correlated transitions*

*Identifying the Invariants*

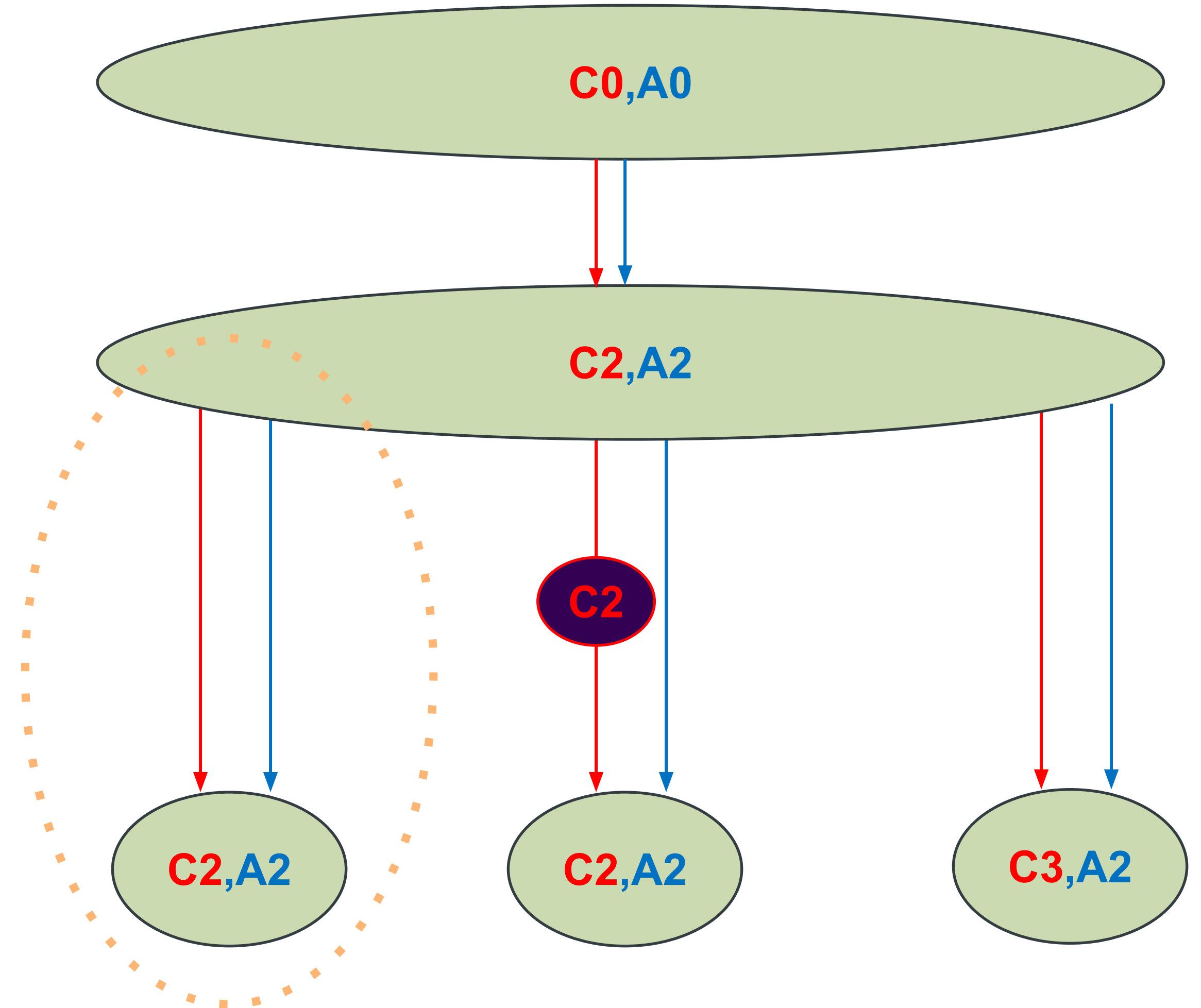
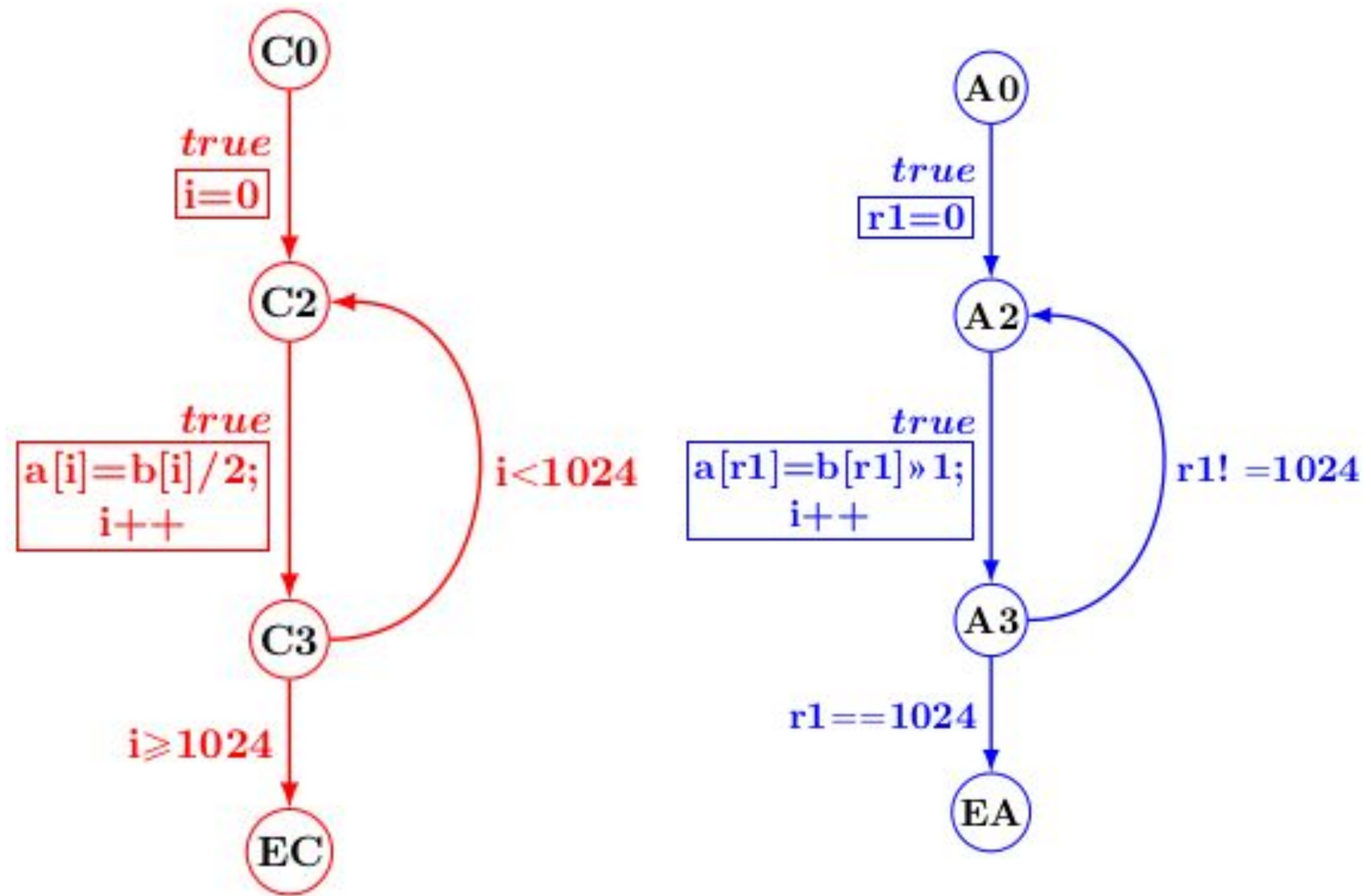
# *Equivalence Checking*

# Robustness

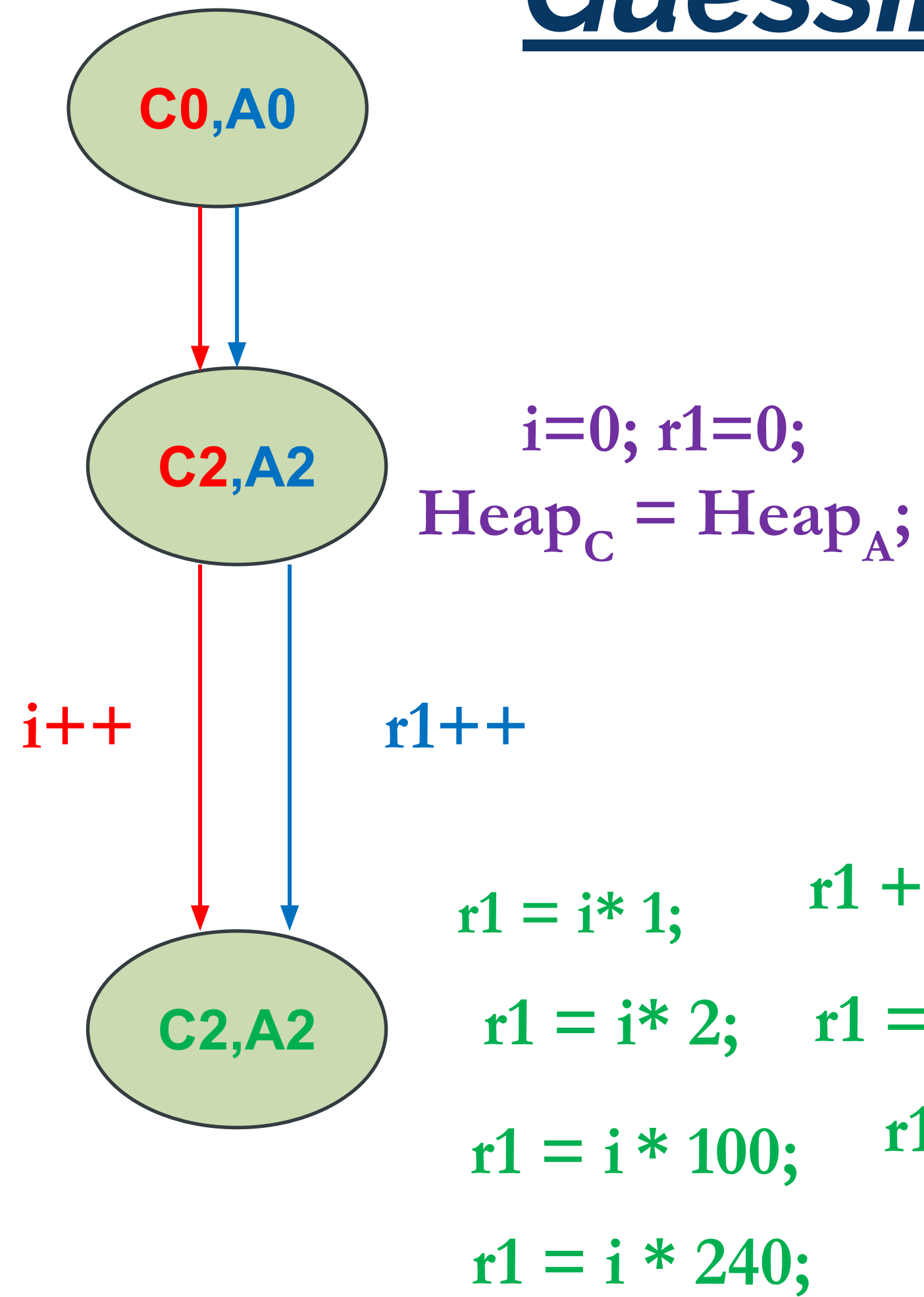


**GOAL**

# Enumerate multiple possible paths



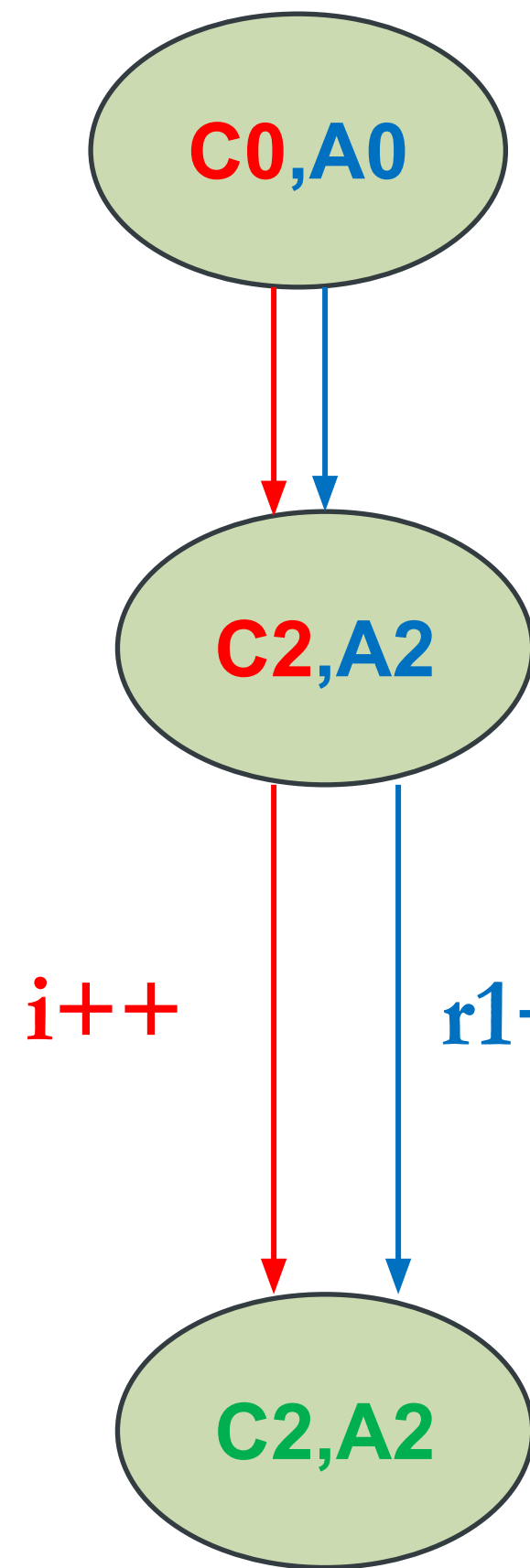
# Guessing the relations



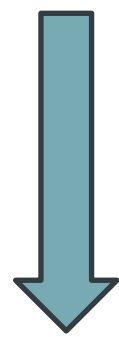
**Affine relations**



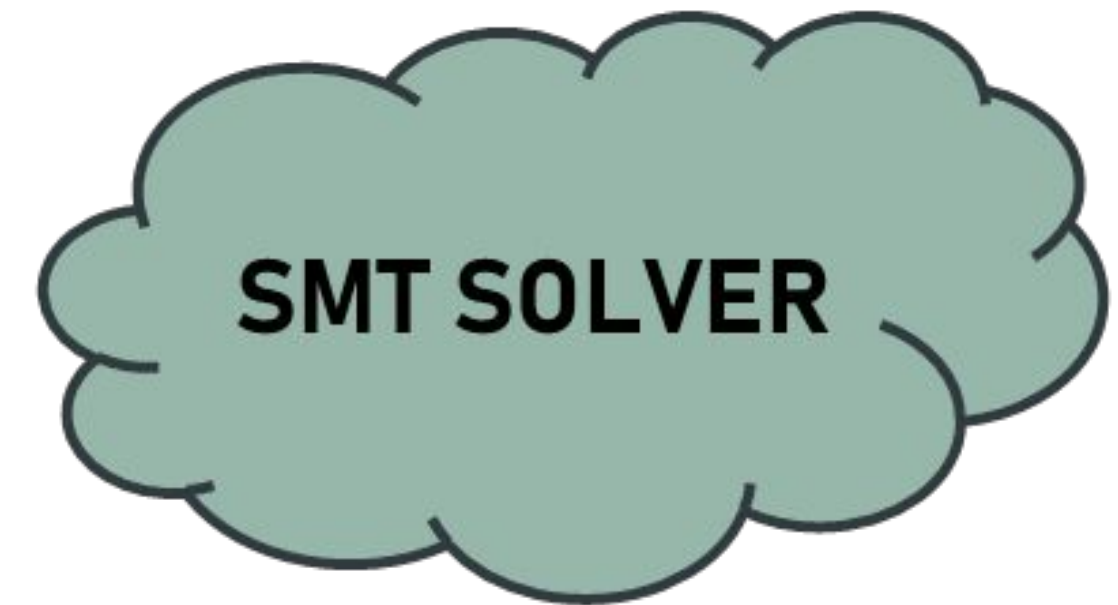
# Guessing the relations



$i == r1$

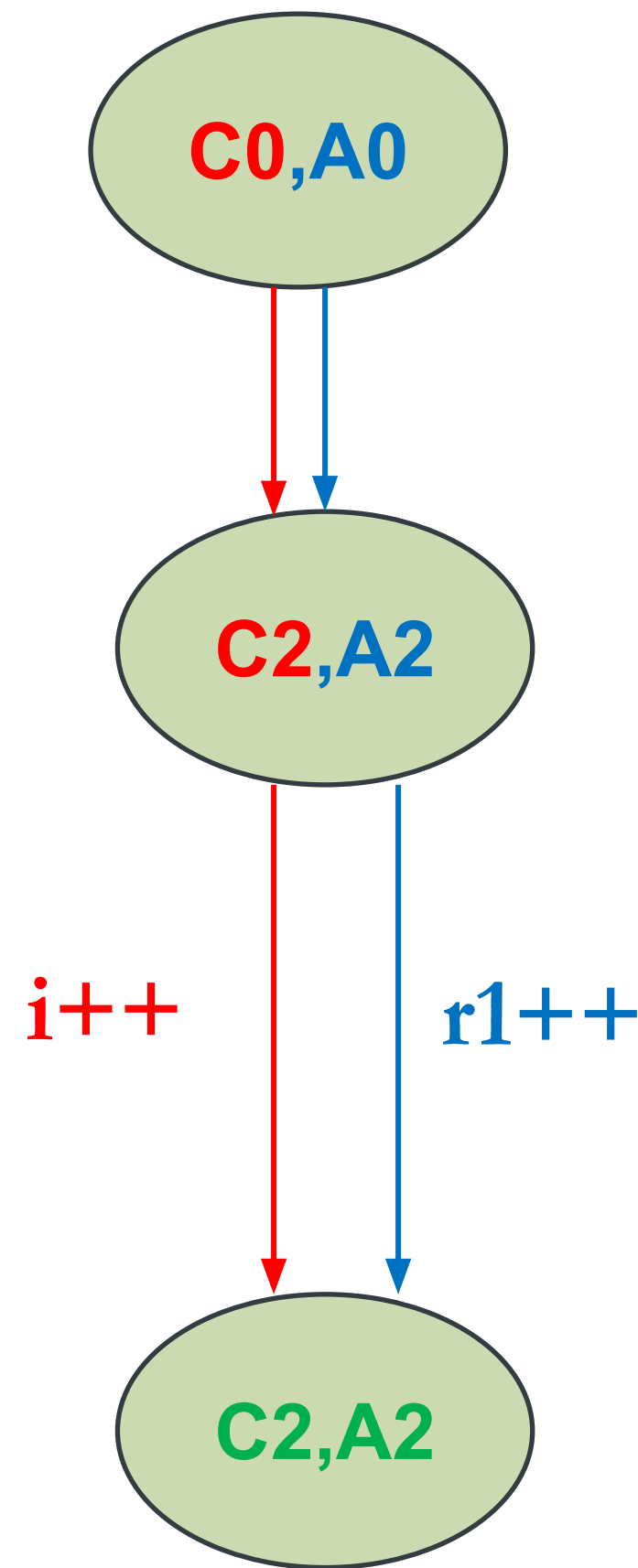


$r1 = i;$        $r1 + 5 = i;$        $2 * r1 = 5 * i;$   
 $r1 = i * 2;$      $r1 = i + 3;$      $3 * r1 = 7 * i;$   
 $r1 = i * 100;$      $r1 * 8 = i;$   
 $r1 = i * 240;$

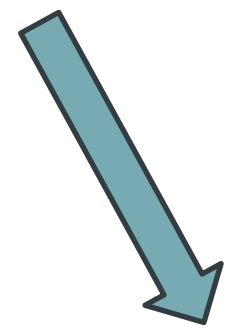


Higher-order theory

# Guessing the relations



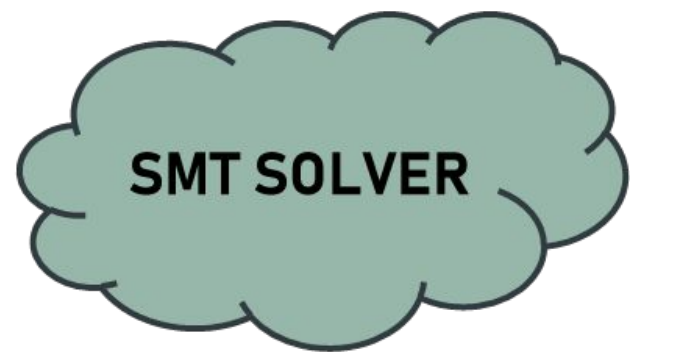
$i = r1$



- $r1 = i * 1;$      $r1 + 5 = i;$      $2 * r1 = 5 * i;$
- $r1 = i * 2;$      $r1 = i + 3;$      $3 * r1 = 7 * i;$
- $r1 = i * 100;$      $r1 * 8 = i;$
- $r1 = i * 240;$

Not Provable Guess

$(i == r1) \Rightarrow (i+1 == r1+5+1) ?$



NO  
model: { i = 100; r1 = 100 }

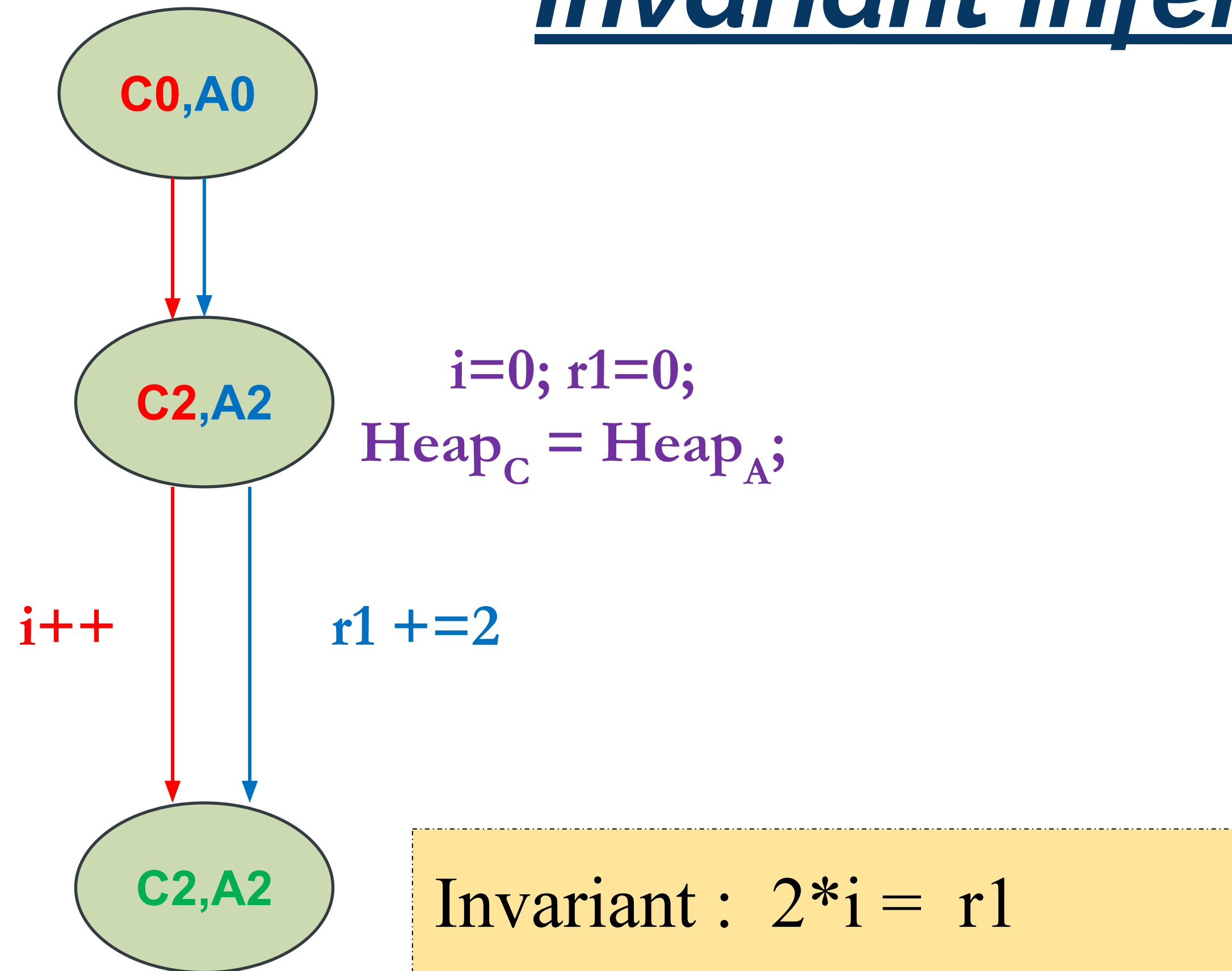
**Counterexample**



# Research Contributions

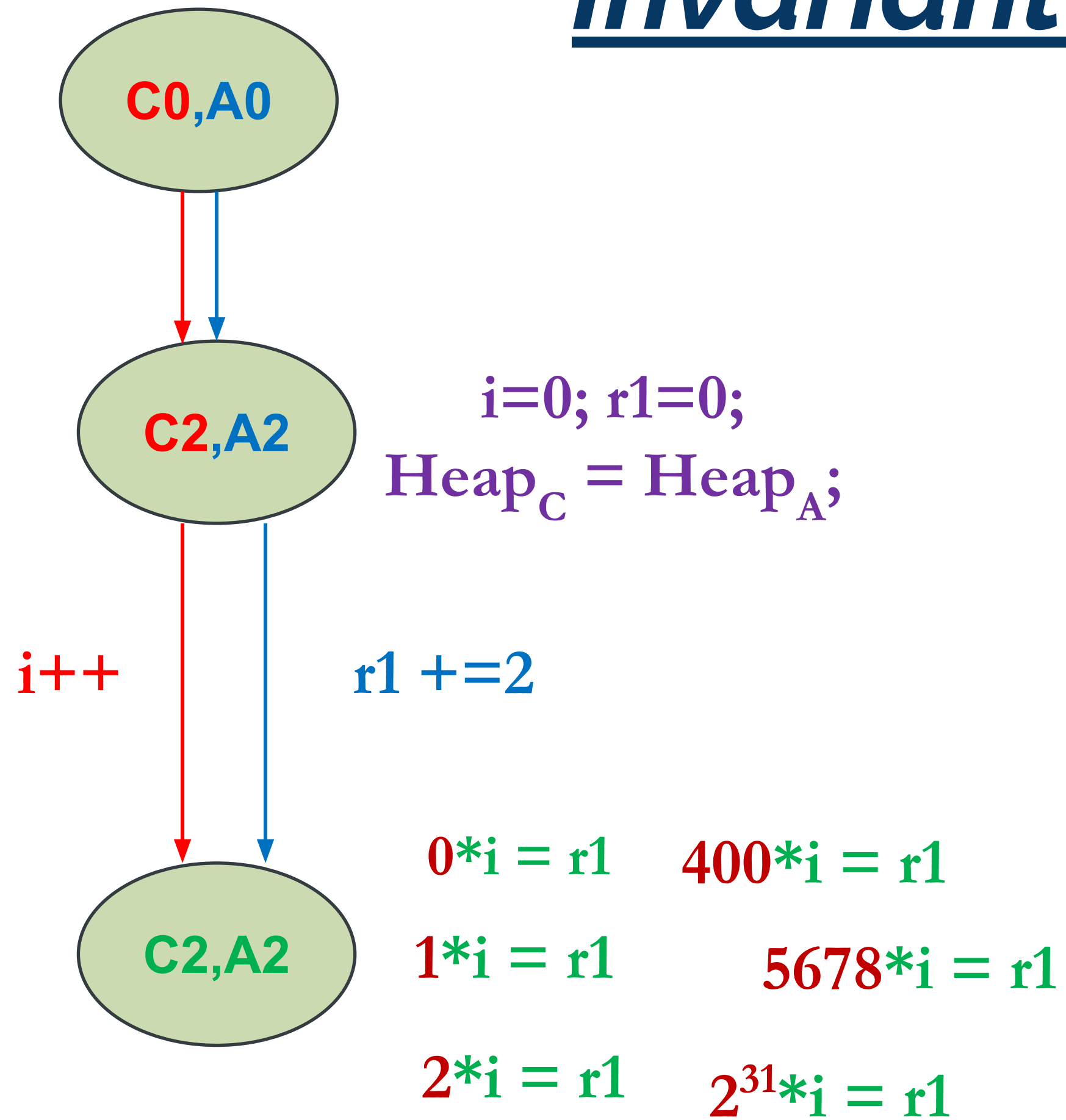
# Counterexample Guided **Invariant Inference**

# Invariant Inference



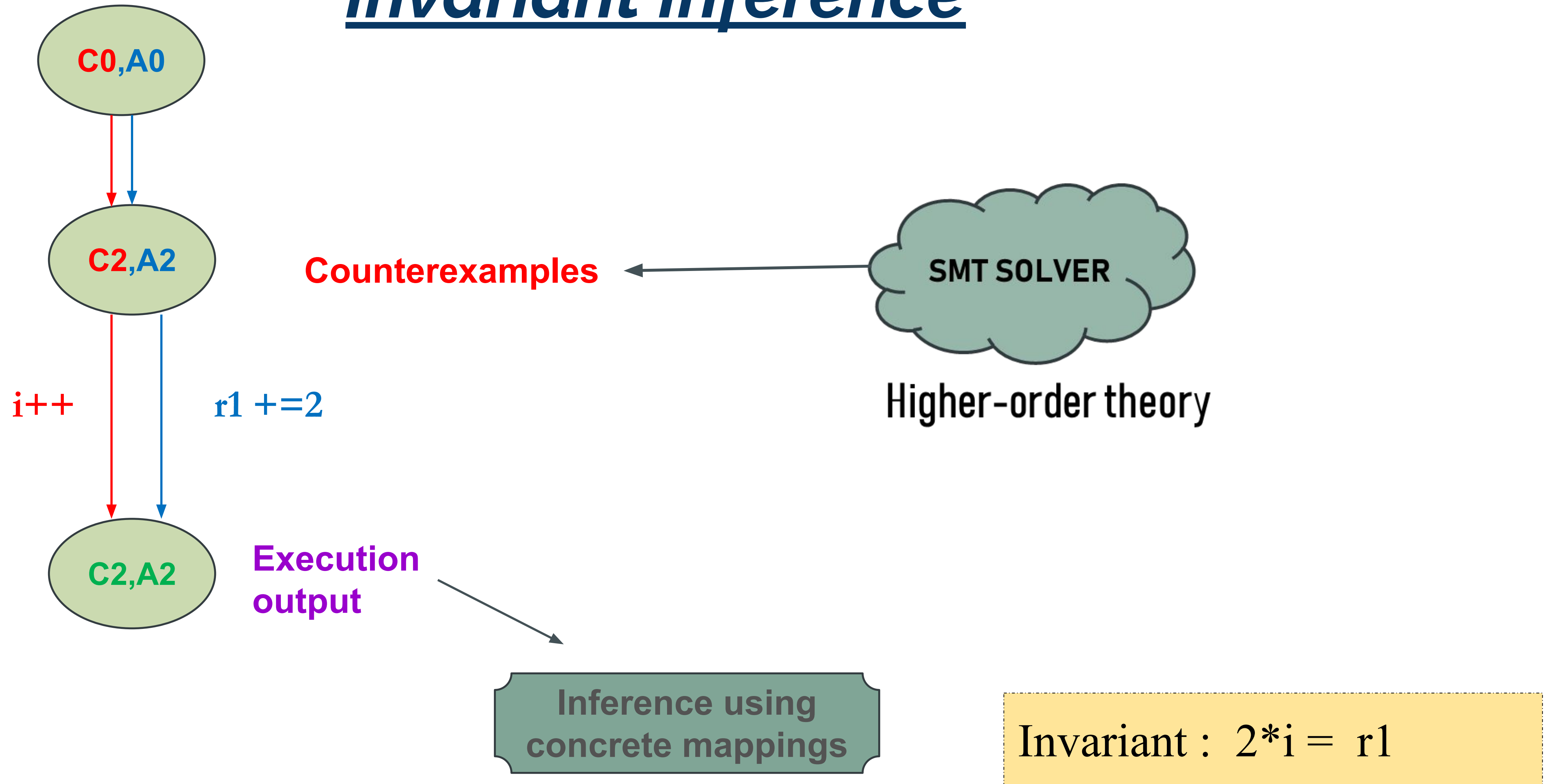


# Invariant Inference

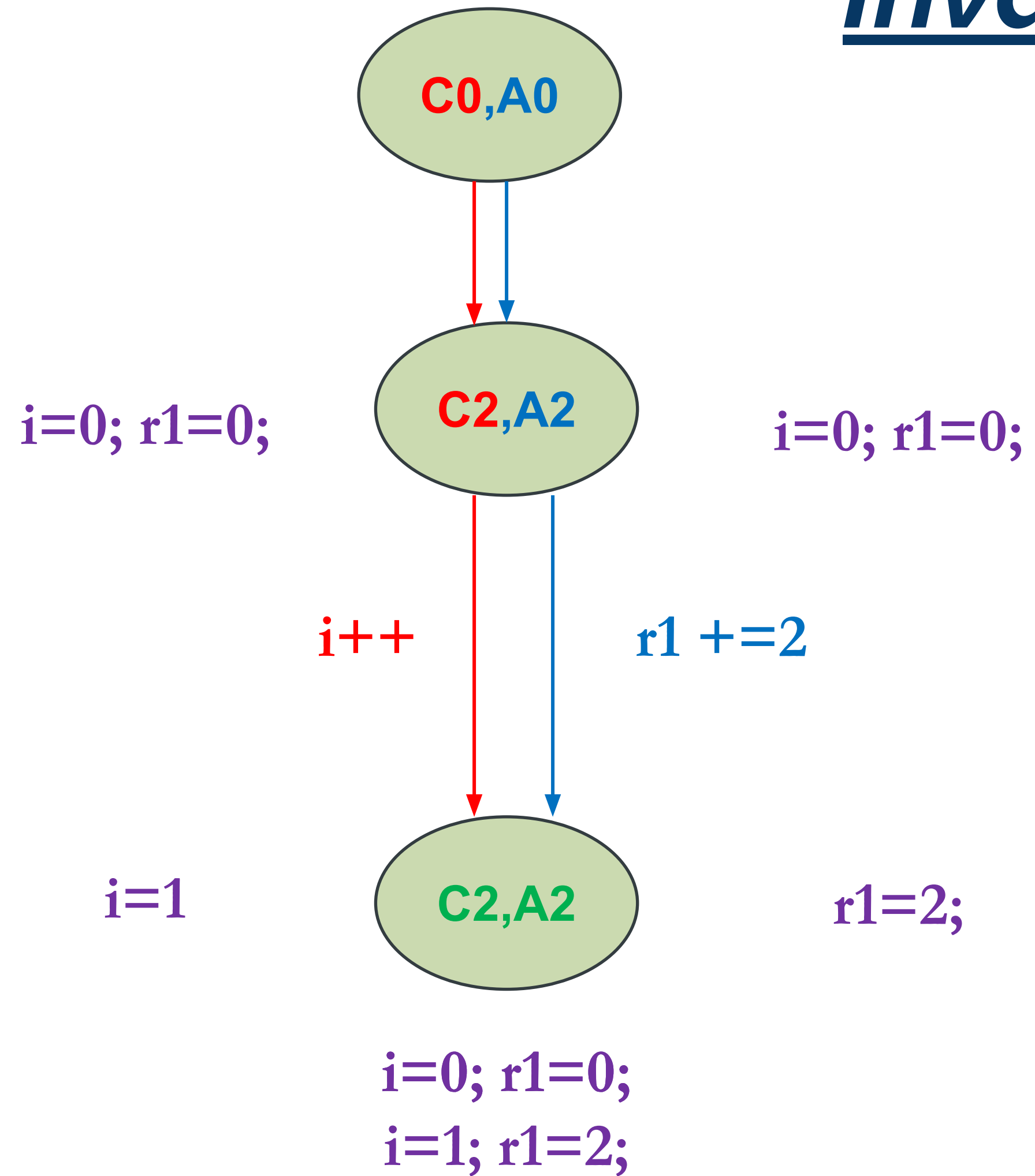


Invariant :  $2*i = r1$

# Invariant Inference

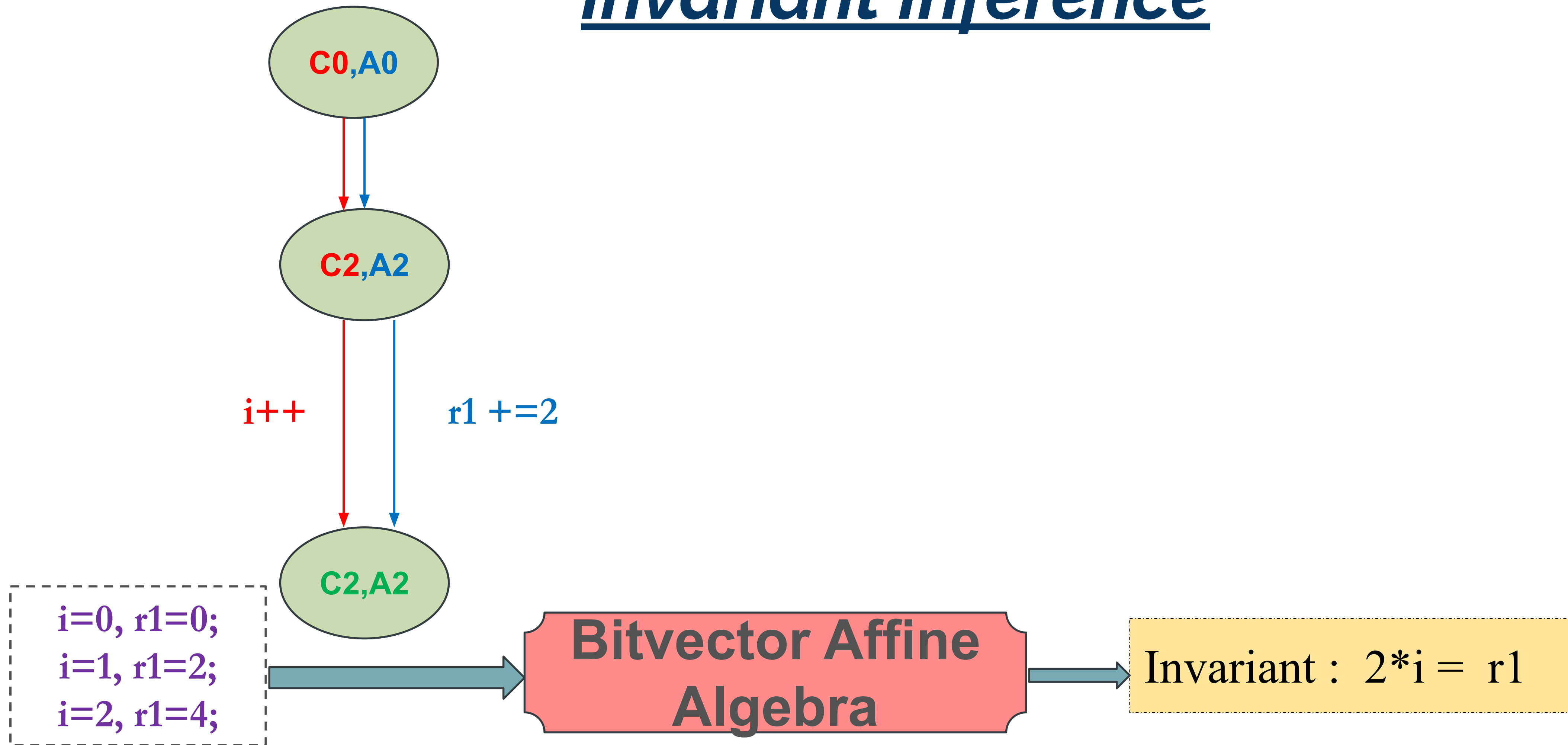


# Invariant Inference



Invariant :  $2*i = r1$

# Invariant Inference



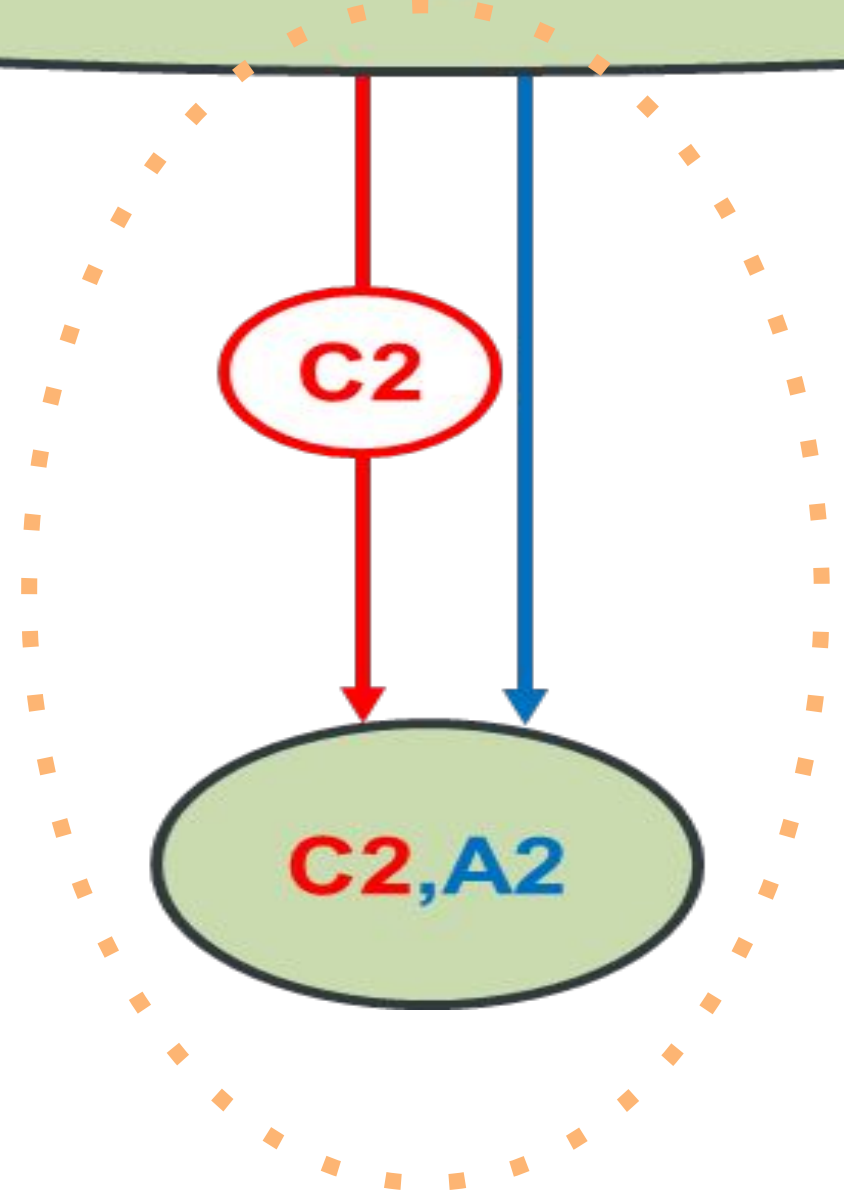
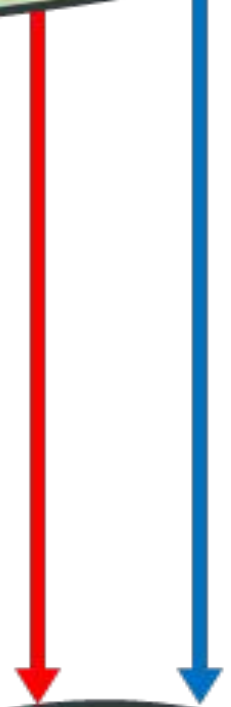
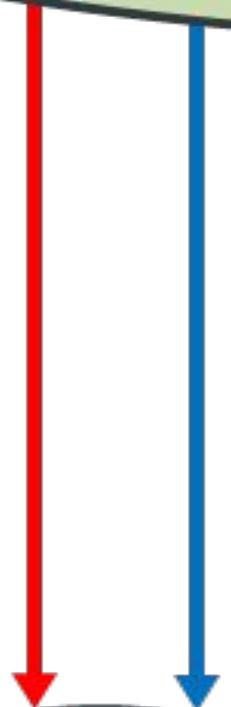
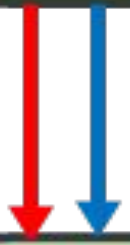
**Effective use of SMT solvers for Program Equivalence  
Checking through Invariant-Sketching and  
Query-Decomposition (SAT2018)**

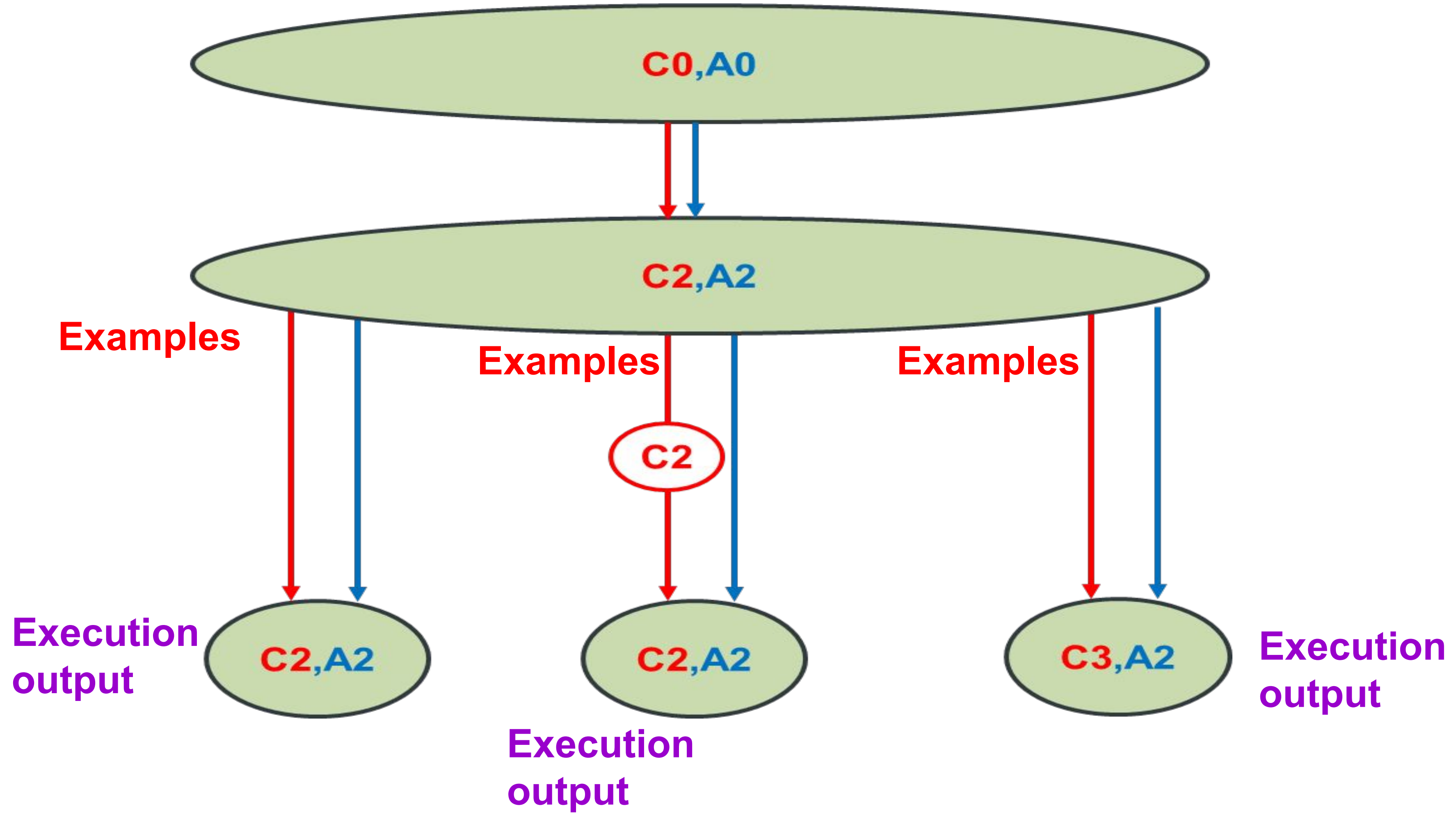
Shubhani Gupta, Aseem Saxena, Anmol Mahajan, Sorav Bansal  
Indian Institute Of Technology Delhi

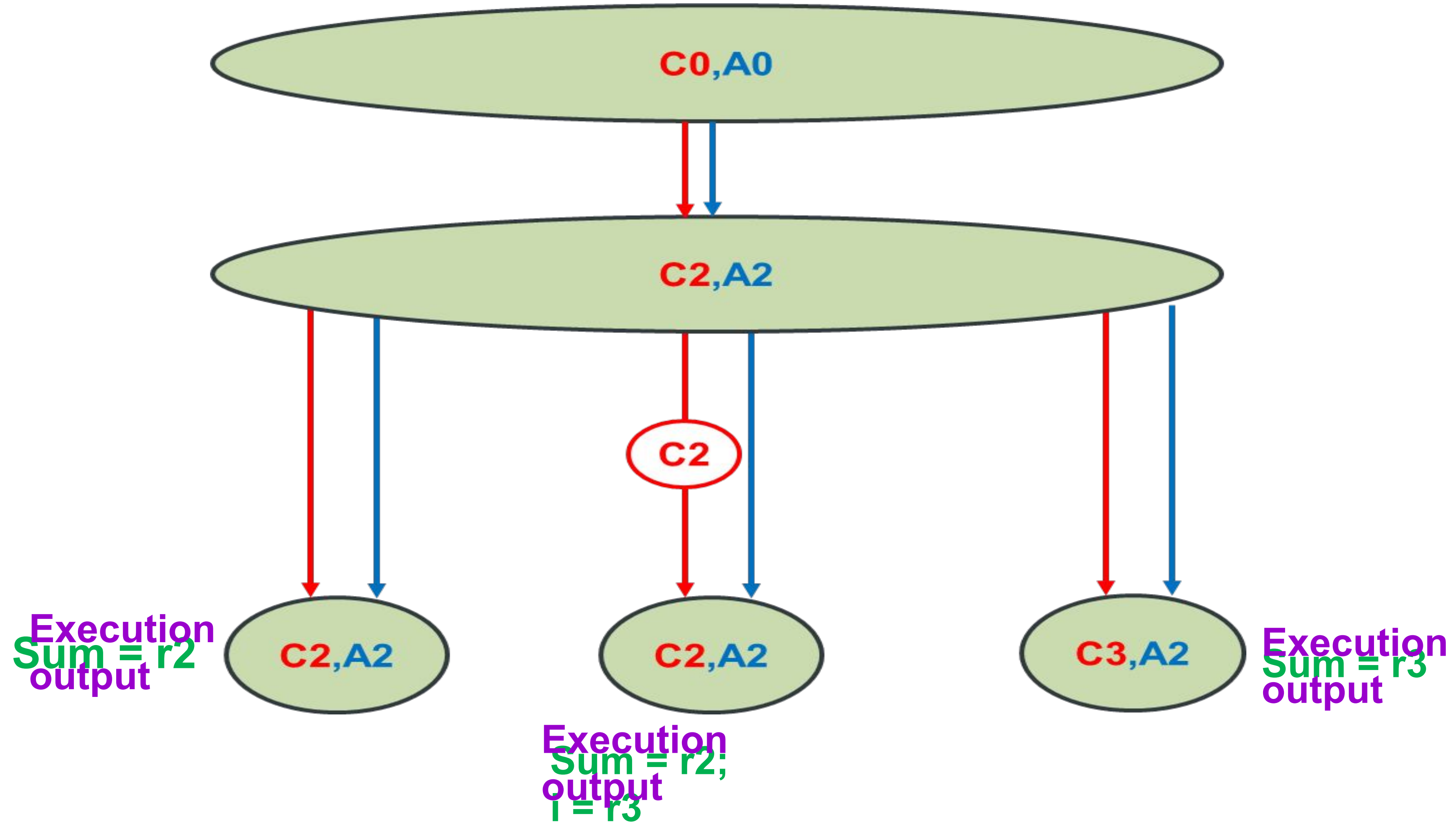
[https://doi.org/10.1007/978-3-319-94144-8\\\_22](https://doi.org/10.1007/978-3-319-94144-8\_22)

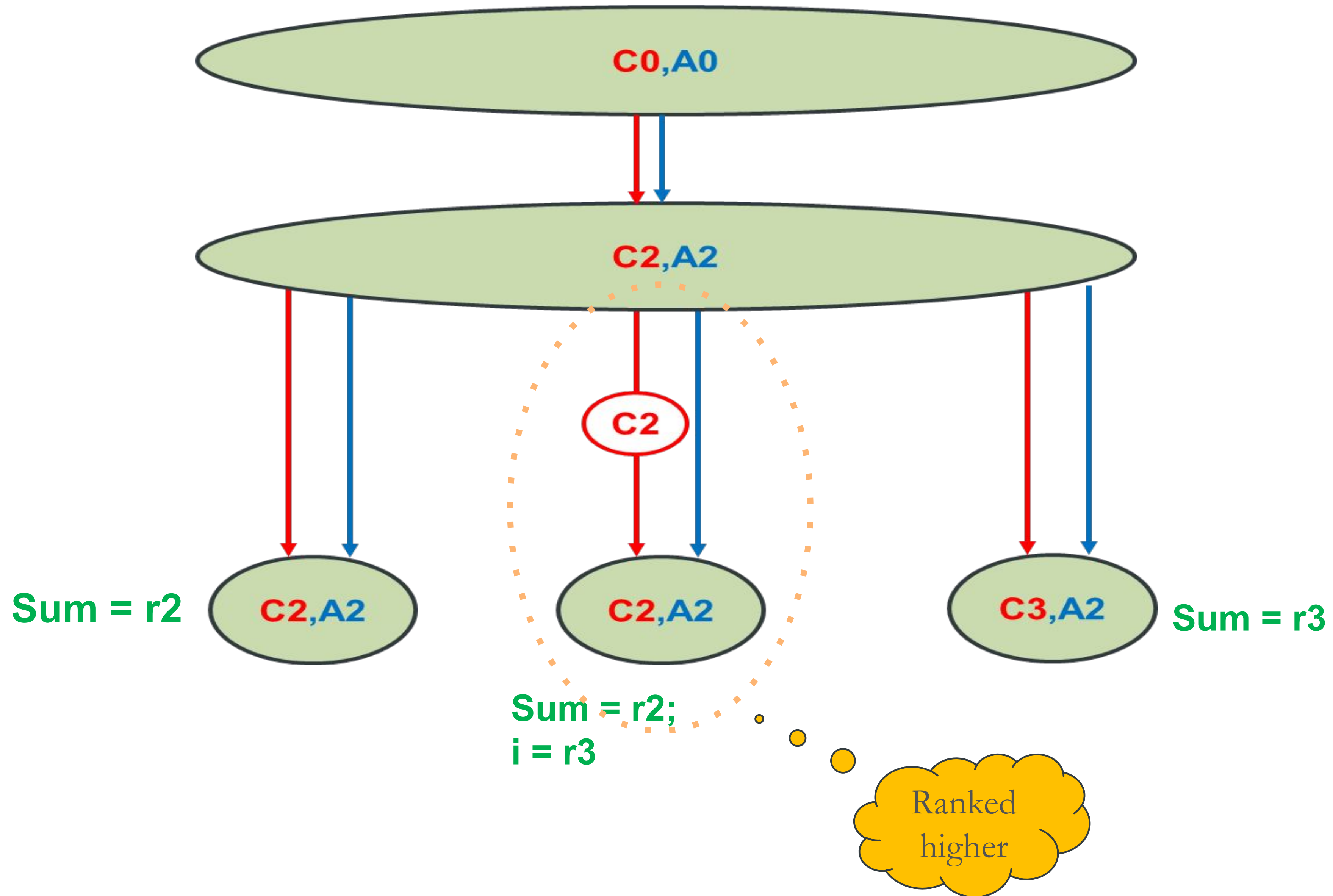


# Counterexample Guided Correlation











# **Counterexample-Guided Correlation Algorithm For Translation Validation (OOPSLA2020)**

Shubhani, Abhishek Rose, Sorav Bansal  
Indian Institute Of Technology Delhi

<https://dl.acm.org/doi/pdf/10.1145/3428289>

# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
#define LEN 1000
int original() {
    int sum = 0;
    int mid = LEN / 2;
    for ( int i = 0; i < LEN ; i ++ ) {
        if ( i < mid ) sum += c[a[i]];
        if ( i >= mid ) sum += b[i];
    }
    return sum ;
}
```

```
int loopSplitting() {
```

```
    int sum = 0;
```

```
    int mid = LEN / 2;
```

```
    for ( int i = 0; i < mid ; i ++ ) {
```

```
        if ( i < mid ) sum += c[a[i]];
        if ( i >= mid ) sum += b[i];
```

```
    }
```

```
    }
```

```
    for ( int i = mid; i < LEN ; i ++ ) {
```

```
        if ( i < mid ) sum += c[a[i]];
        if ( i >= mid ) sum += b[i];
```

```
    }
```

```
    }
```

```
    return sum ;
```

```
}
```

# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
int loopSplitting() {
```

```
    int sum = 0;
```

```
    int mid = LEN / 2;
```

```
    for ( int i = 0; i < mid ; i ++ ) {  
        if ( i < mid ) sum += c[a[i]];  
        if ( i >= mid ) sum += b[i];  
    }
```

```
    for ( int i = mid; i < LEN ; i ++ ) {  
        if ( i < mid ) sum += c [a[i]];  
        if ( i >= mid ) sum += b[i];  
    }
```

```
    return sum ;
```

```
}
```

```
int loopUnswitching() {
```

```
    int sum = 0;
```

```
    int mid = LEN / 2;
```

```
    for ( int i = 0; i < mid ; i ++ ) {  
        sum += c[a[i]];  
    }
```

```
    for ( int i = mid; i < LEN ; i ++ ) {  
        sum += b[i];  
    }
```

```
    return sum ;
```

```
}
```

# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
int loopUnswitching() {  
    int sum = 0;  
    int mid = LEN / 2;  
    for ( int i = 0; i < mid ; i++) {  
        sum += c[a[i]];  
    }  
    for ( int i = mid; i < LEN ; i++) {  
        sum += b[i];  
    }  
    return sum ;  
}
```

```
int loopUnrolling() {  
    int sum = 0;  
    int mid = LEN / 2;  
    for ( int i = 0; i < mid ; i++) {  
        sum += c[a[i]];  
    }  
    for ( int i = mid; i < LEN ; i += 4) {  
        sum += b[ i ];  
        sum += b[ i + 1 ];  
        sum += b[ i + 2 ];  
        sum += b[ i + 3 ];  
    }  
    return sum ;  
}
```



# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
int loopUnrolling() {  
    int sum = 0;  
    int mid = LEN / 2;  
    for ( int i = 0; i < mid ; i ++ ) {  
        sum += c[a[i]];  
    }  
    for ( int i = mid; i < LEN ; i += 4 ) {  
        sum += b[ i ];  
        sum += b[ i + 1 ];  
        sum += b[ i + 2 ];  
        sum += b[ i + 3 ];  
    }  
    return sum ;  
}
```

A0 : loopVectorizedAndRegAllocated :

A1 : r1 = 0; r2 = 0;

A2 : r2 += c [ a [ r1 ] ]

A3 : r1 ++

A4 : if ( r1 != mid ) goto A2

A5 : r1 = &b[mid]; r3=& b[LEN]; xmm0 = 0

A6 : xmm0 += \* r1 , .. , \*( r1 + 12)

A7 : r1 += 16

A8 : if ( r1 != r3 ) goto A6

A9 : xmm0 += ( xmm0 >> 8)

A10 : xmm0 += ( xmm0 >> 4)

A11 : r2 += xmm0 [31:0]

EA : ret r2

# End-to-End Equivalence Check

```

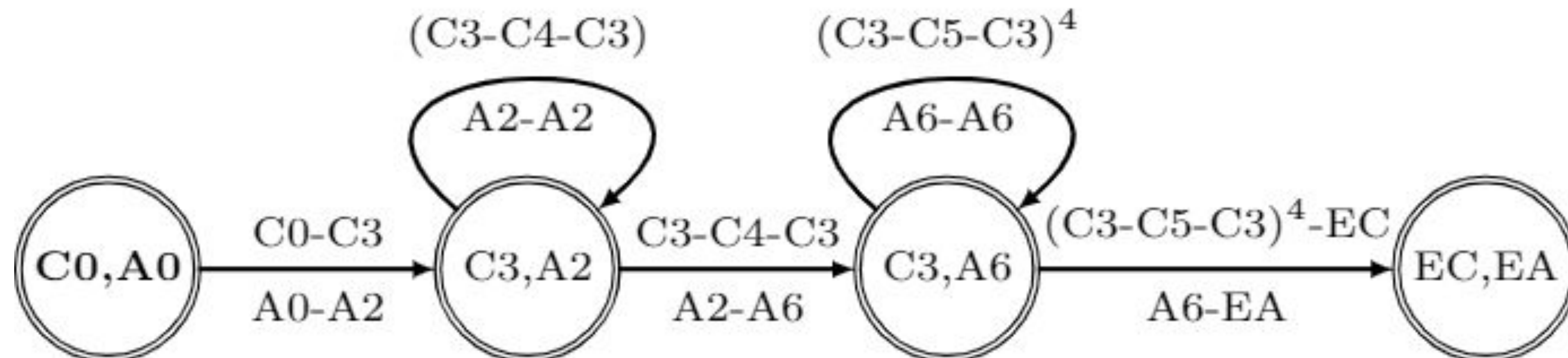
#define LEN 1000
C0: int original() {
C1:  int sum = 0;
C2:  int mid = LEN / 2;
C3:  for ( int i = 0; i < LEN ; i ++ ) {
C4:    if ( i < mid ) sum += c[a[ i ]];
C5:    if ( i >= mid ) sum += b[i];
C6:  }
EC:  return sum ;
    }

```

```

A0 : loopVectorizedAndRegAllocated :
A1 :  r1 = 0; r2 = 0;
A2 :    r2 += c [ a [ r1 ]]
A3 :    r1 ++
A4 :    if ( r1 != mid ) goto A2
A5 :  r1 = &b[mid]; r3=& b[LEN]; xmm0 = 0
A6 :    xmm0 += * r1 , .. , *( r1 +12)
A7 :    r1 += 16
A8 :    if ( r1 != r3 ) goto A6
A9 :  xmm0 += ( xmm0 >> 8)
A10 : xmm0 += ( xmm0 >> 4)
A11 : r2 += xmm0 [31:0]
EA  : ret r2

```



# Incremental Construction of the Product CFG

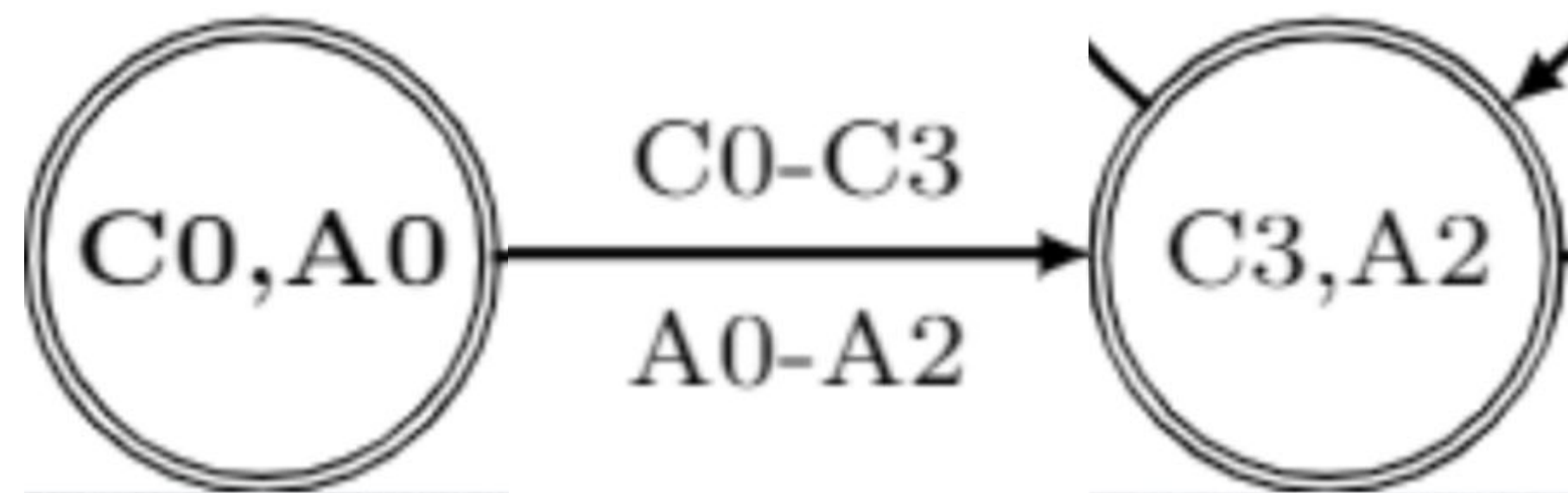


# Incremental Construction of the Product CFG



# Incremental Construction of the Product CFG

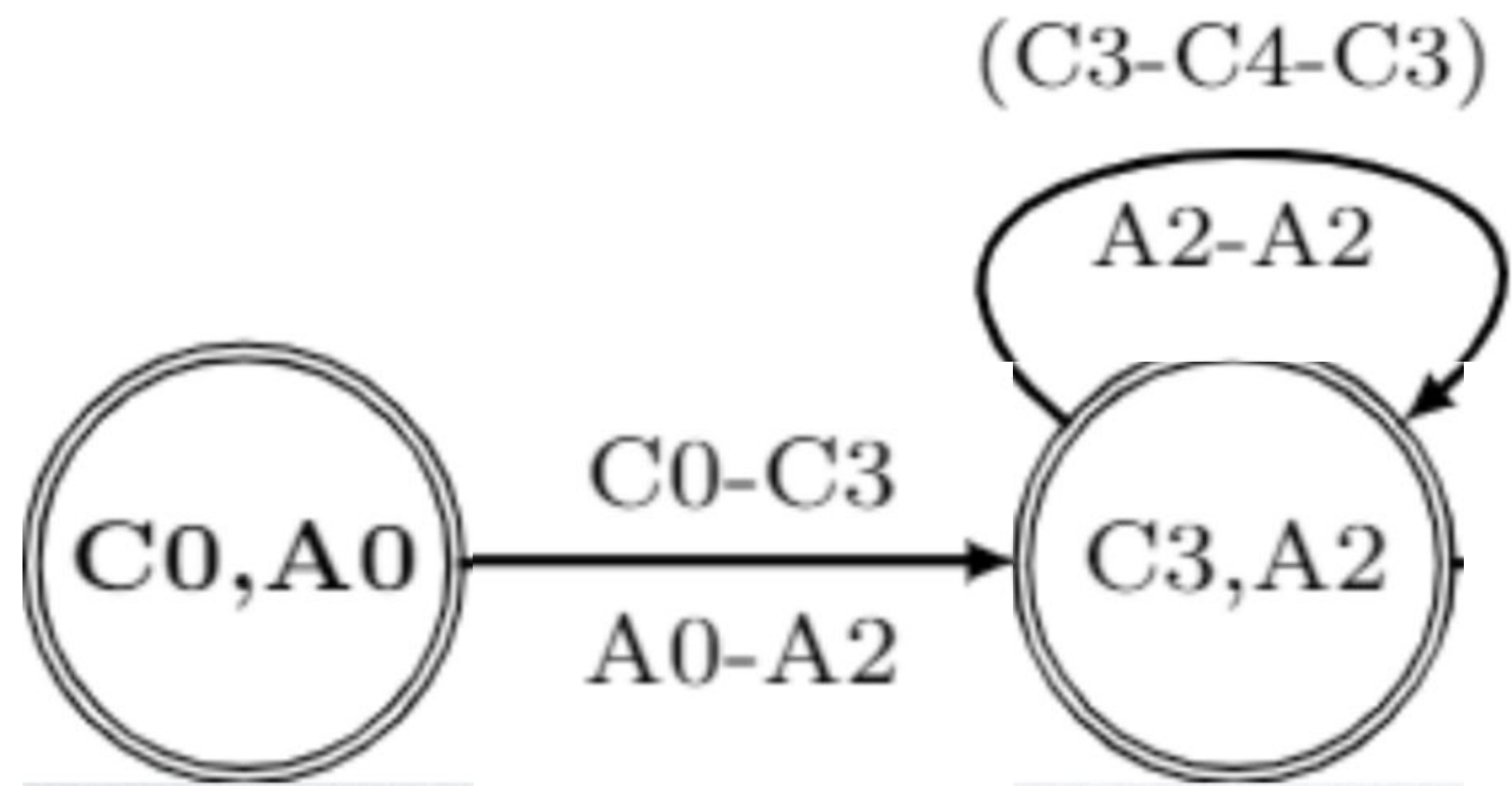
Use off-the-shelf invariant inference algorithms to infer affine, equality and inequality invariants on bitvectors and memory states



Infer Invariants at  
 $(C3, A2)$

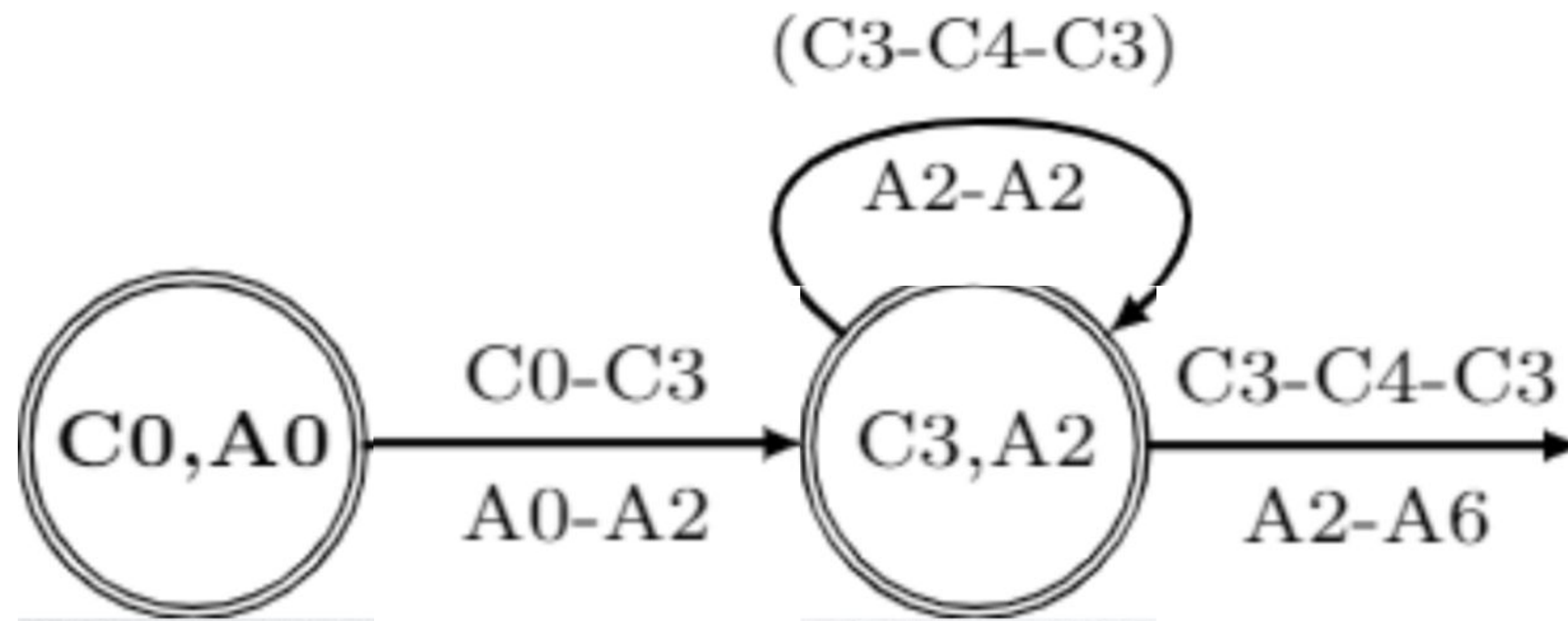


# Incremental Construction of the Product CFG

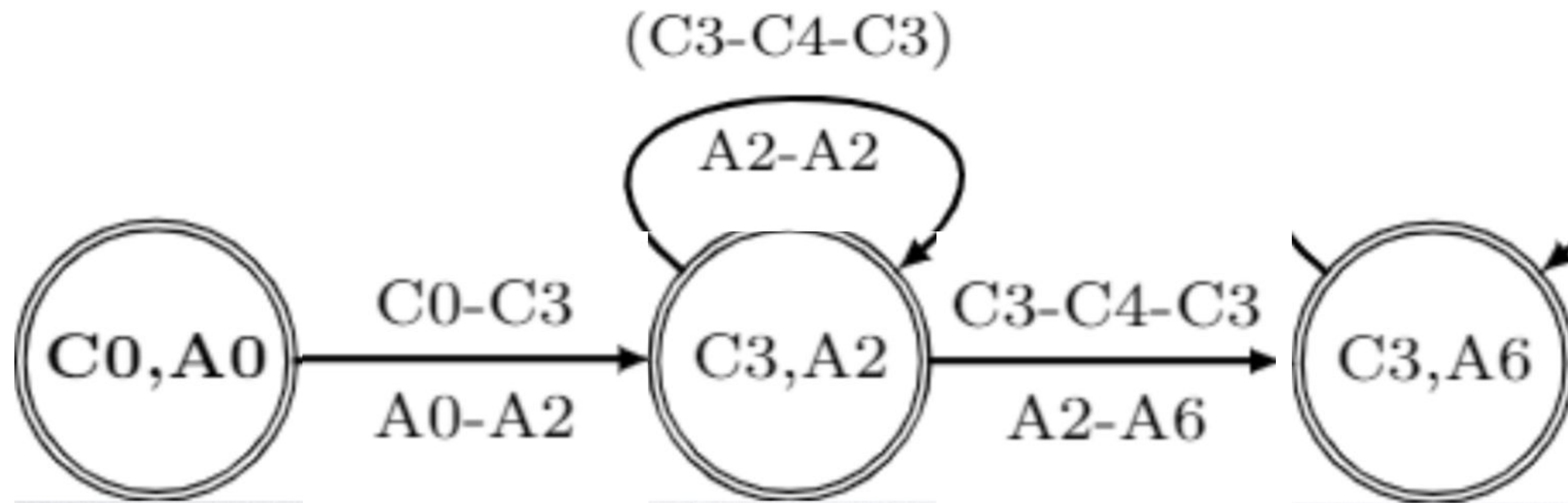


Relax Invariants  
at  $(C3, A2)$

# Incremental Construction of the Product CFG

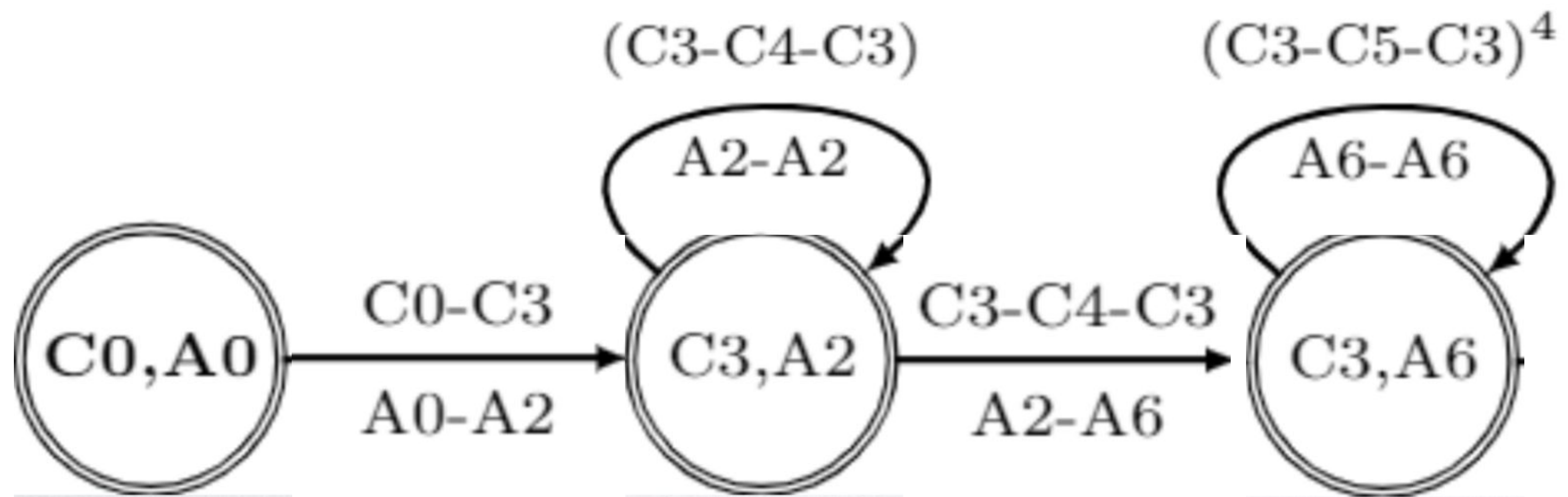


# Incremental Construction of the Product CFG



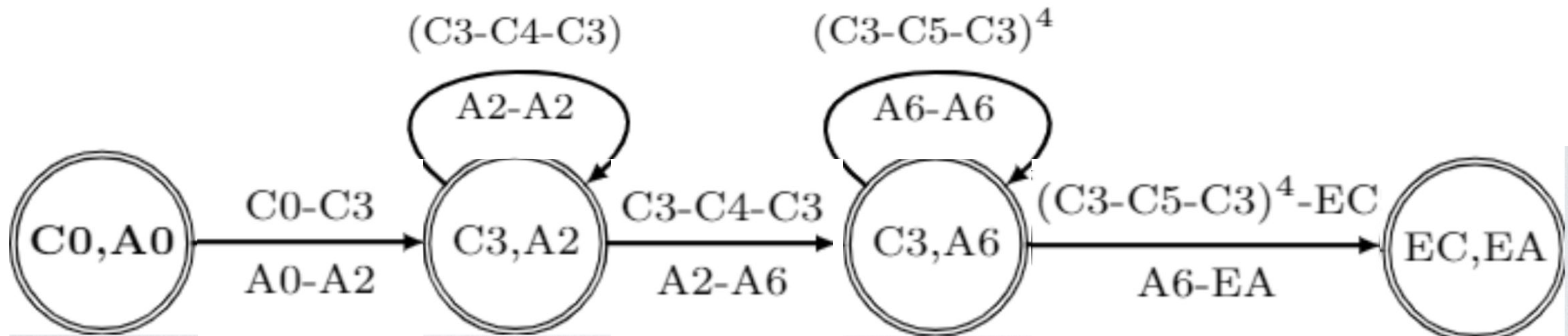
Infer Invariants at  
 $(C_3, A_6)$

# Incremental Construction of the Product CFG



Relax Invariants  
at  $(C_3, A_6)$

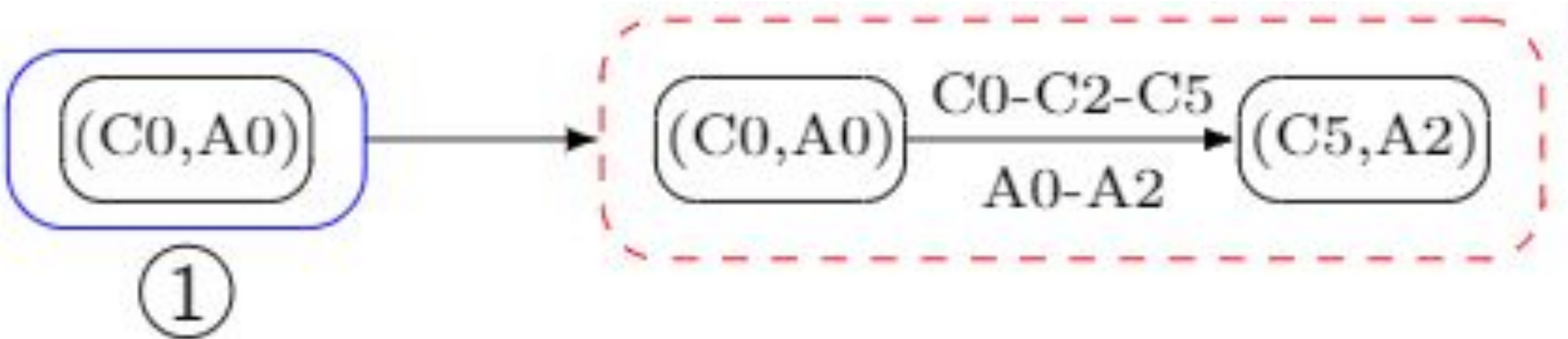
# Incremental Construction of the Product CFG



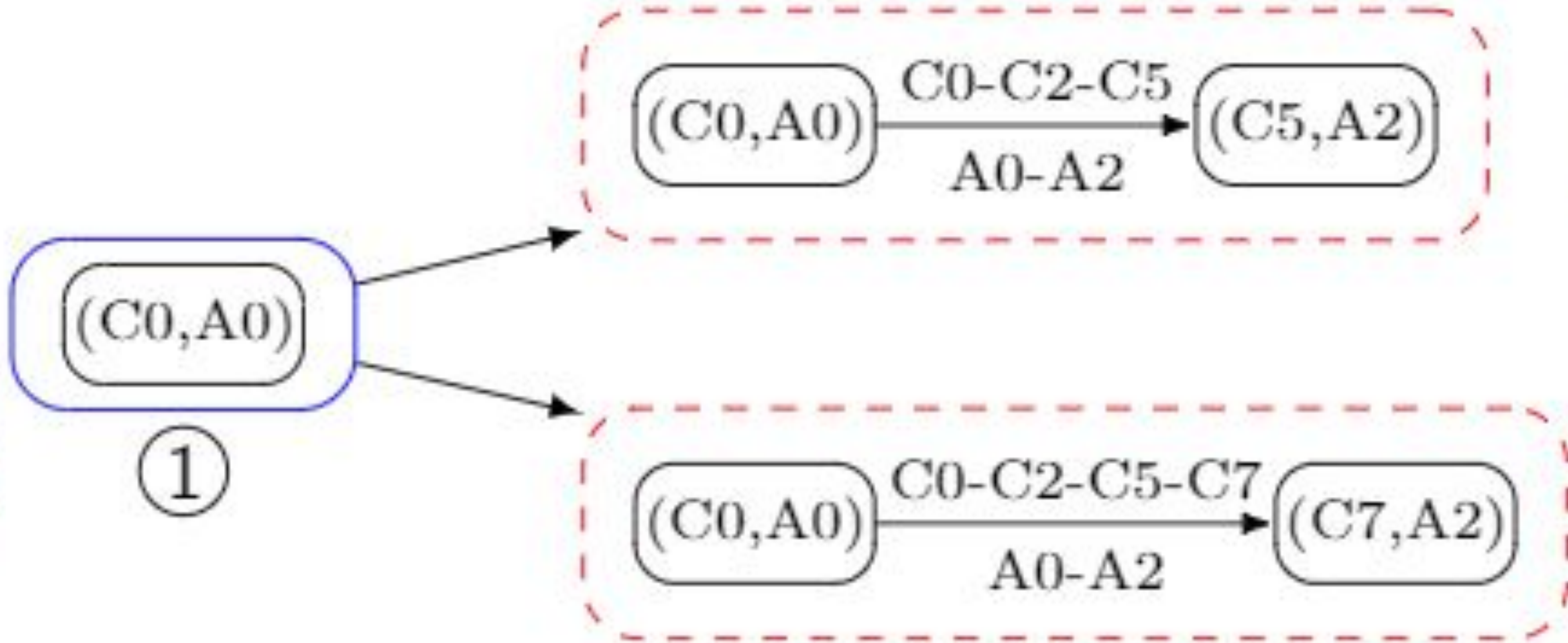
Check equivalence of  
return values under  
inferred invariants



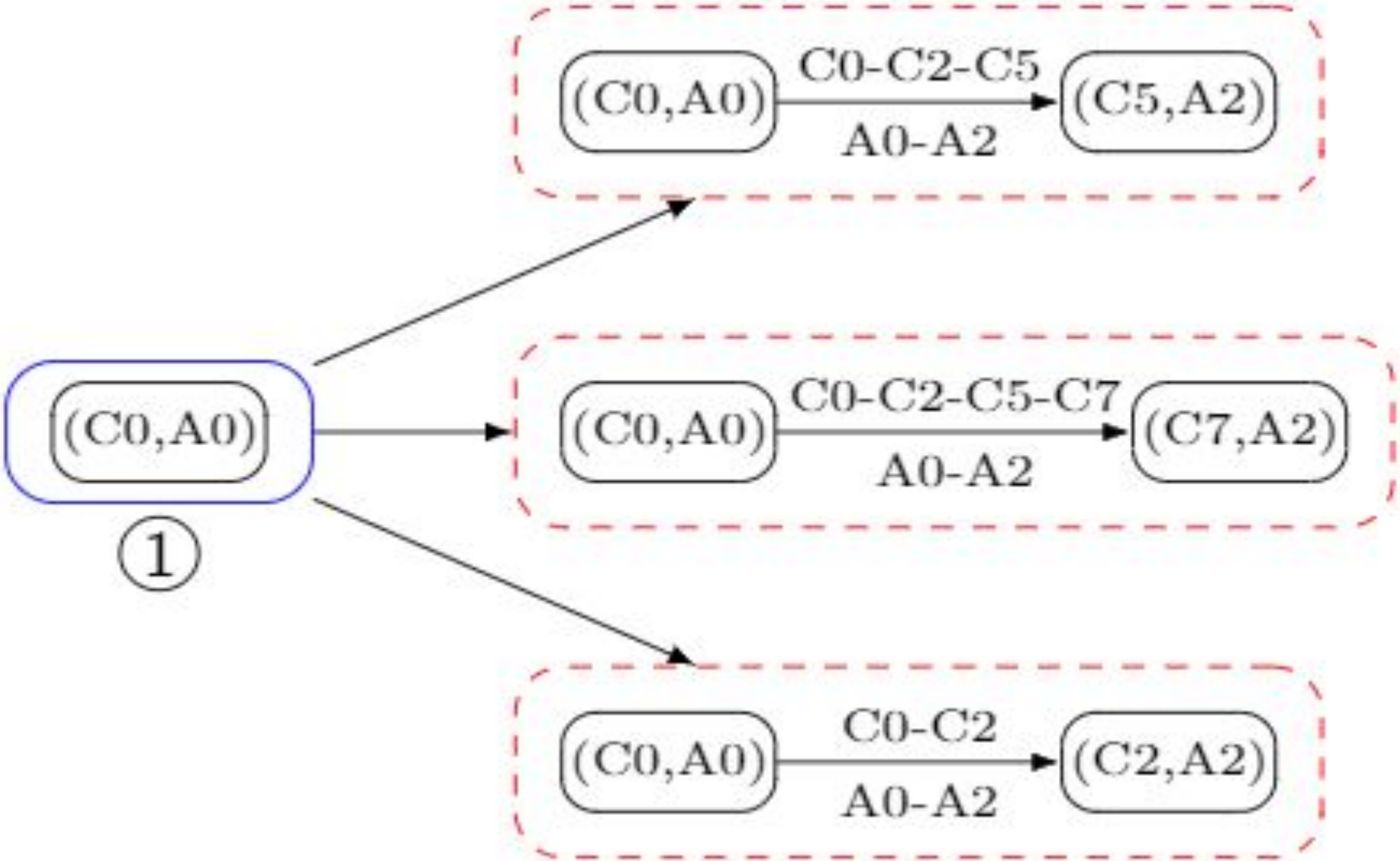
# SEARCH SPACE



# SEARCH SPACE

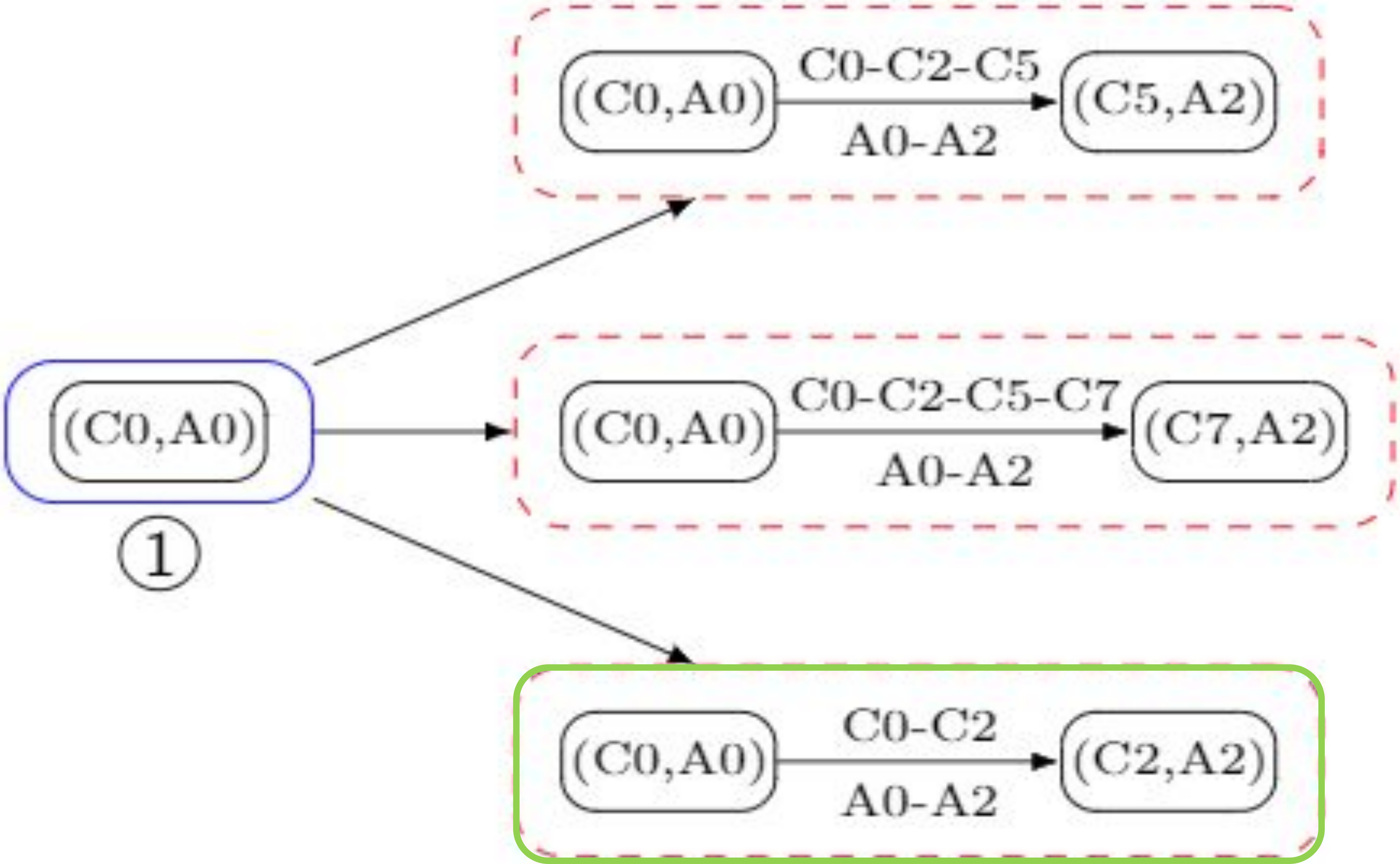


# SEARCH SPACE

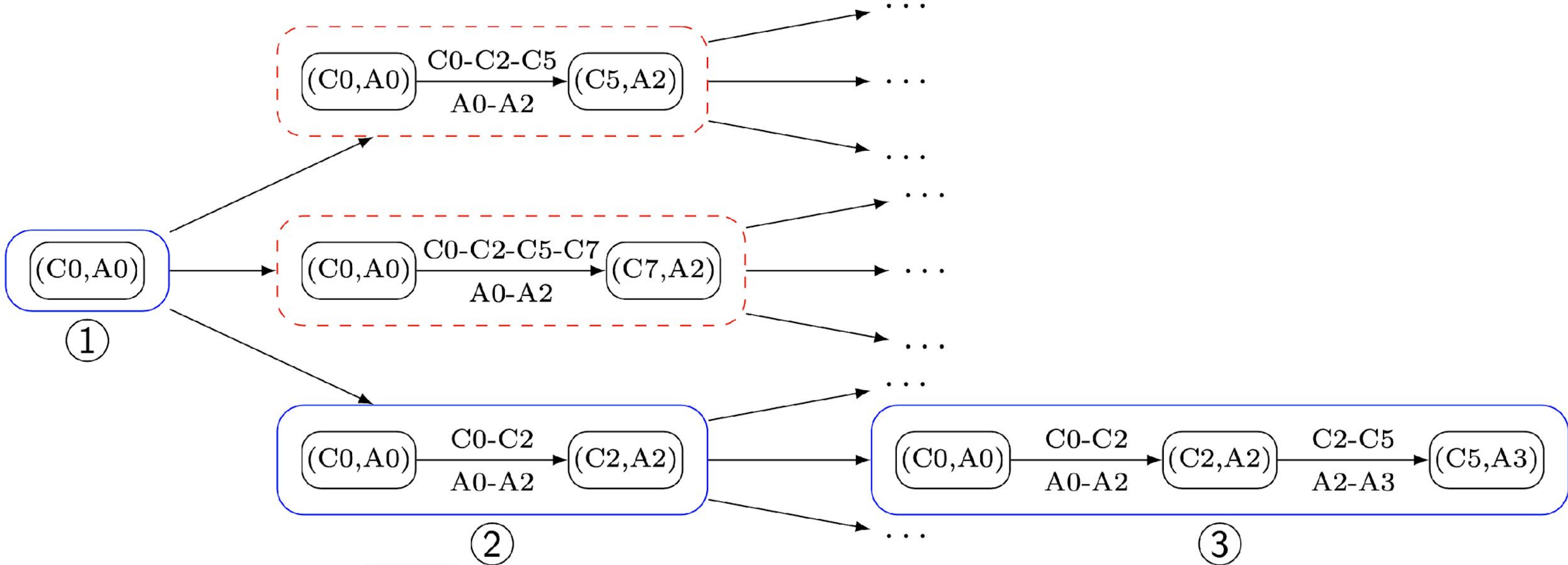




# SEARCH SPACE



# SEARCH SPACE

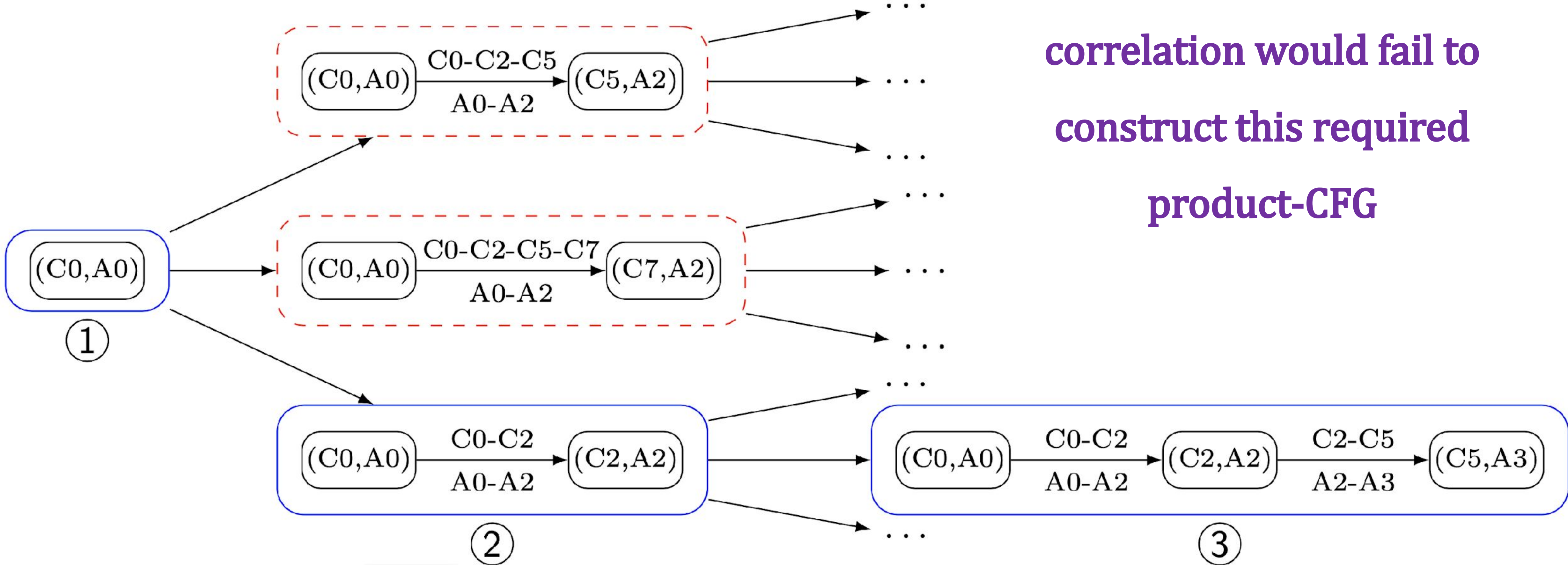


**Exhaustive search would take millions of years to compute equivalence**



# SEARCH SPACE

Prior work on data driven correlation would fail to construct this required product-CFG



**Exhaustive search would take millions of years to compute equivalence**

# Counterexamples

During invariant inference, we make potential GUESSES for invariants. We try to prove a GUESS using an SMT Solver.

- If the GUESS is provable, we have found an invariant.
- If not, the SMT solver returns a counterexample

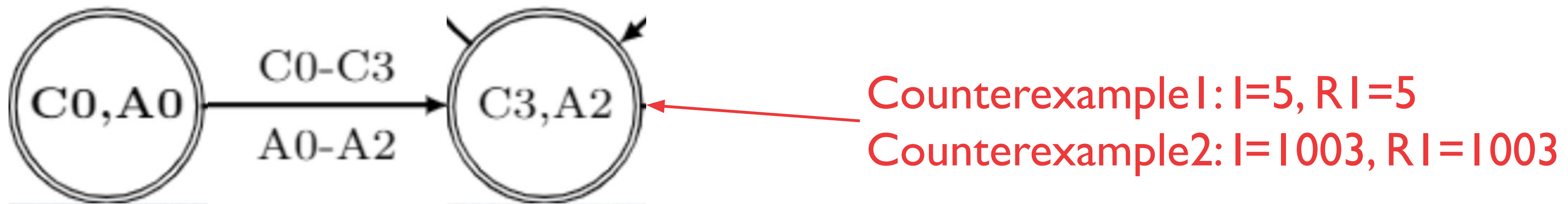


Infer Invariants at  
 $(C3, A2)$

# Counterexamples

A counterexample at a node is a potential concrete machine state that may occur at that particular node during execution.

The concrete state would involve valuations for (related) variables of both C and A.

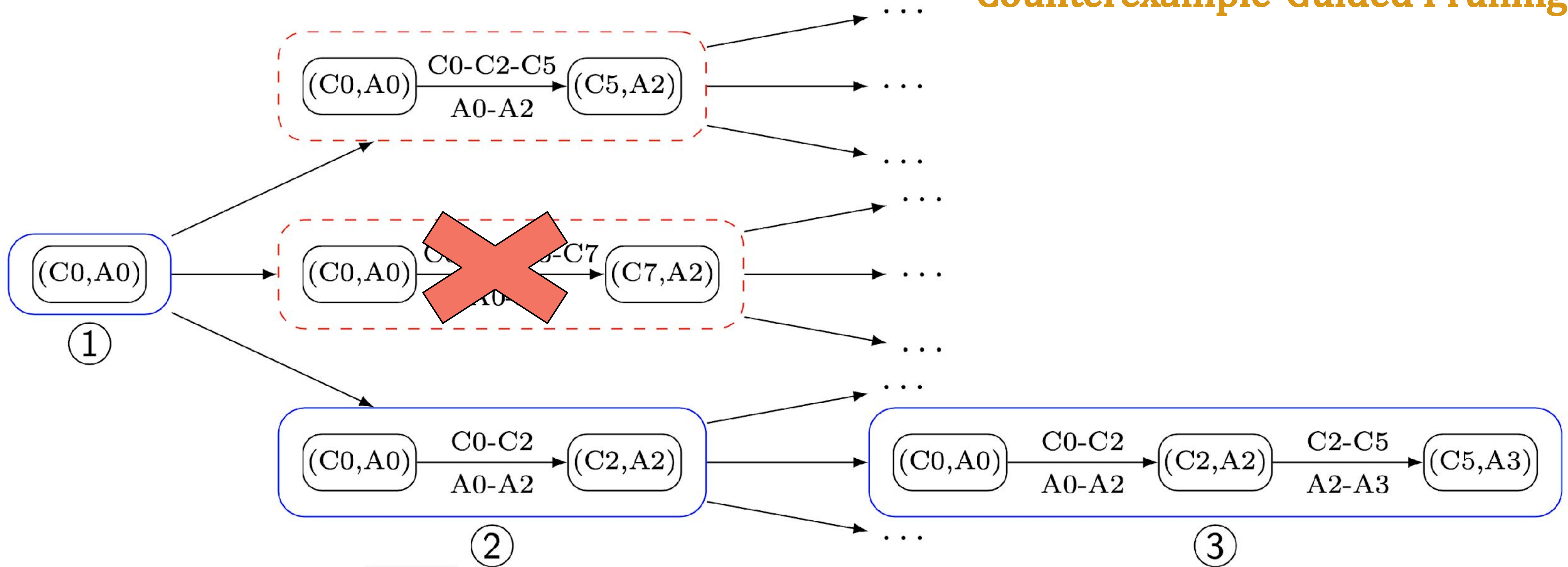


Infer Invariants at  
(C3,A2)

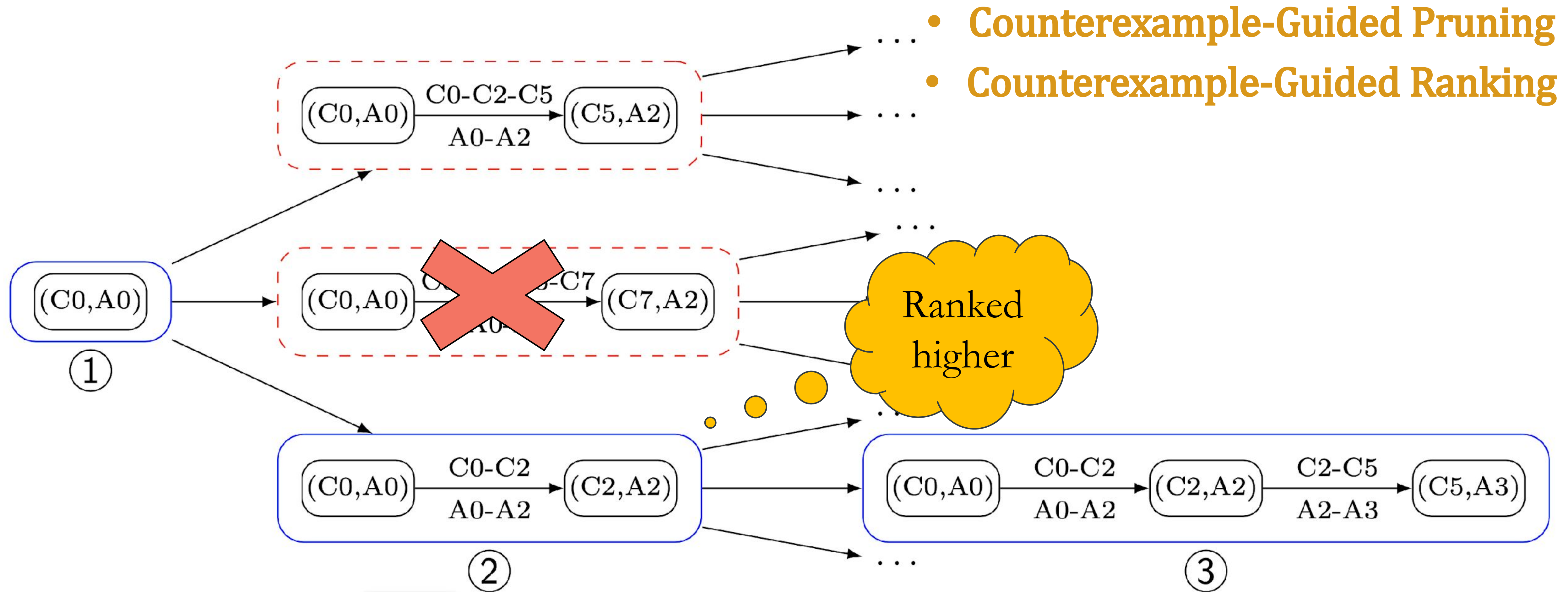


# COUNTEREXAMPLE GUIDED BEST-FIRST SEARCH

- Counterexample-Guided Pruning

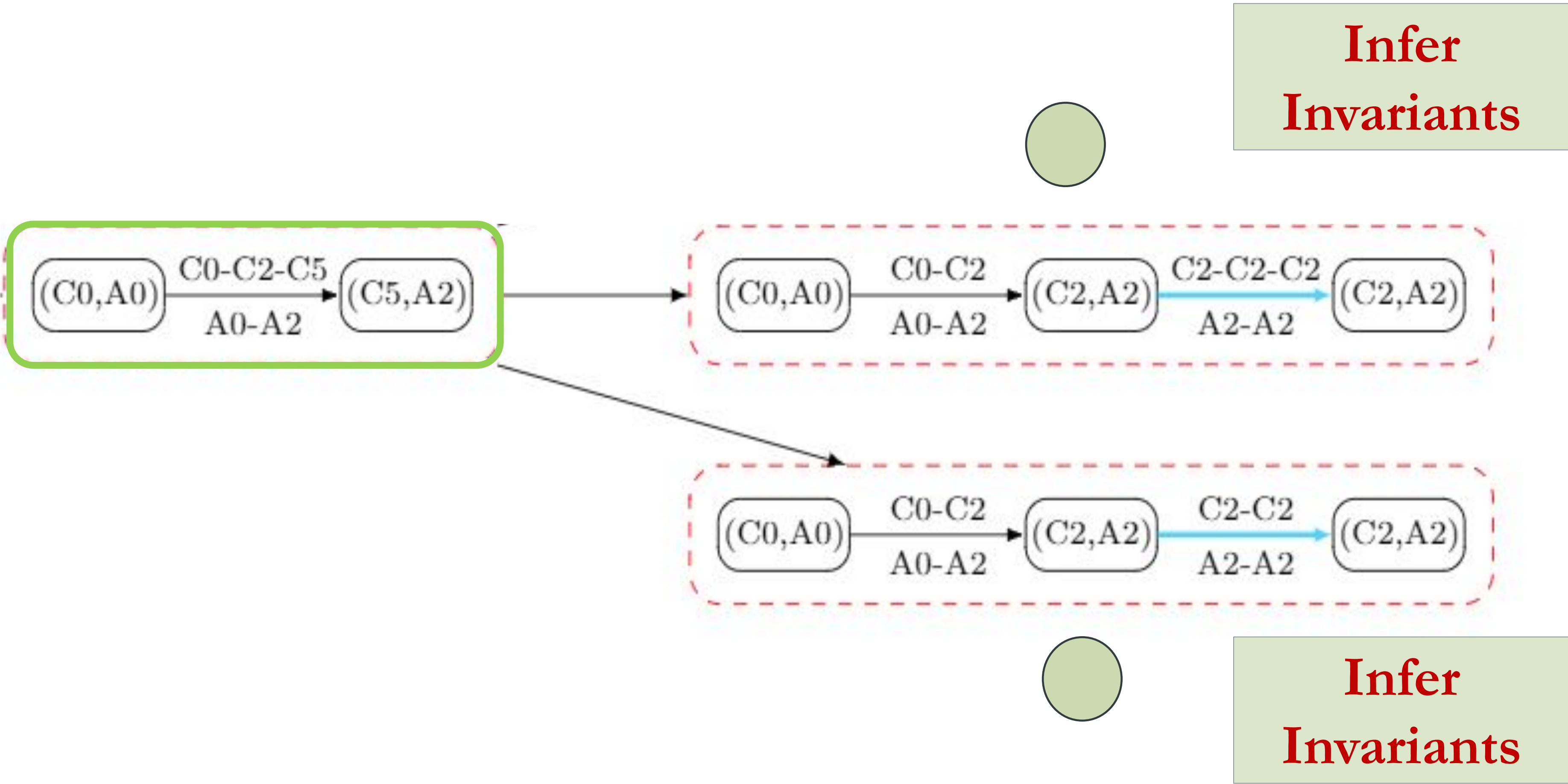


# COUNTEREXAMPLE GUIDED BEST-FIRST SEARCH

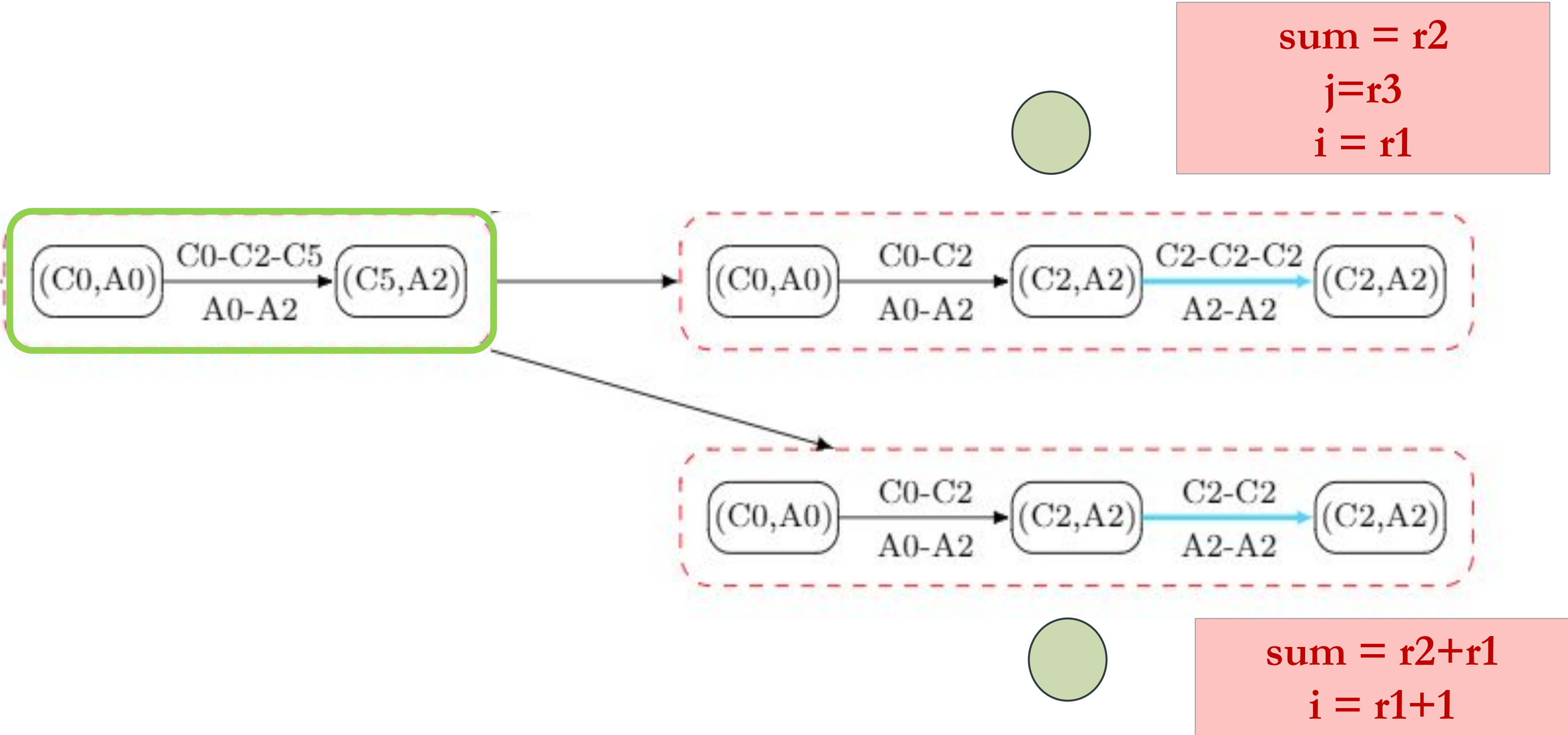




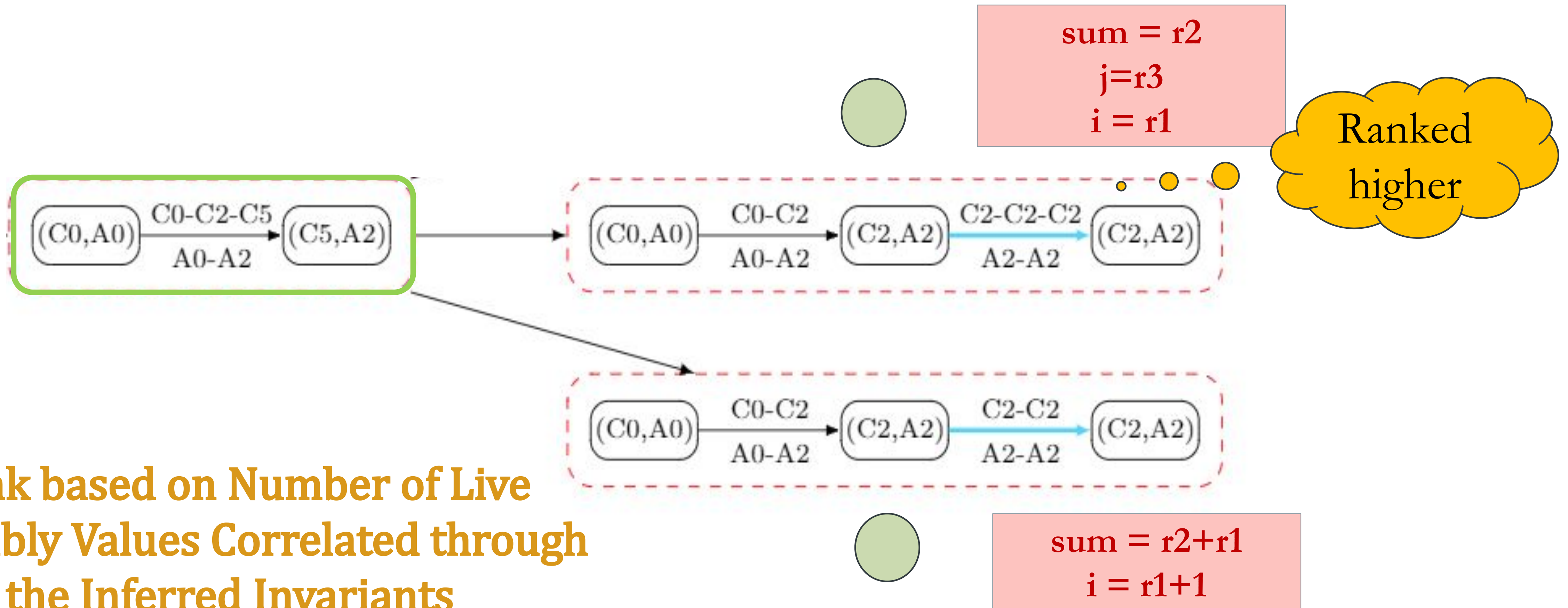
# Infer Invariant Covers for Executed Counterexamples



# Infer Invariant Covers for Executed Counterexamples

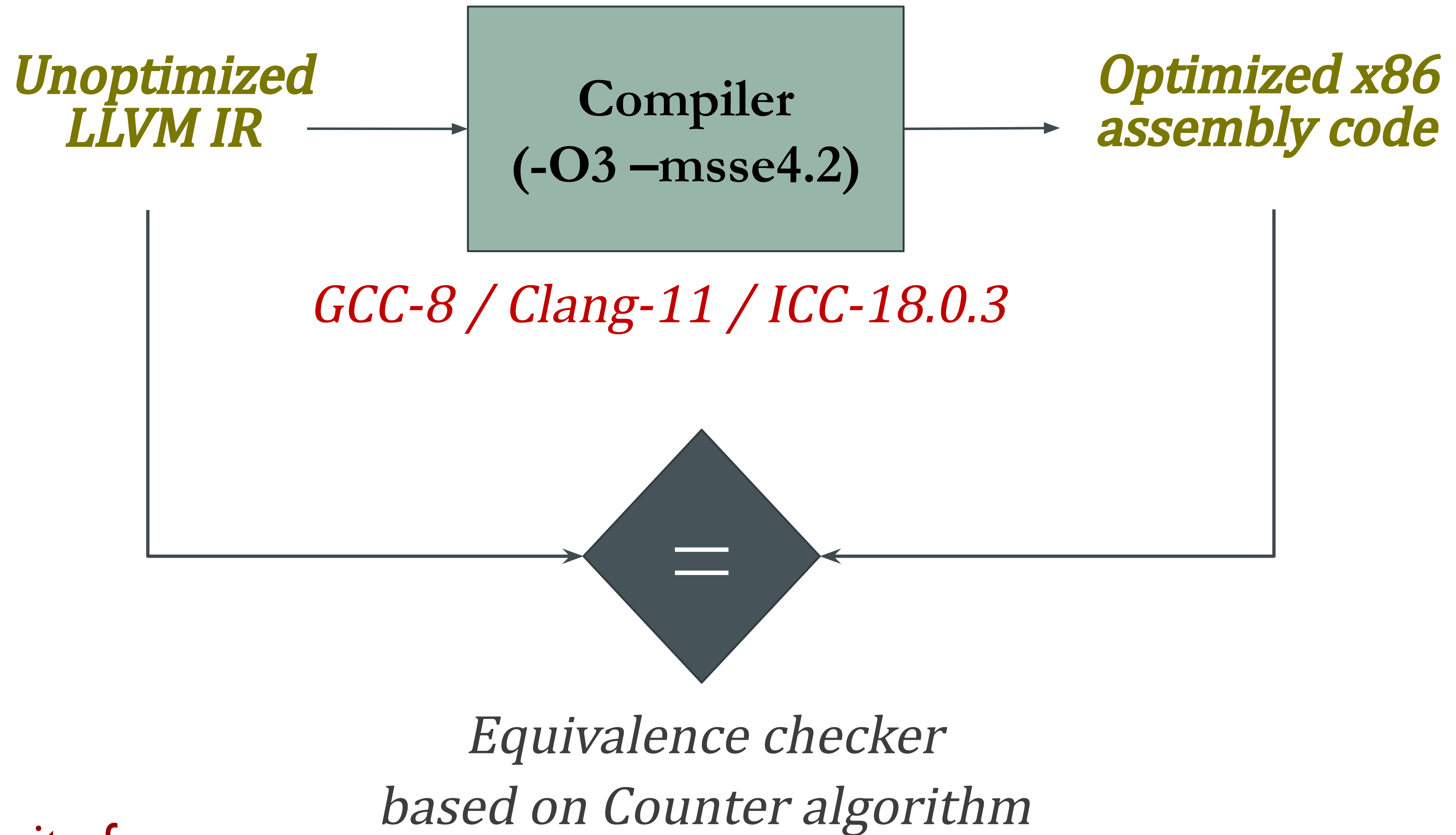


# Infer Invariant Covers for Executed Counterexamples



Rank based on Number of Live Assembly Values Correlated through the Inferred Invariants

# Counter Evaluation



**Evaluated on Testsuite for  
Vectorizing Compilers**



# Bugs Discovered

## <https://compiler.ai/bugs>

- Bug in ICC-16.03 involving integer overflow
- Bug in ICC-16.03 related to incorrect reordering of memory accesses
- Bug in GCC-4.8 involving incorrect reordering of memory accesses
- Bug in Qemu machine emulator that is shipped with Linux/KVM hypervisor
- Three bugs in DietLibc related to missing unsigned-to-signed typecasts
- Bug in the Yices SMT Solver related to incorrect query result



# Automatic Generation of Debug Headers through Blackbox Equivalence Checking

# An Example Debug Session

```
#define LEN 32000
```

```
int X[LEN] , Y[LEN], val;
```

```
C0: void addAndCopy ( ) {
```

```
C1:   for (int i=0; i < LEN; i++) {
```

```
C2:     X[i] = Y[i] + val;
```

```
C3:   }
```

```
EC: }
```

**C Program**

# An Example Debugging Session

```
#define LEN 32000

int X[LEN] , Y[LEN], val;

C0: void addC( ) {
C1:   for (int i=0; i < LEN; i++) {
C2:     X[i] = Y[i] + val;
C3:   }
EC: }
```

## C Program

```
(gdb) break addC:C2
```

```
(gdb) run
```

```
Starting program: addC
```

```
Breakpoint 1, addC () at addC.c:C3
```

```
    X[i] = Y[i] + val;
```

```
(gdb) print i
```

```
$1 = 0
```

```
(gdb) continue
```

```
Continuing.
```


```
Breakpoint 1, addC () at addC.c:C3
```

```
    X[i] = Y[i] + val;
```

```
(gdb) print i
```

```
$2 = 0
```

**i appears to be  
always 0**



# An Example Debugging Session

```
#define LEN 32000

int X[LEN] , Y[LEN], val;

C0: void addC( ) {
C1:   for (int i=0; i < LEN; i++) {
C2:     X[i] = Y[i] + val;
C3:   }
EC: }
```

## C Program

```
(gdb) break addC:C2

(gdb) run
Starting program: addC
Breakpoint 1, addC () at addC.c:C3
    X[i] = Y[i] + val;
(gdb) print i
<value optimized out>
(gdb) continue
Continuing.
Breakpoint 1, addC () at addC.c:C3
    X[i] = Y[i] + val;
(gdb) print i
<value optimized out>
```

# Debug Headers : Src names $\rightarrow$ Asm names

```
# define LEN 32000
```

```
int X [ LEN ], Y [ LEN ], val ;
```

```
C0: void foo () {
```

```
C1:   int i = 0;
```

```
C2:   for ( ; i < LEN ; i ++ )
```

```
C3:   X [ i ] = Y [ i ] + val ;
```

```
EC: }
```

C Program

Hard for developers to  
maintain debugging  
information in the presence  
of aggressive optimization

```
A0: foo:
```

```
A1:  r1 = & X [ 0 ]; r2 = & Y [ 0 ]
```

```
A2:  r3 = val
```

```
A3:  r4 = r1 + 4 * LEN
```

```
A4:  mem [ r1 ] = mem [ r2 ] + r3
```

```
A5:  r1 += 4; r2 += 4
```

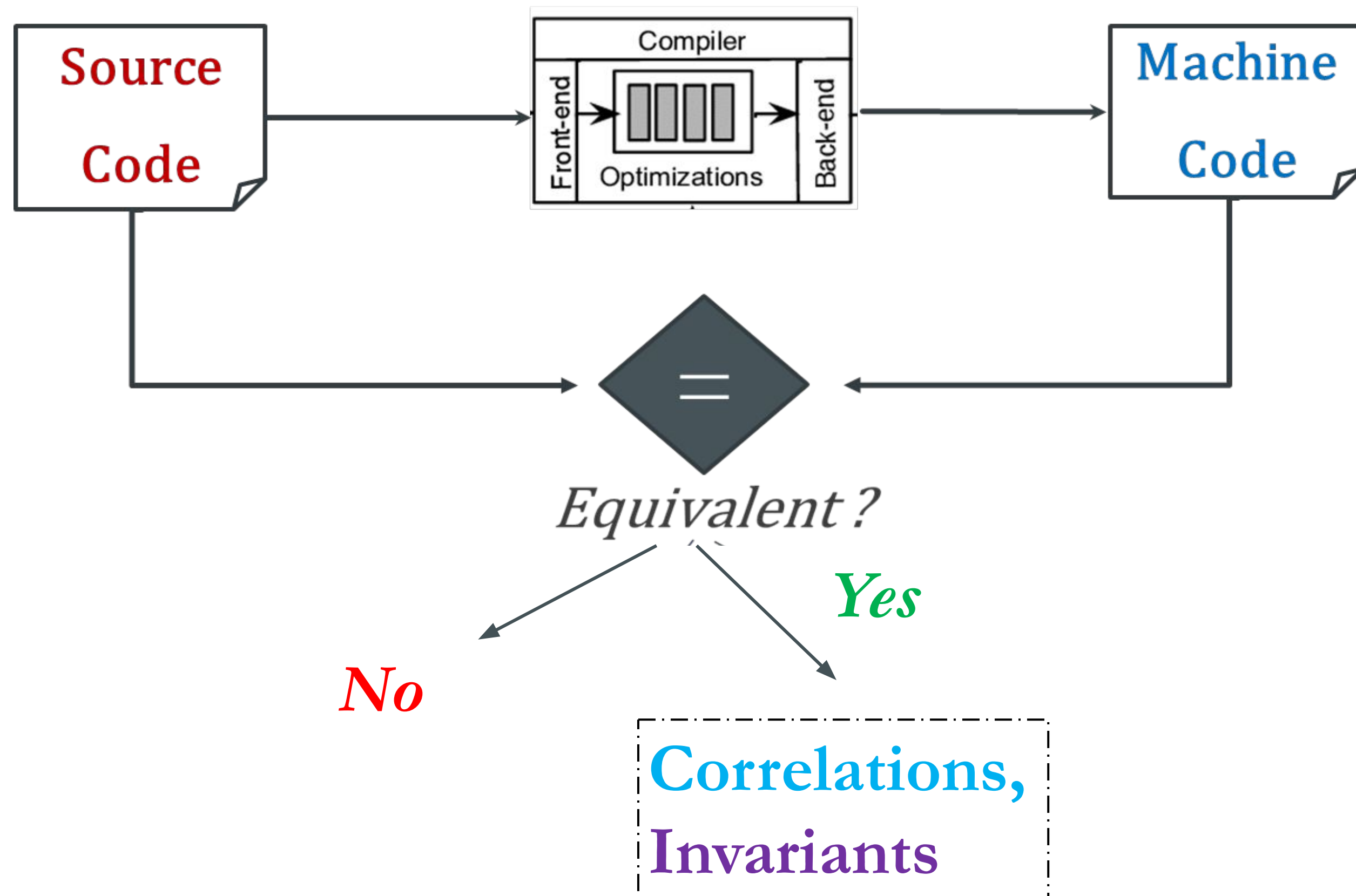
```
A6:  if( r1 != r4 ) goto A4
```

```
EA:  ret
```

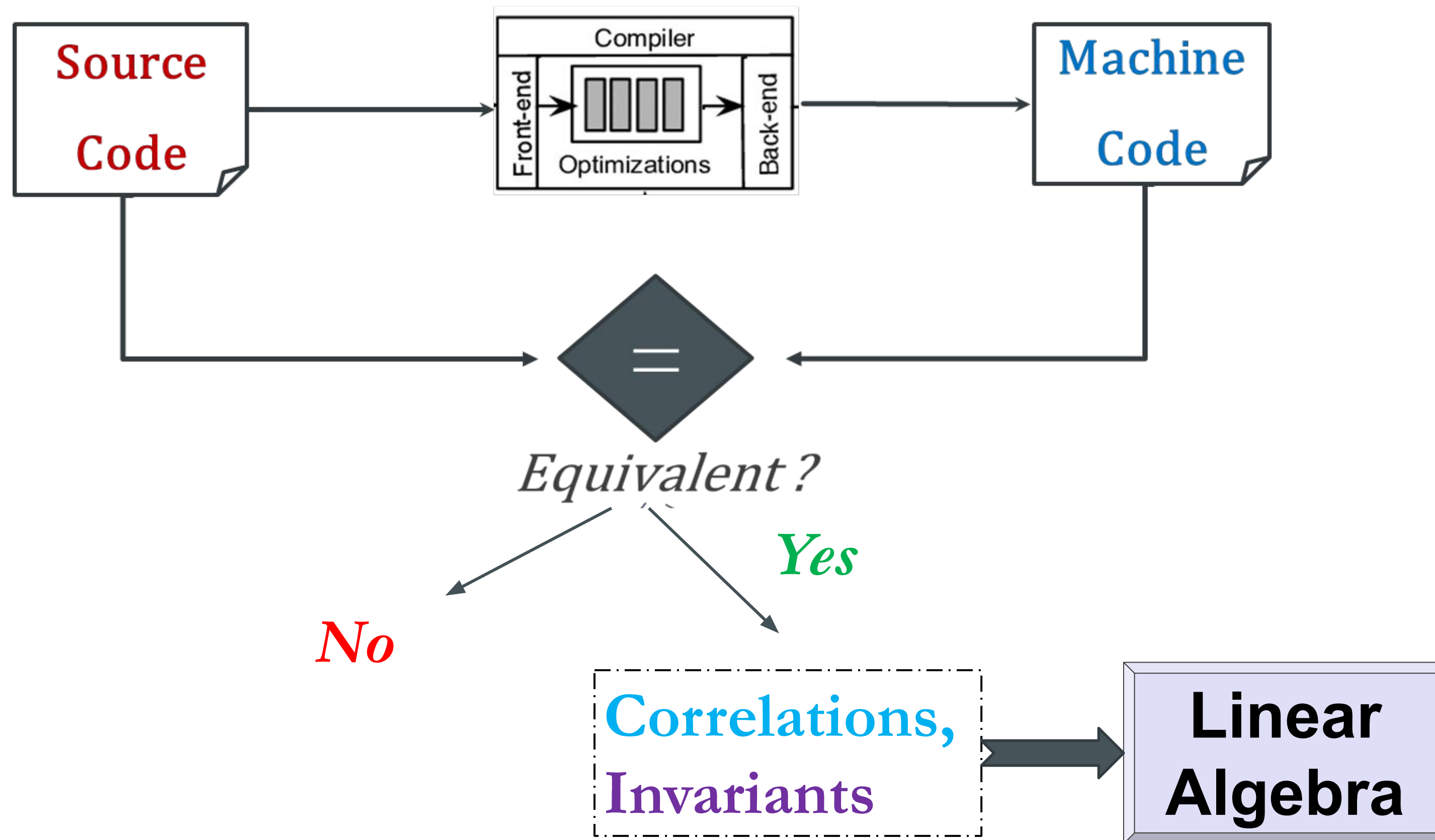
(abstracted) Assembly



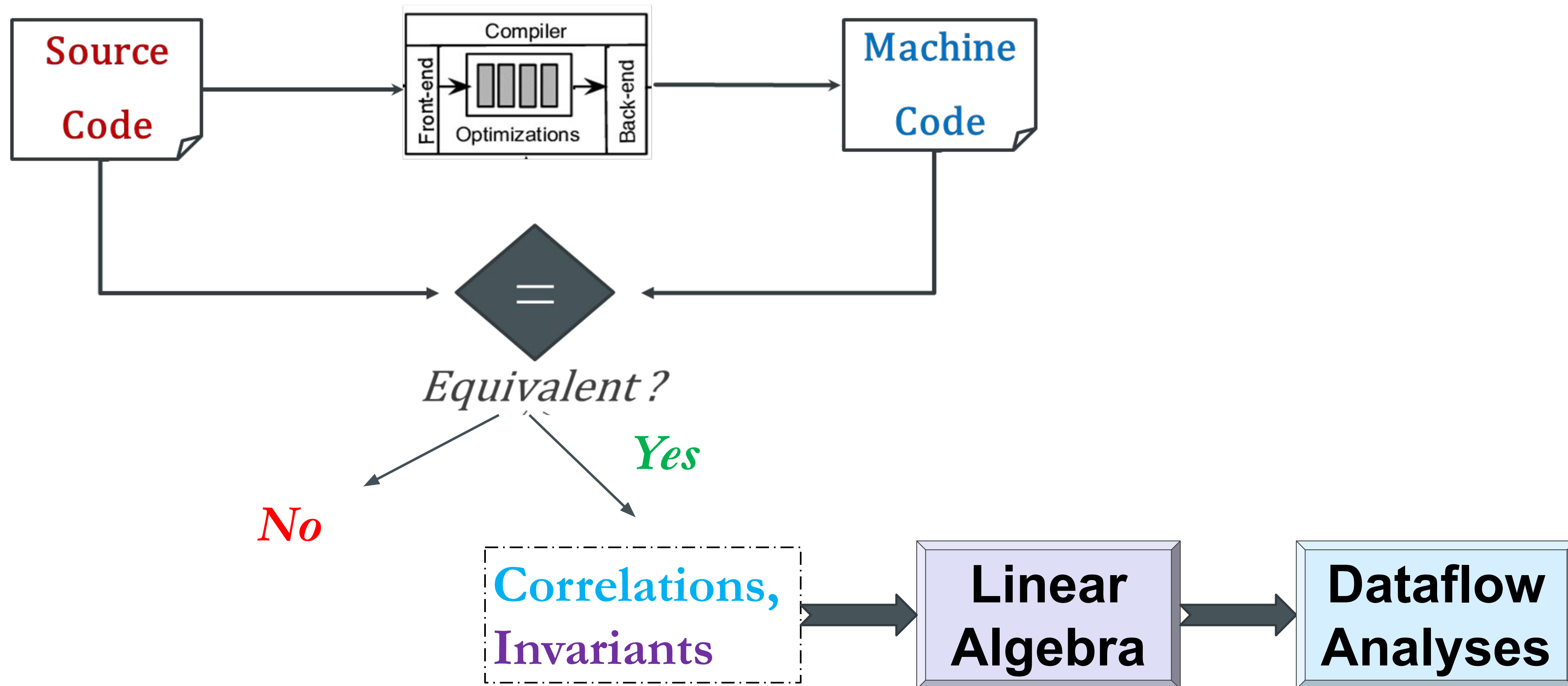
# Automatic Generation of Debug Headers



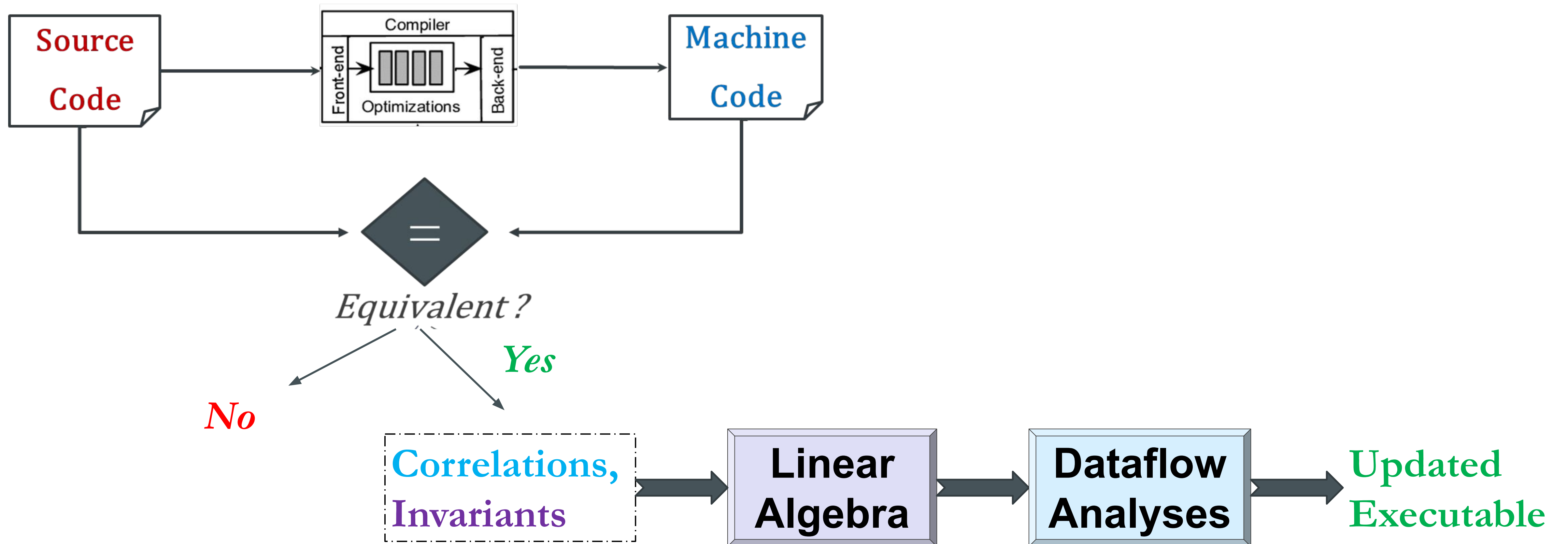
# Automatic Generation of Debug Headers



# Automatic Generation of Debug Headers



# Automatic Generation of Debug Headers



# Summary of Results

On the Testsuite for Vectorizing Compilers

Clang/LLVM	GCC	IntelCC
73 %	75 %	12 %

Percentage of PC-variable pairs where the debugging information was improved by this approach



# **Automatic Generation of Debug Headers through Blackbox Equivalence Checking (CGO **2022)****

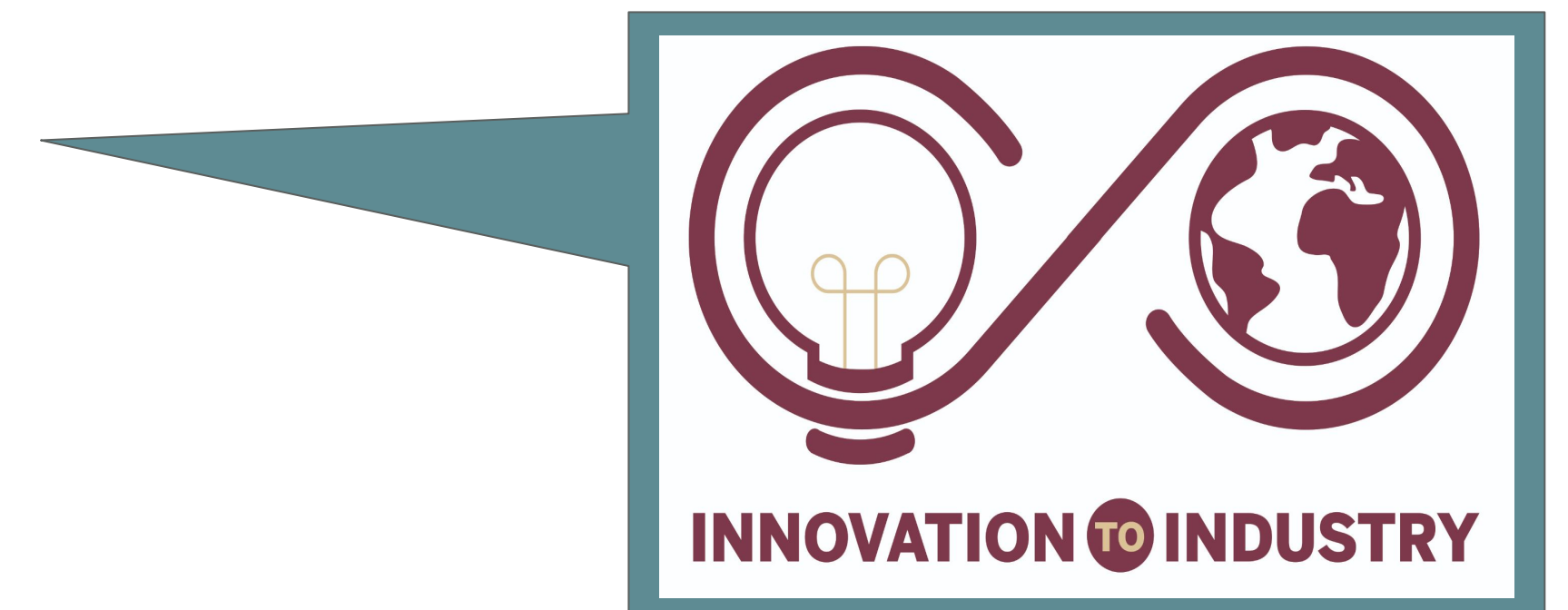
Vaibhav Kurhe, Pratik Karia, Shubhani, Abhishek Rose, Sorav Bansal  
Indian Institute Of Technology Delhi

# CONCLUSIONS

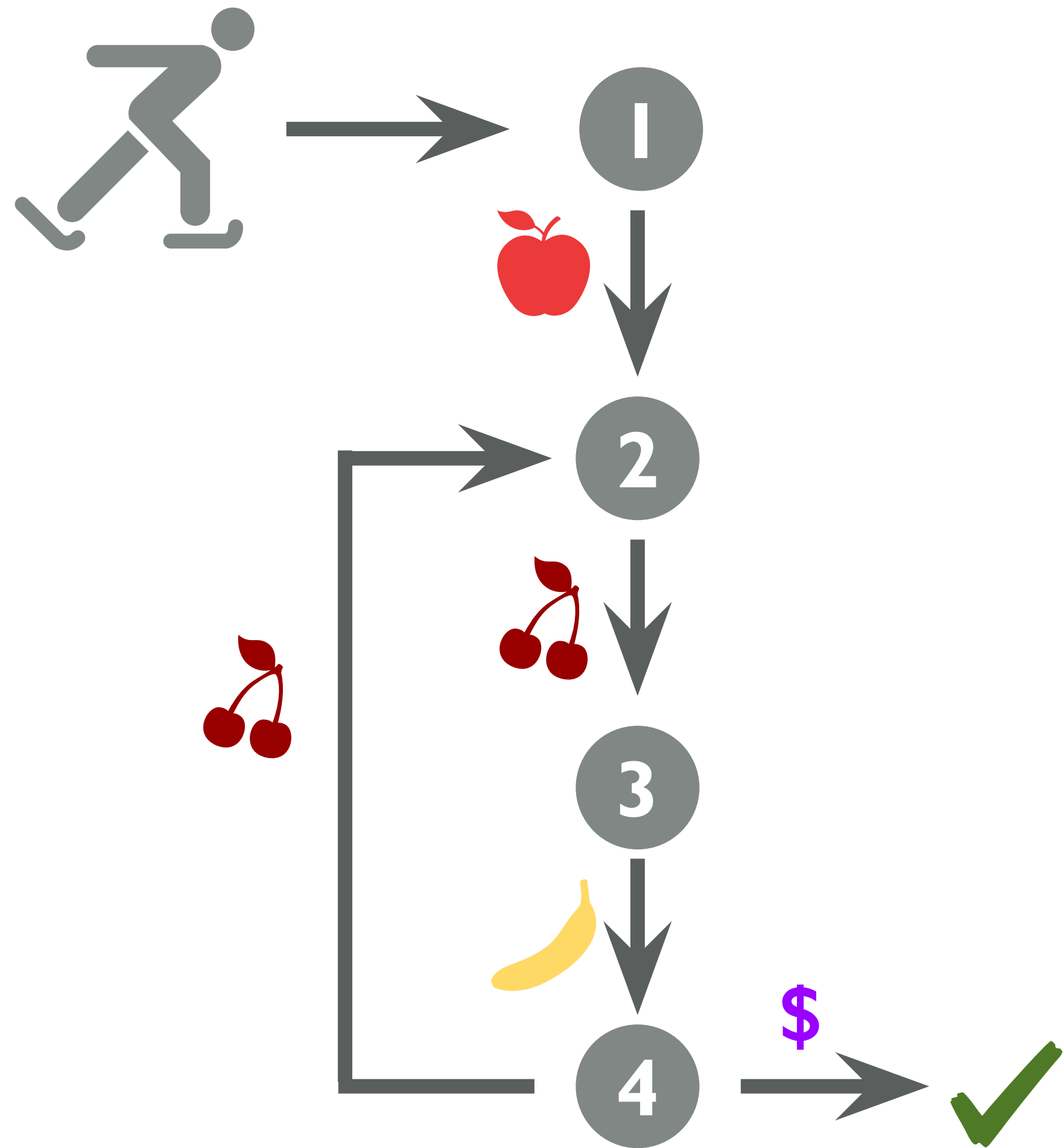
- Compiler Development is Hard but Increasingly Important
- Superoptimization is a Plausible Solution
- Equivalence Checking is an Important Pre-Requisite
- Scalable Algorithms for Equivalence Checking are Possible
  - And have several other applications



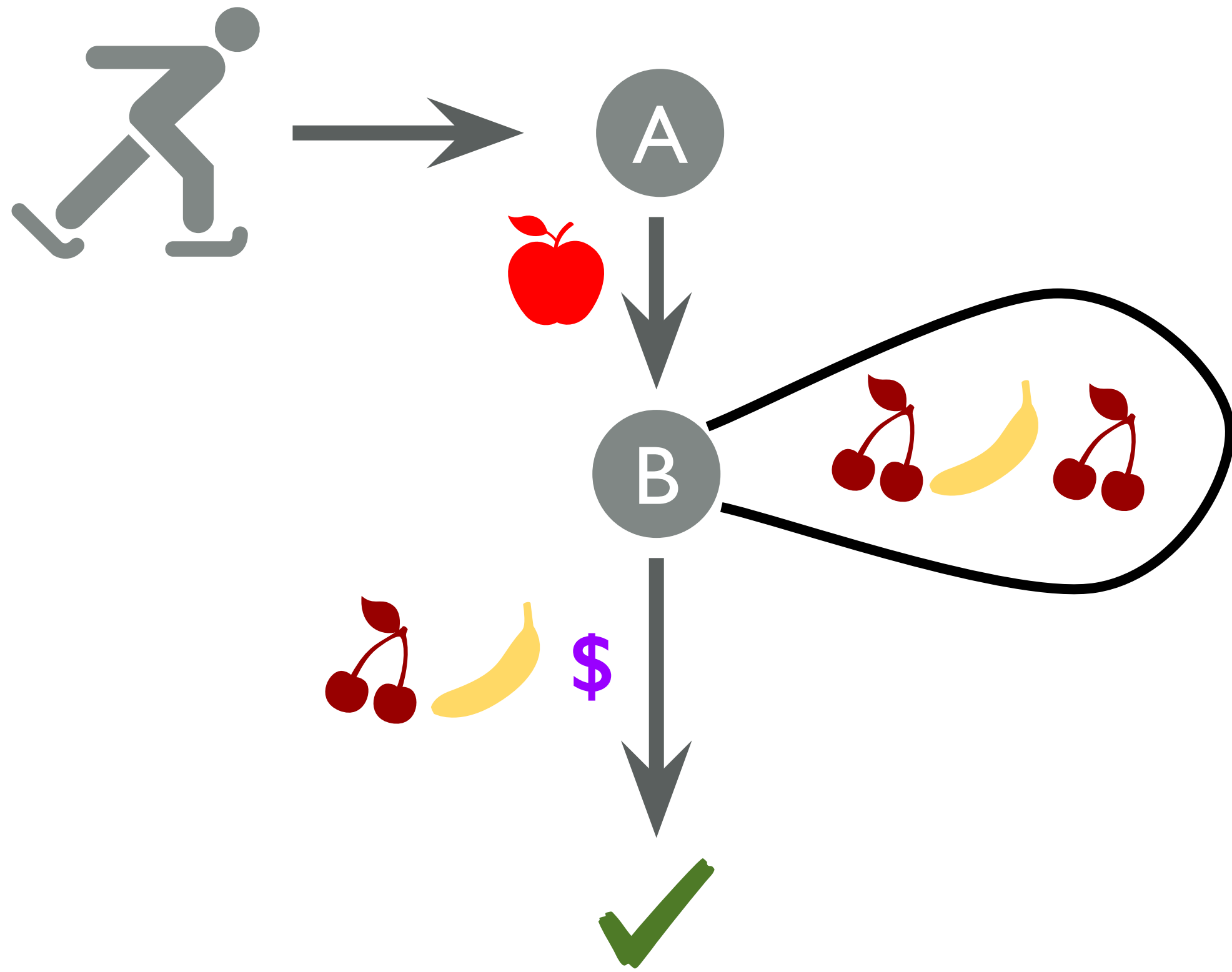
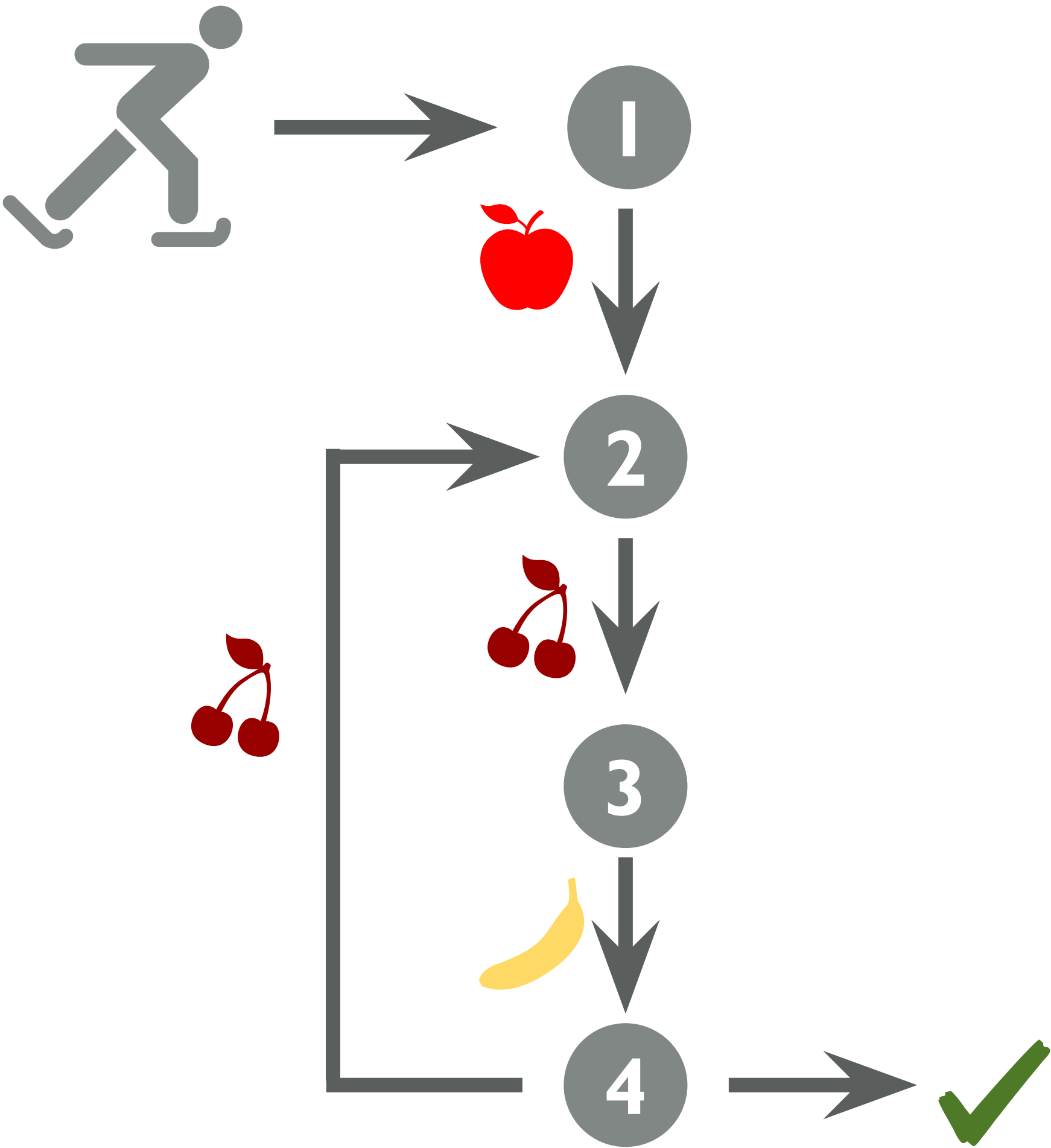
COMPILERAI  
<https://compiler.ai>



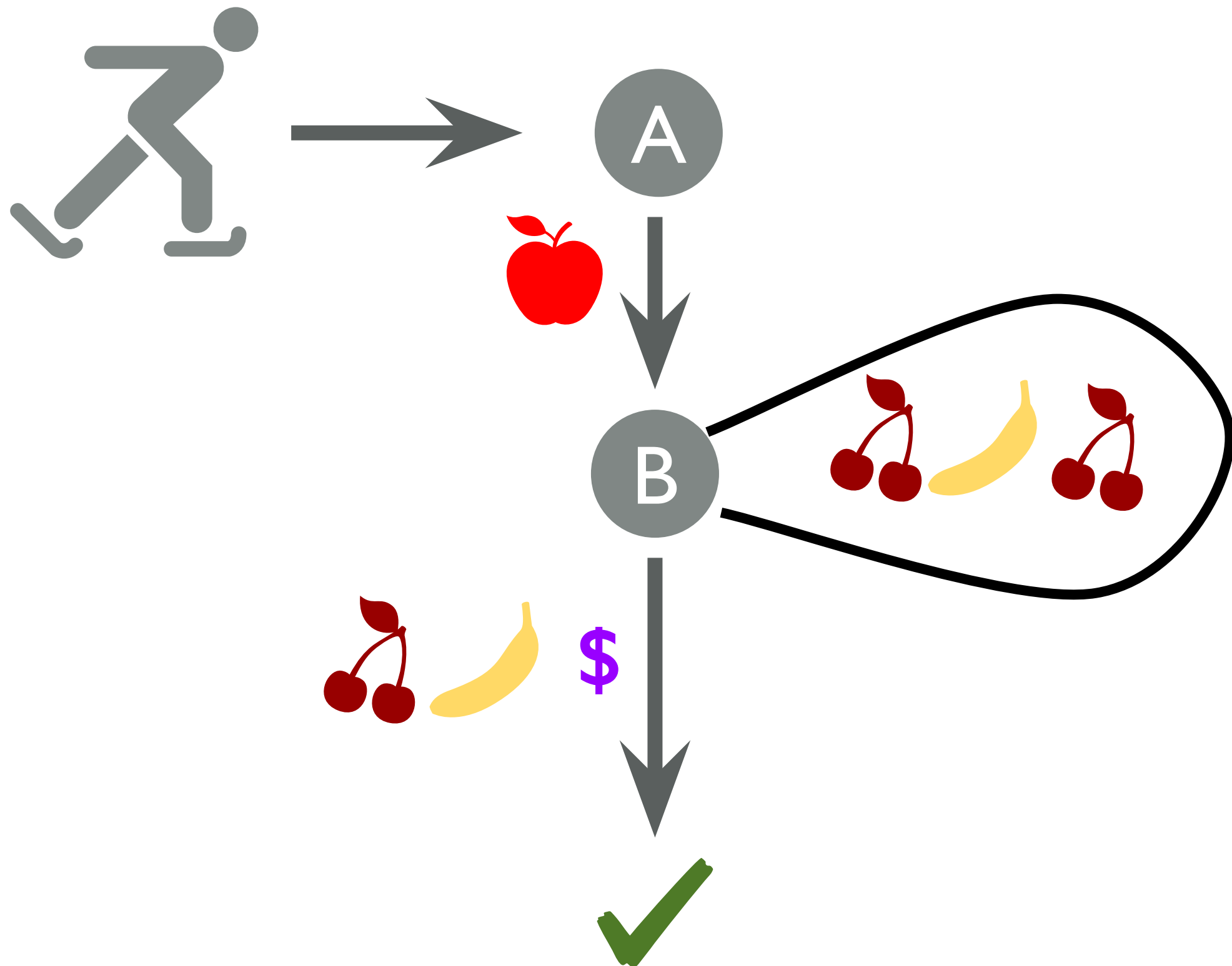
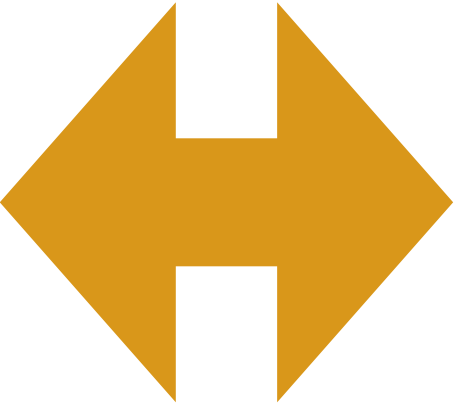
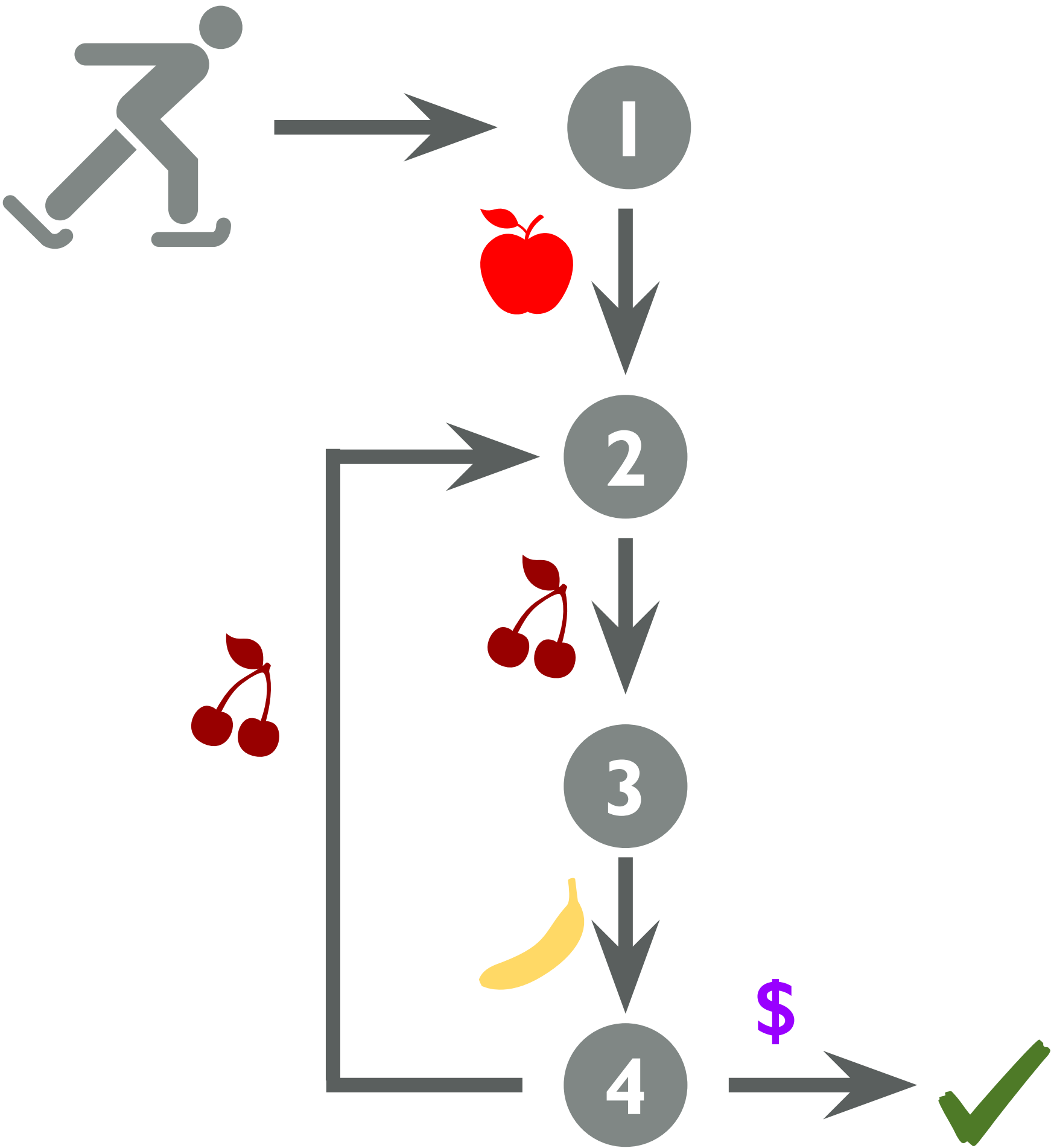
# DETERMINISTIC FINITE AUTOMATON



# TWO DFAS

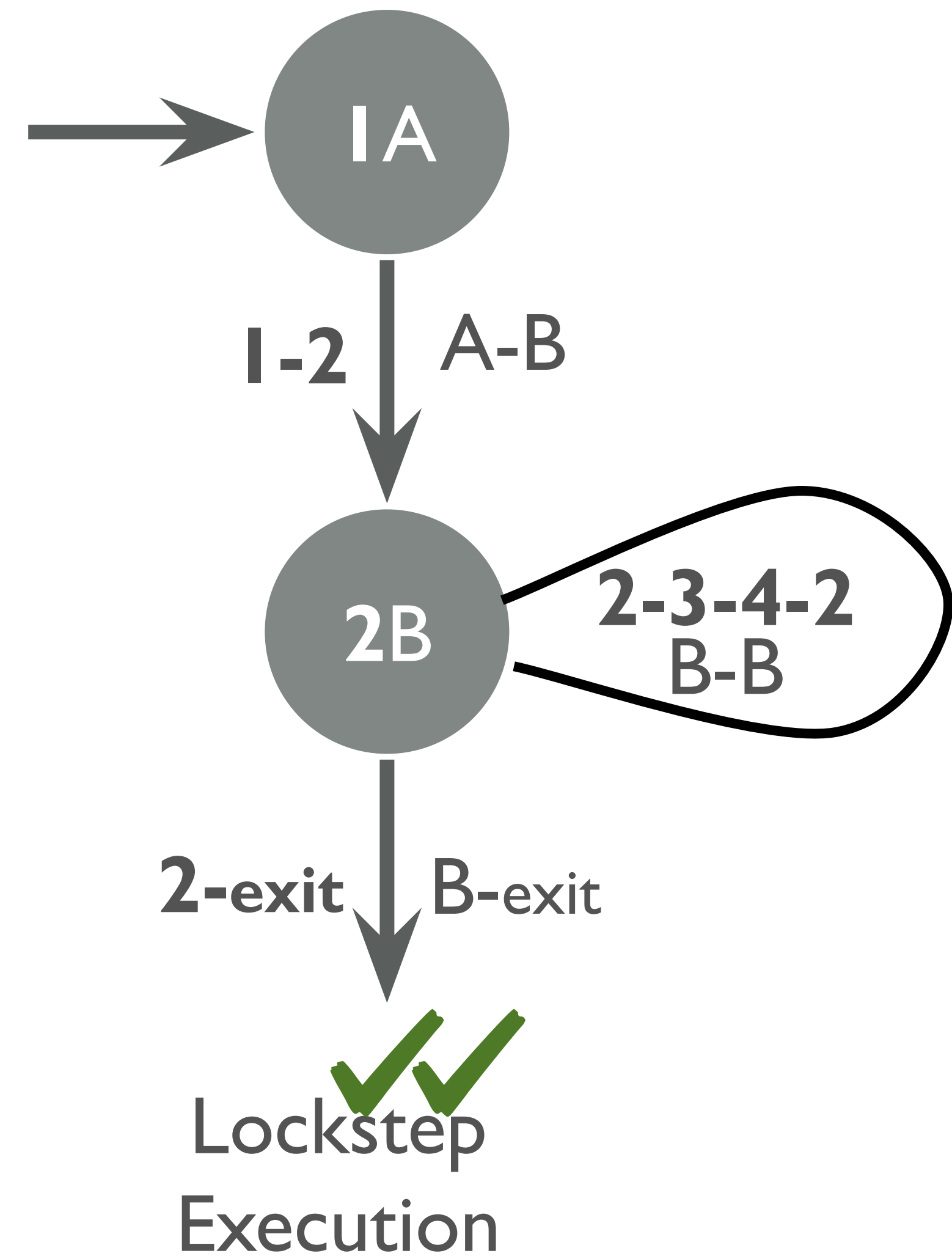
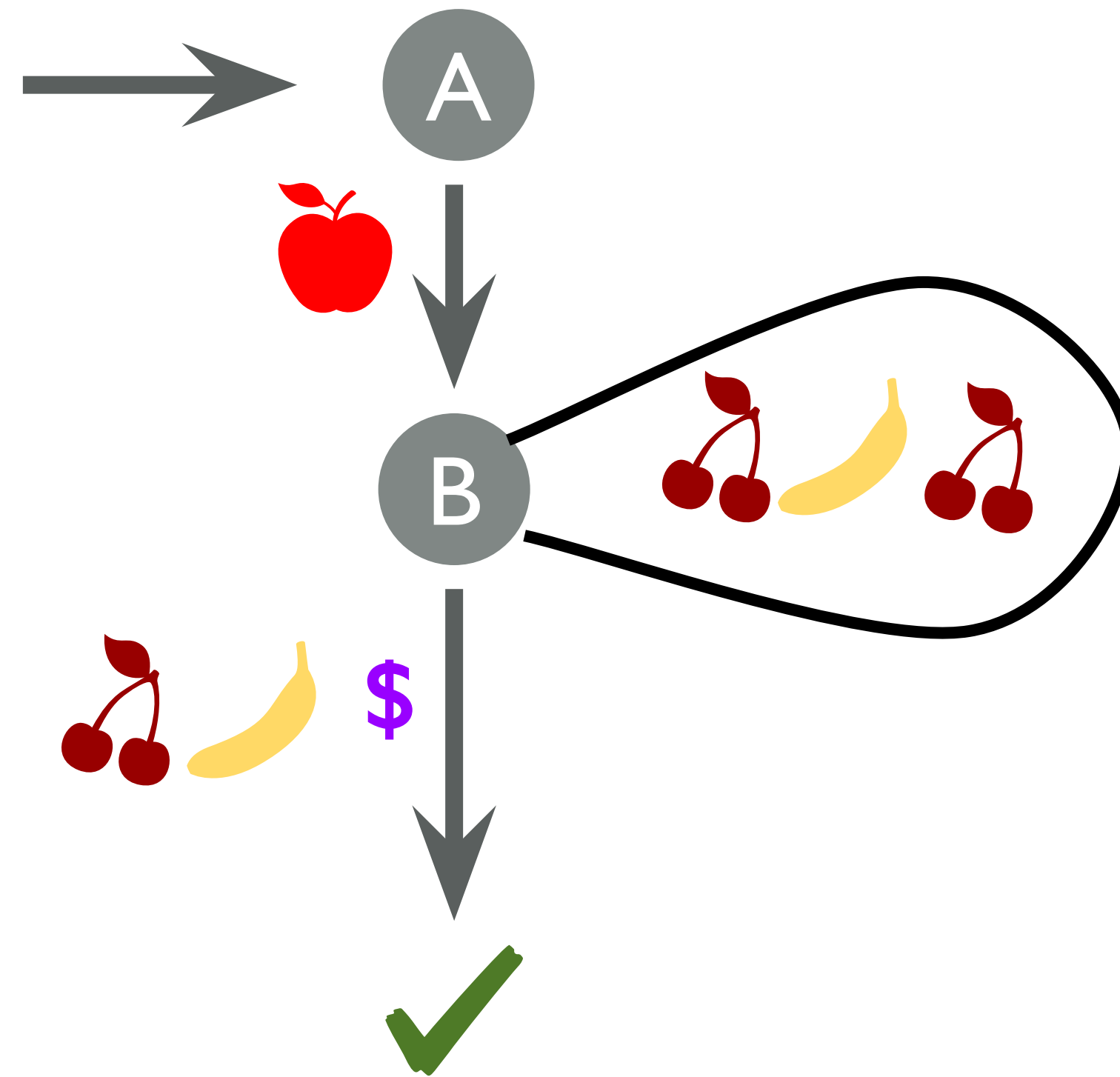
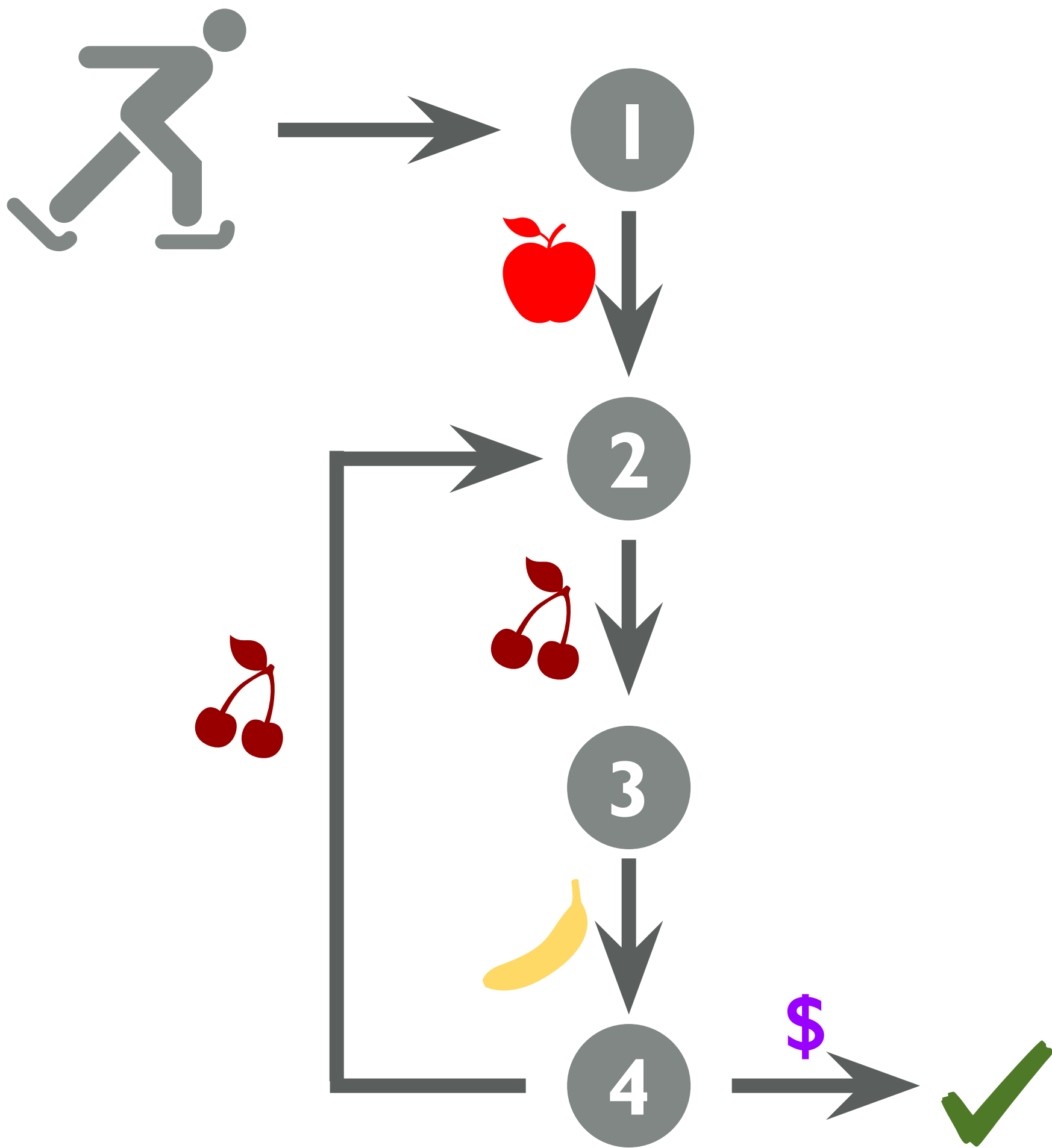


# EQUIVALENCE





# BISIMULATION AS A PRODUCT DFA



# IMPERATIVE LANGUAGE SYNTAX

```
if eat() != apple //Head1
  ERROR
loop forever { //Body 1
  if eat() != cherry
    ERROR
  if eat() != banana
    ERROR
  next = eat()
  if next == cherry
    CONTINUE
  if next == $
    STOP
}
```

```
if eat() != apple //Head2
  ERROR
loop forever { //Body 2
  n1 = eat()
  n2 = eat()
  n3 = eat()
  if n1 == cherry
    && n2 == banana
    && n3 == cherry
    CONTINUE
  else if n1 == cherry
    && n2 == banana
    && n3 == $
    STOP
  else ERROR
}
```

```
Head1
Head2
loop forever {
  Body1
  Body2
}
```

# IMPERATIVE LANGUAGE SYNTAX

```
if eat() != apple //Head1
  ERROR
loop forever { //Body 1
  if eat() != cherry
    ERROR
  if eat() != banana
    ERROR
  next = eat()
  if next == cherry
    CONTINUE
  if next == $
    STOP
}
```

```
if eat() != apple //Head2
  ERROR
loop forever { //Body 2
  n1 = eat()
  n2 = eat()
  n3 = eat()
  if n1 == cherry
    && n2 == banana
    && n3 == cherry
    CONTINUE
  else if n1 == cherry
    && n2 == banana
    && n3 == $
    STOP
  else ERROR
}
```

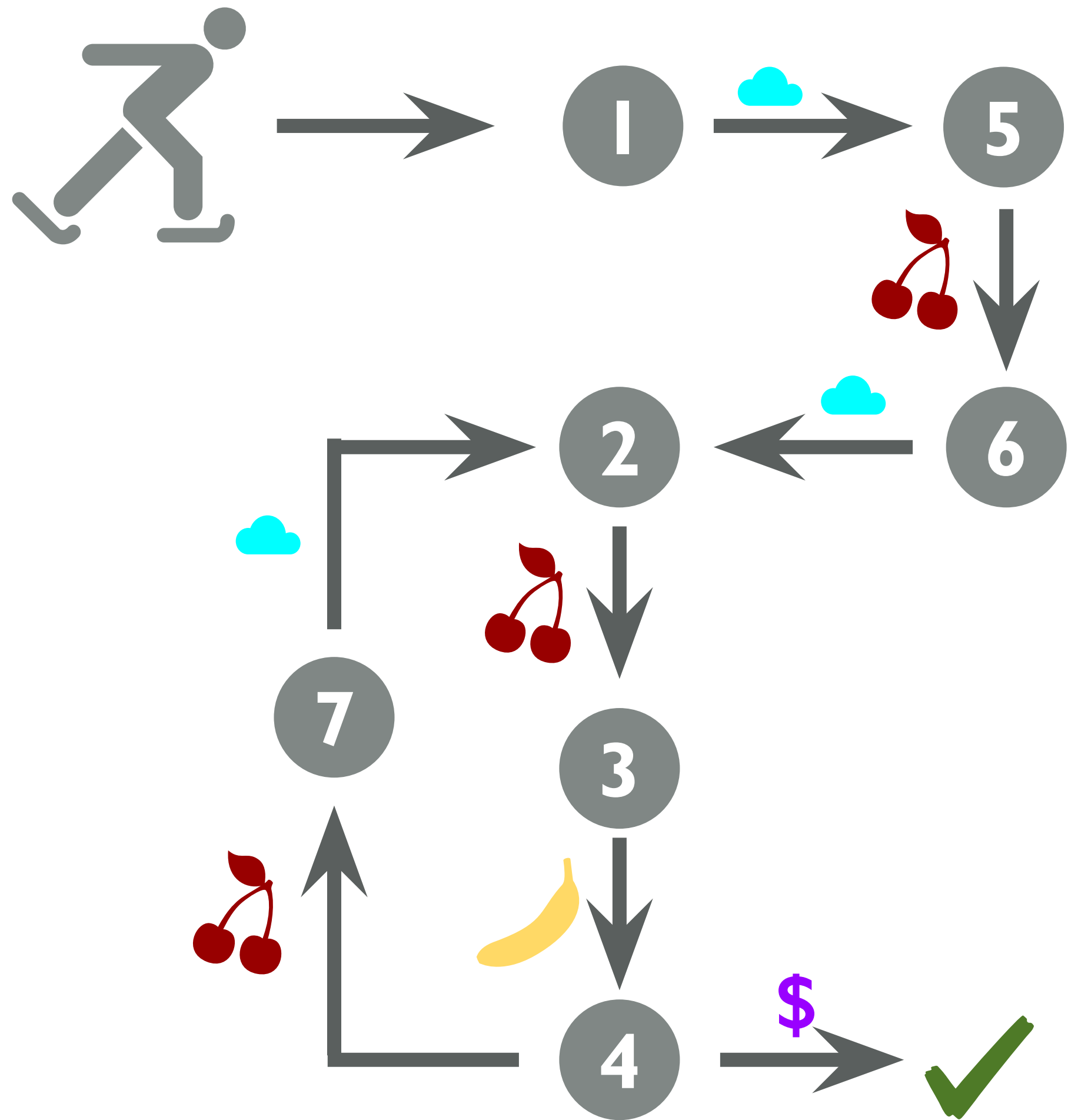
```
Head1
Head2
loop forever {
  Body1
  Body2
}
```



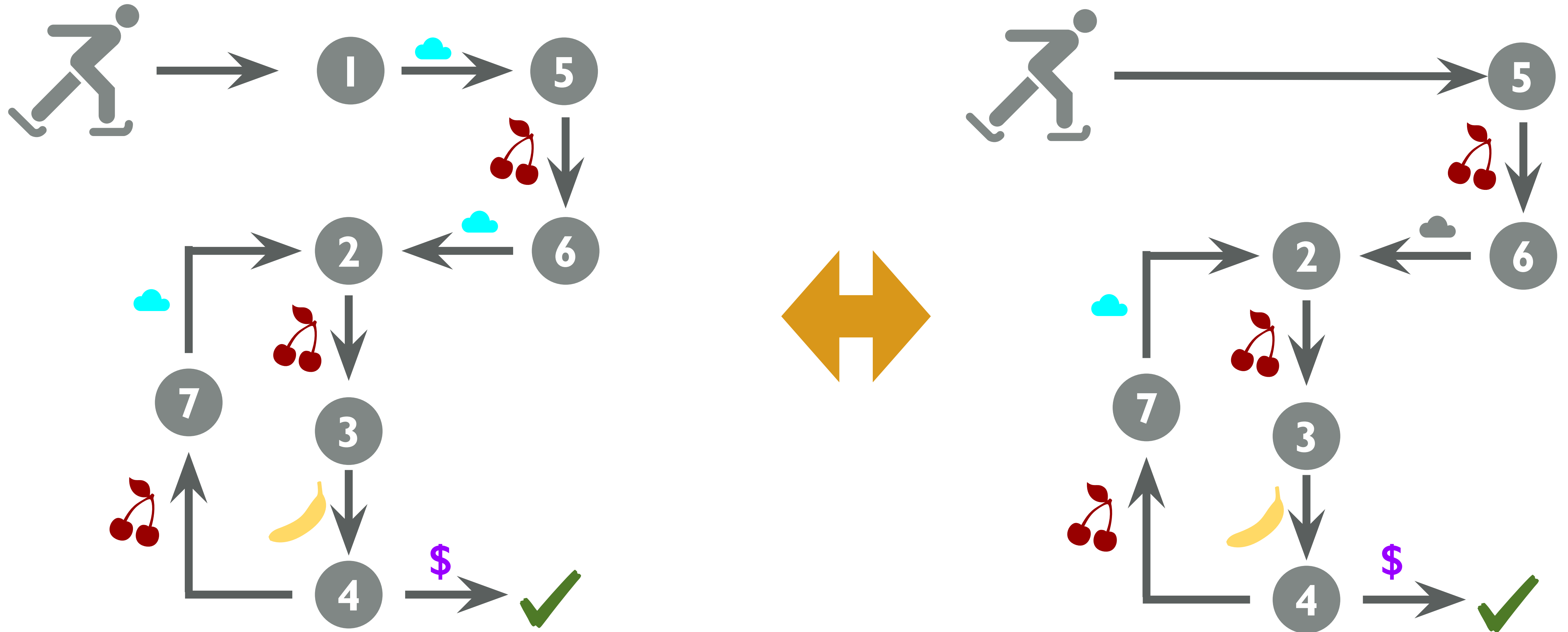
```
Head1
Head2
loop forever {
  Body1
}
loop forever {
  Body2
}
```



# INTERNAL ACTION

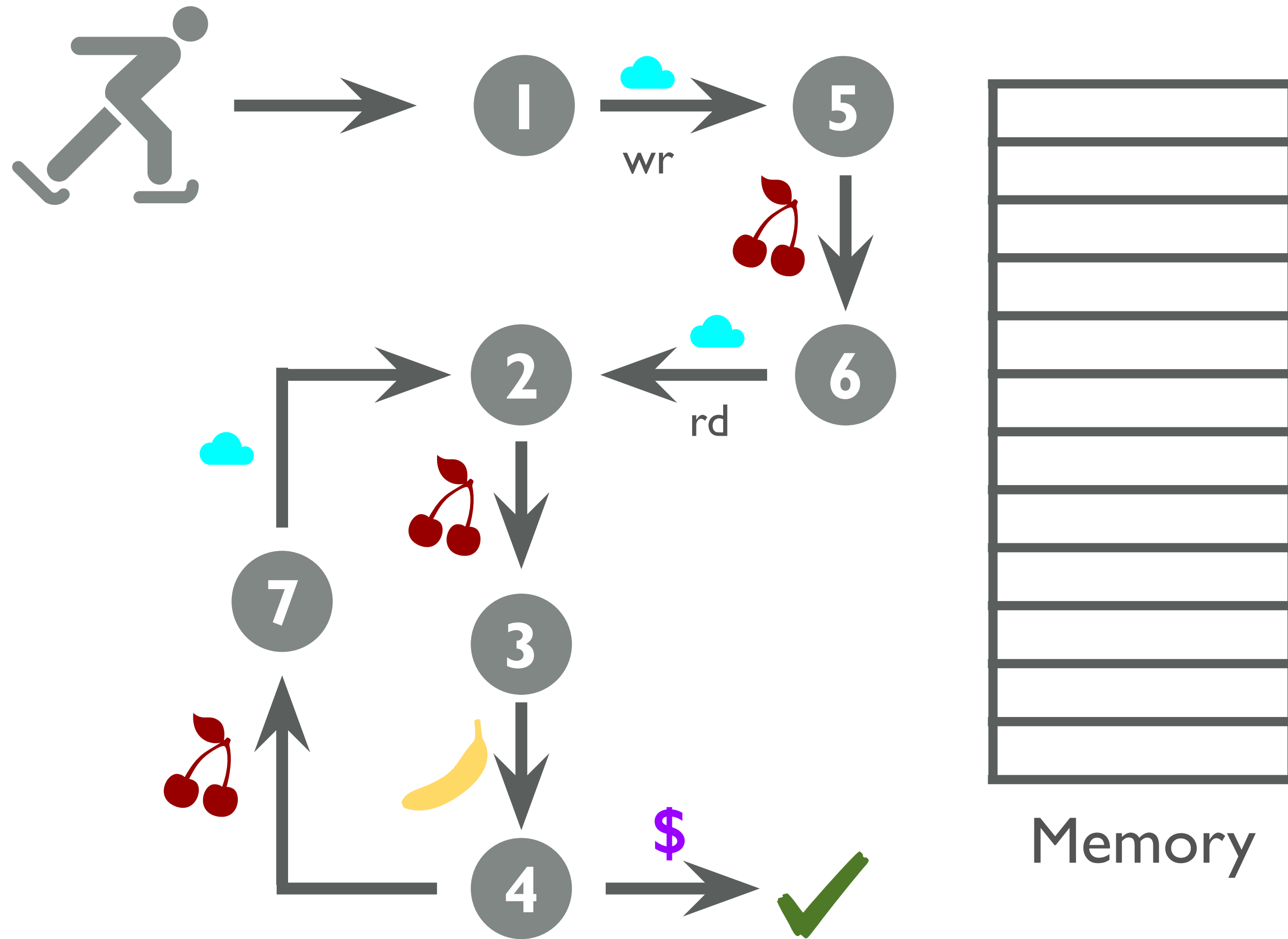


# EQUUIVALENCE IN THE PRESECE OF INTERNAL ACTIONS

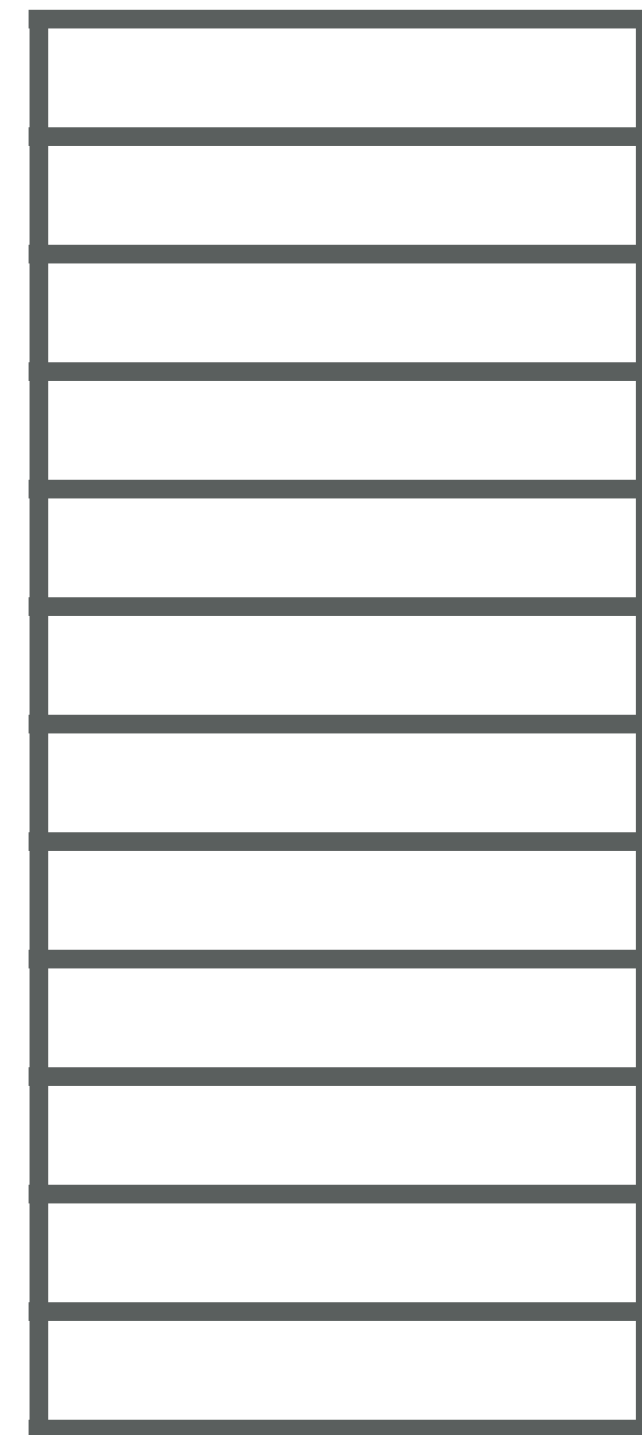
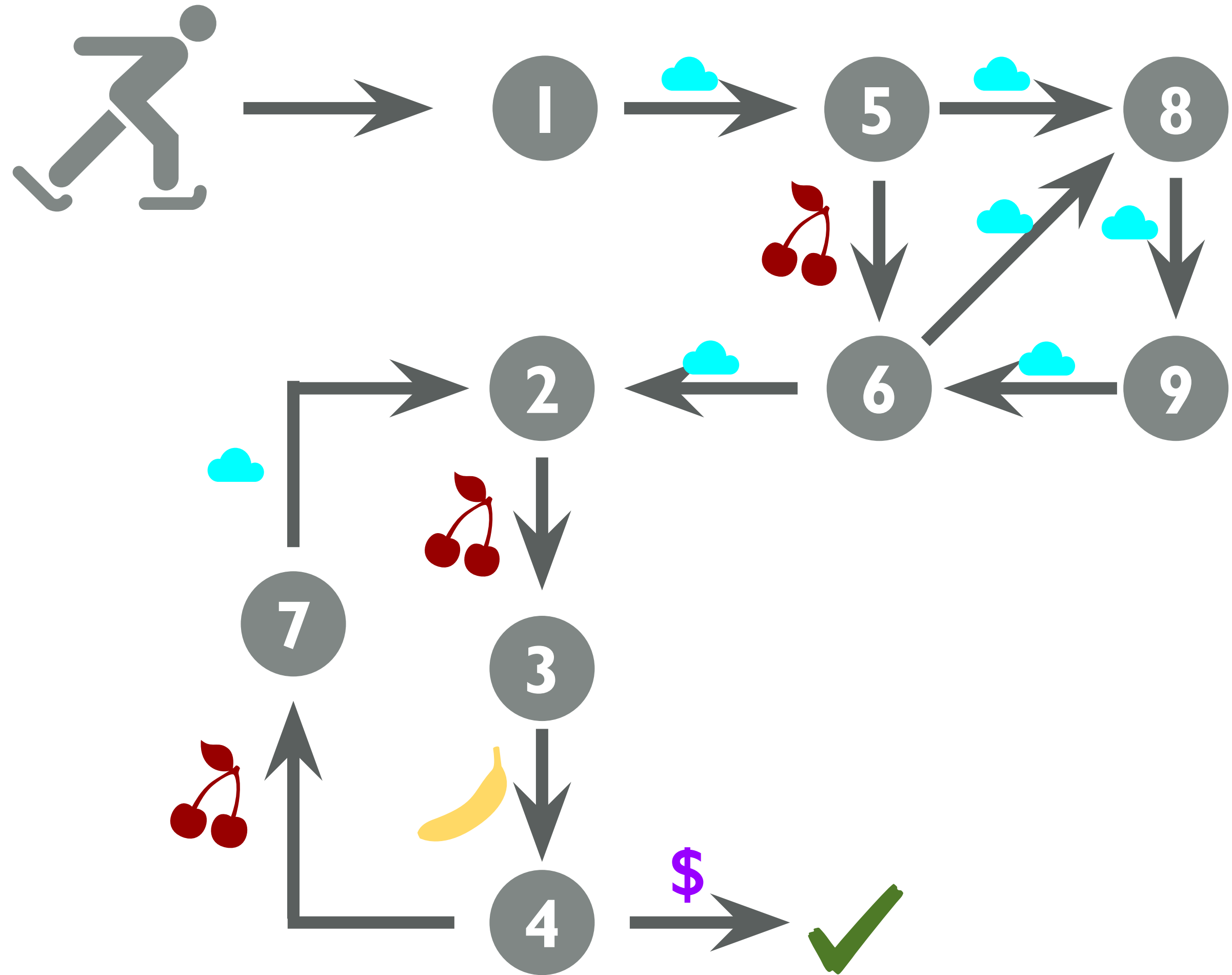




# MEMORY

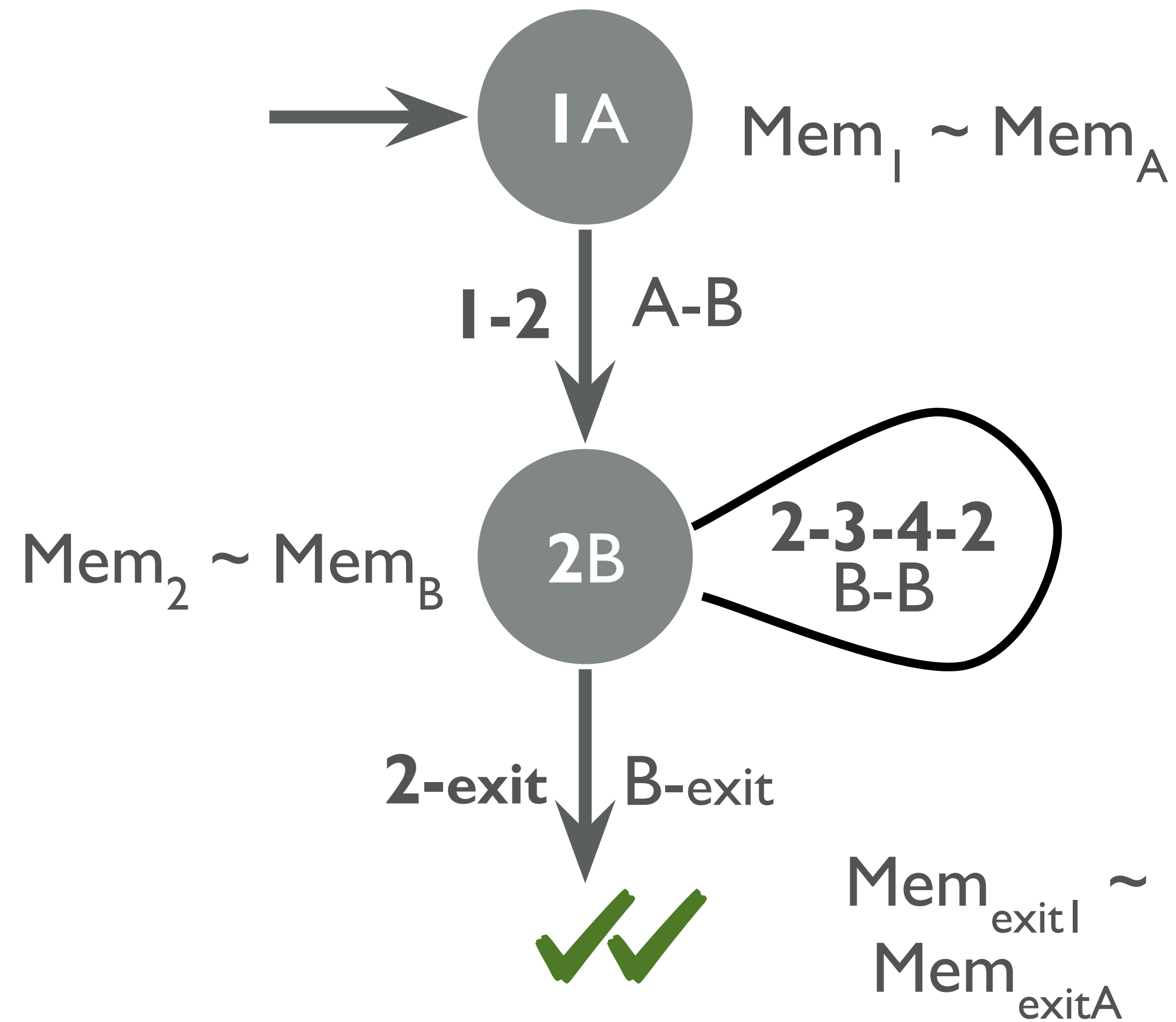


# MEMORY WITH LOOPS

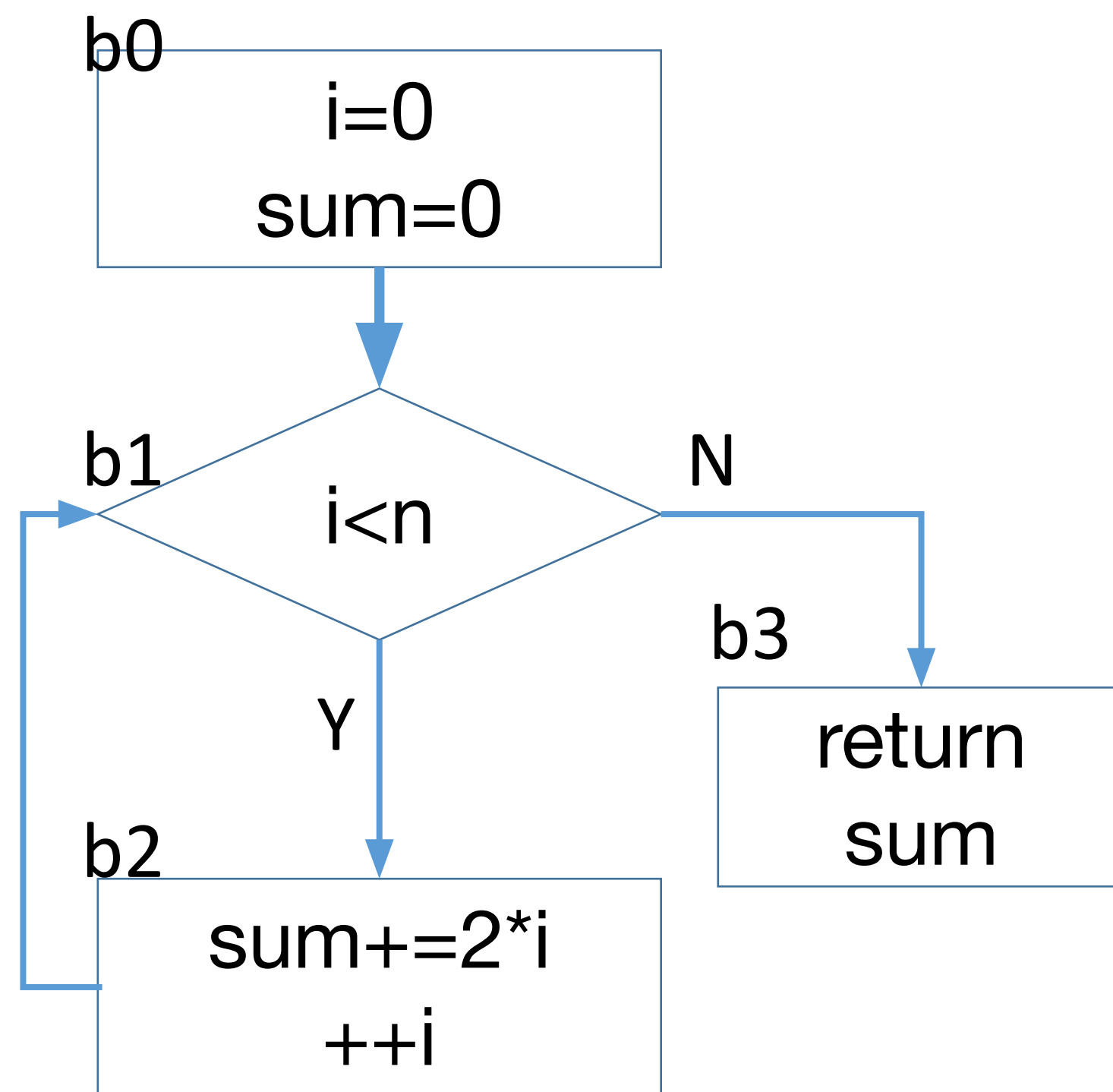


Memory

# BISIMULATION WITH MEMORY RELATIONS



# EXAMPLE 1



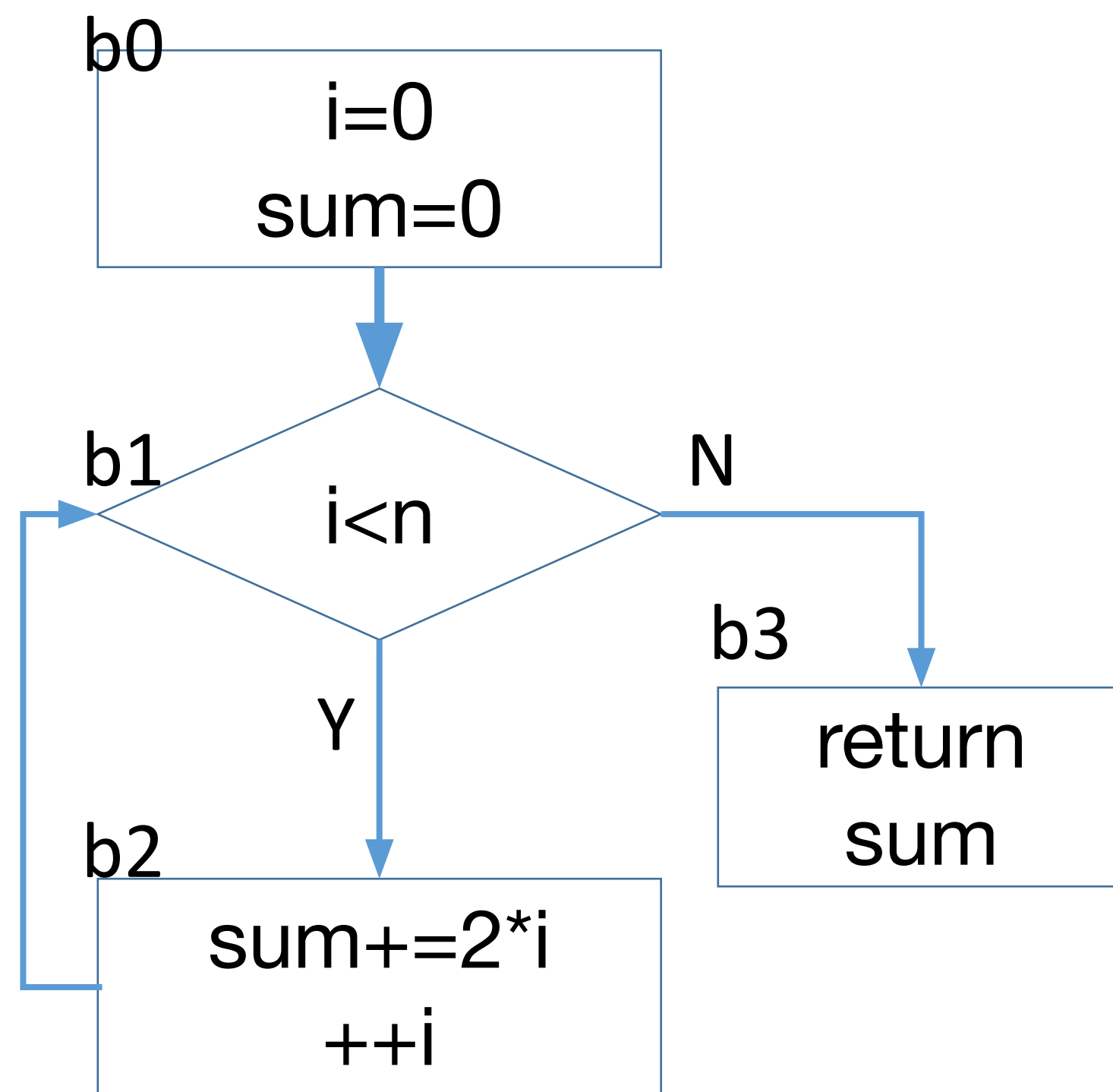
Program 1:

Computes:  $\Sigma$

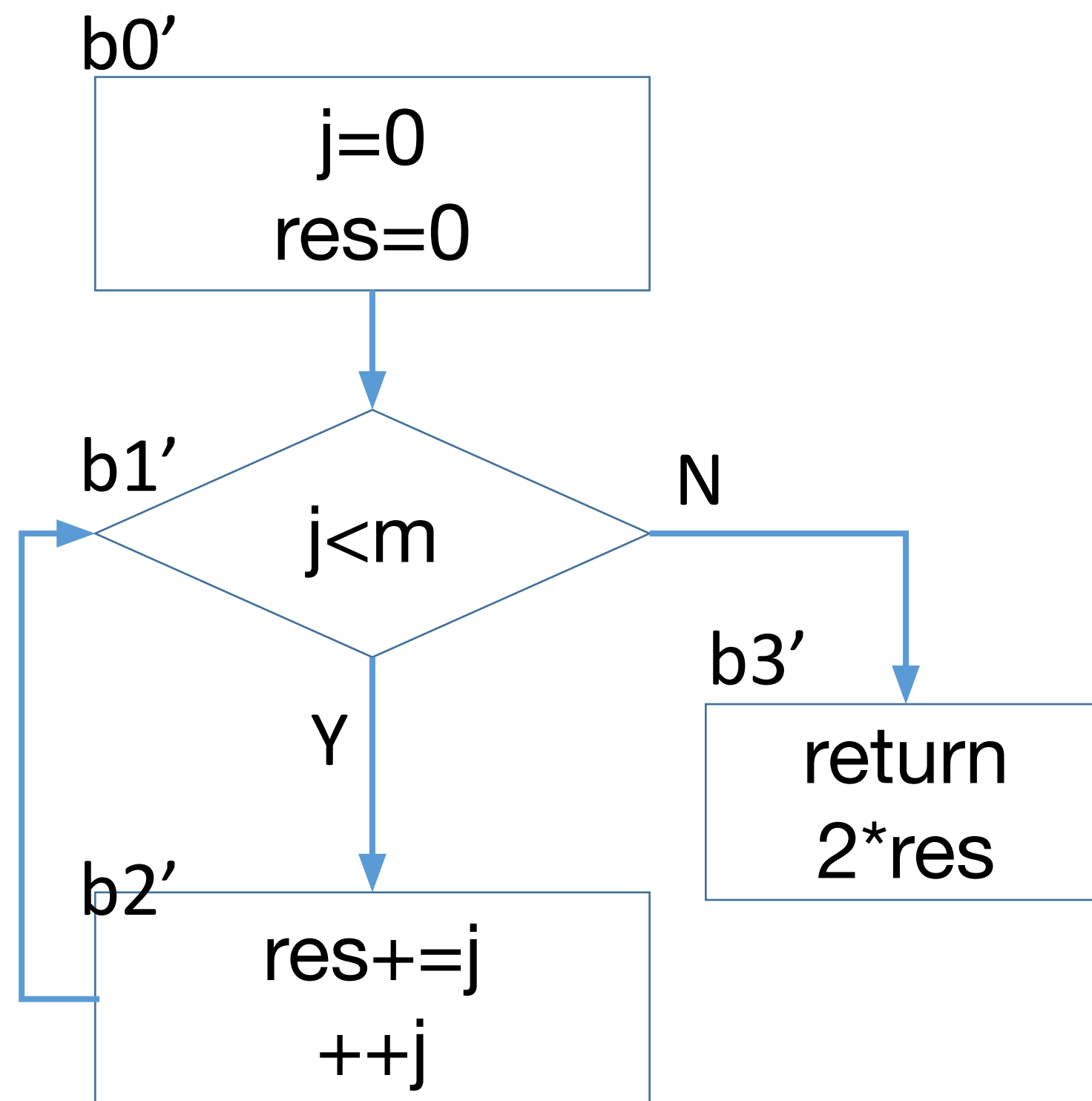
$(2*i)$

For  $i \in [0, n)$

# EXAMPLE 1



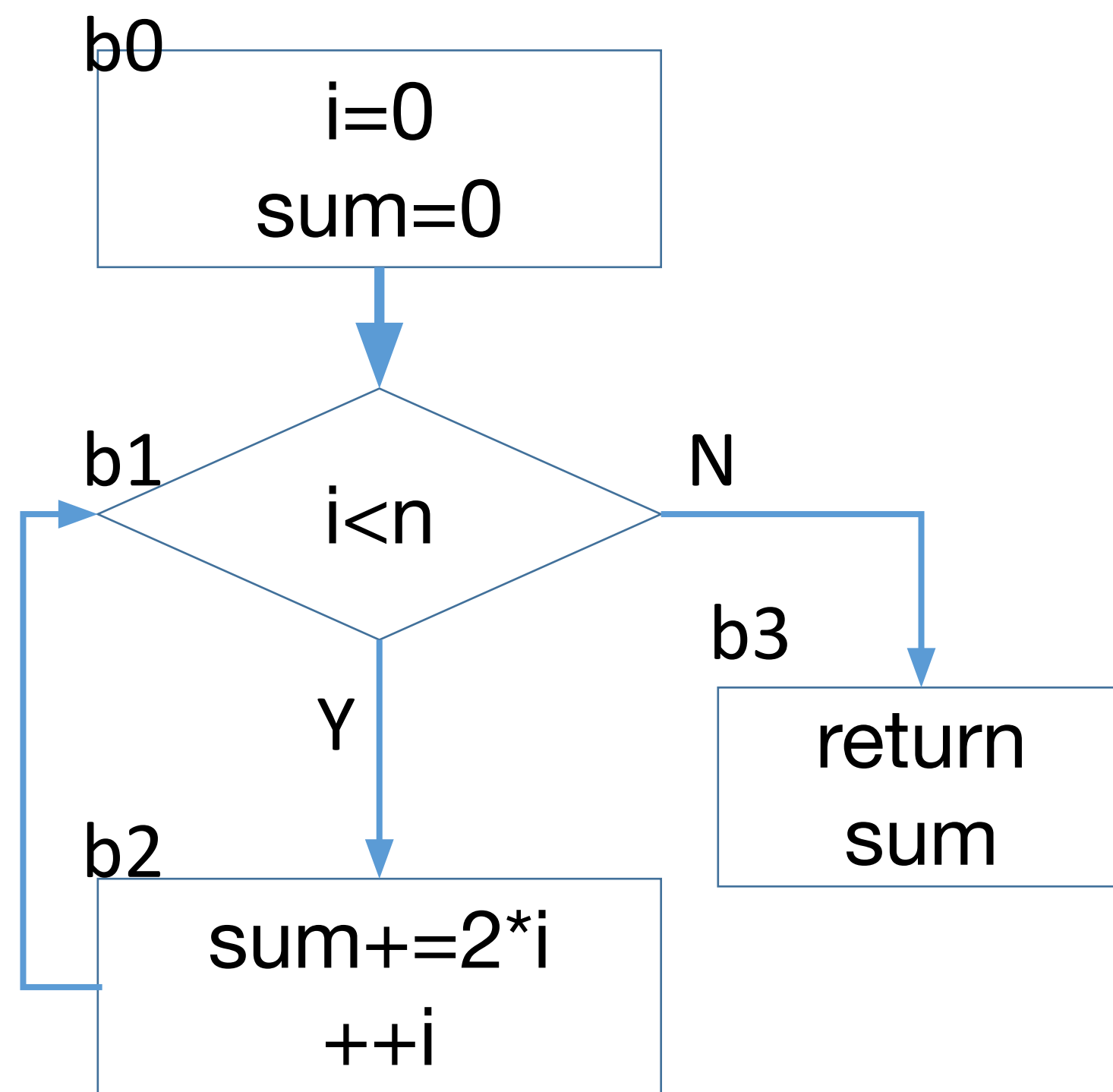
Program 1:  
Computes:  $\Sigma$   
 $(2*i)$   
For  $i \in [0, n)$



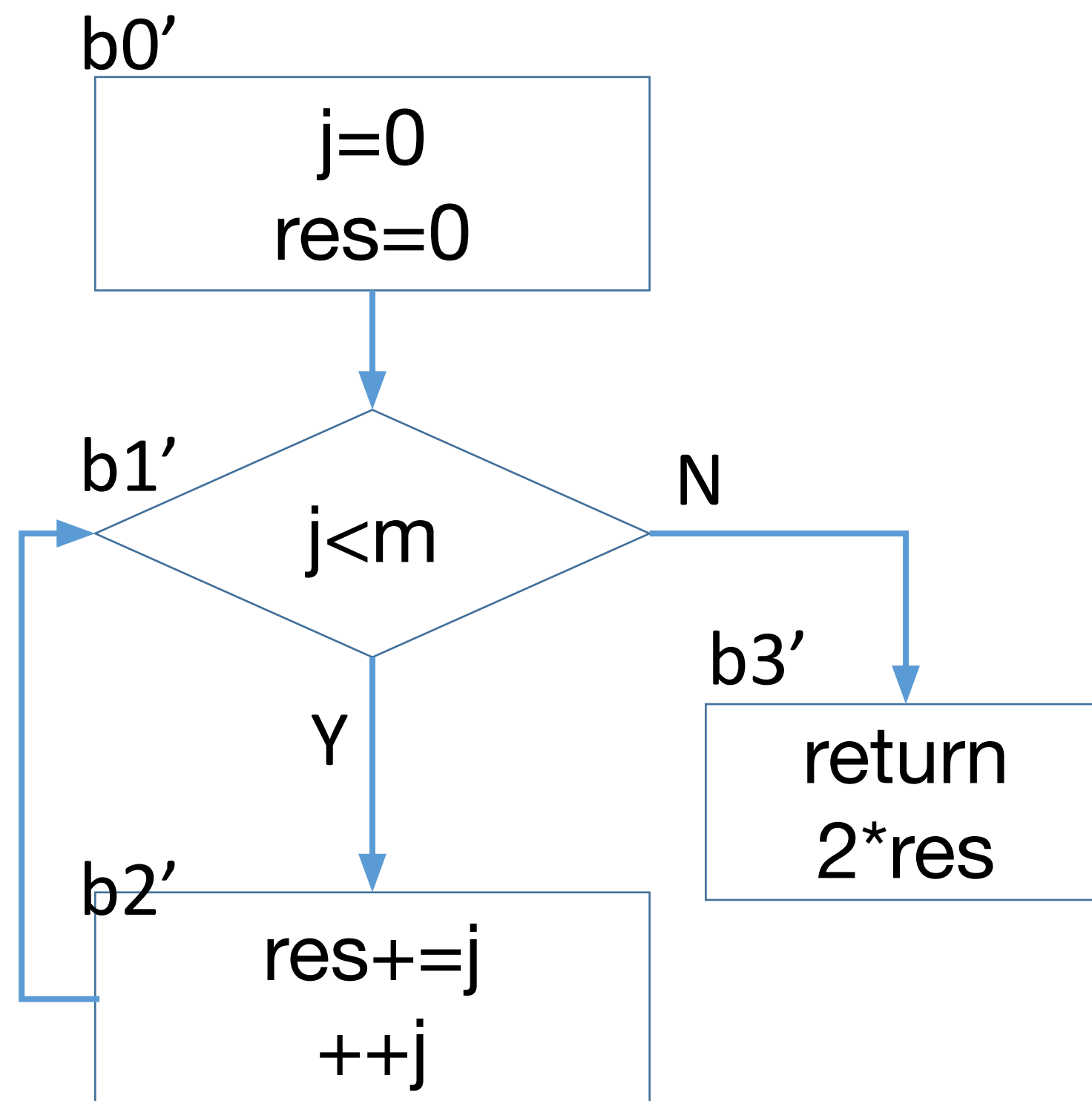
Program 2:  
Computes:  
 $2 * \Sigma j$   
For  $j \in [0, m)$



# EXAMPLE 1



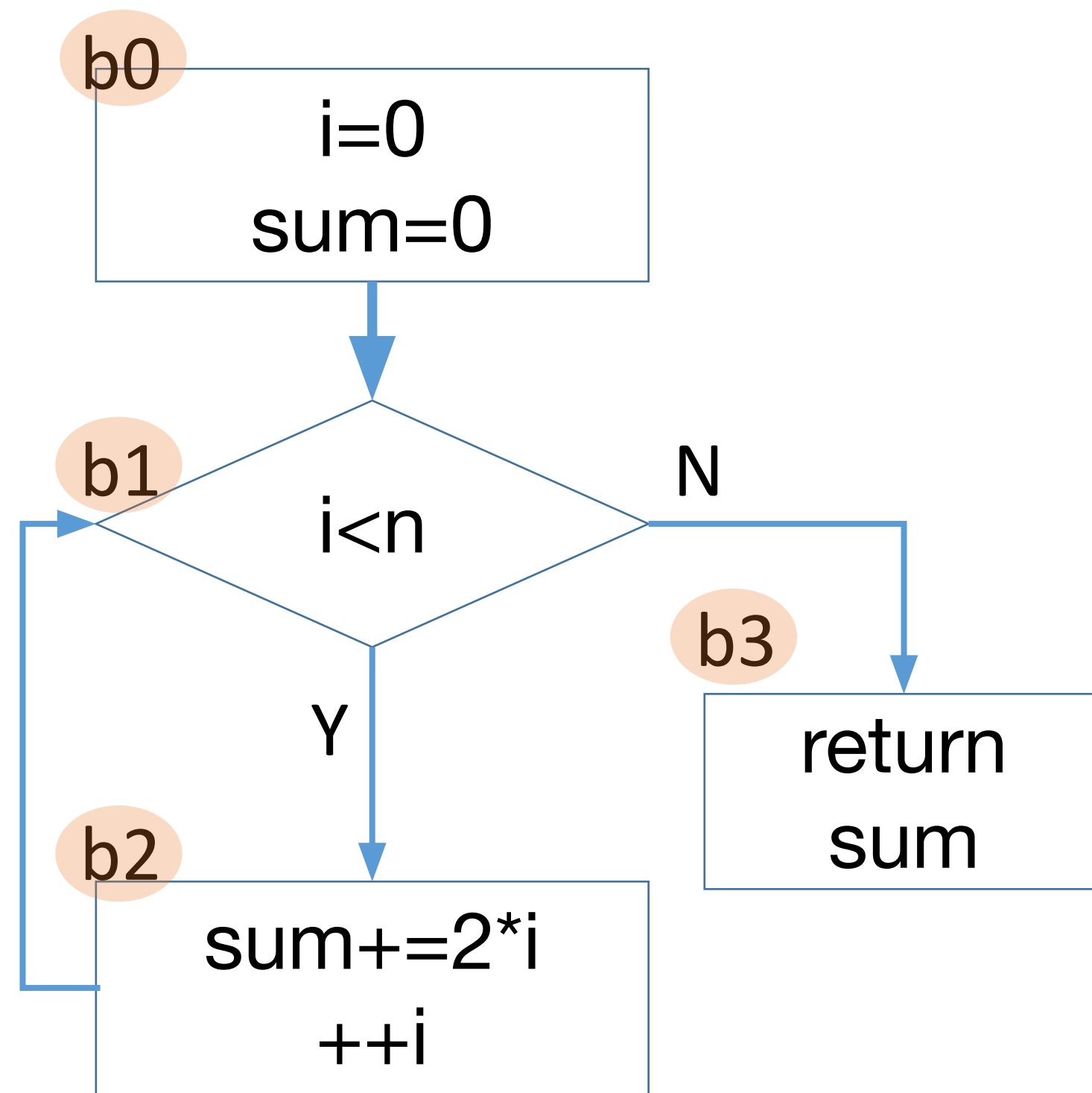
Program 1:  
Computes:  $\Sigma$   
 **$(2*i)$**   
For  $i \in [0, n)$



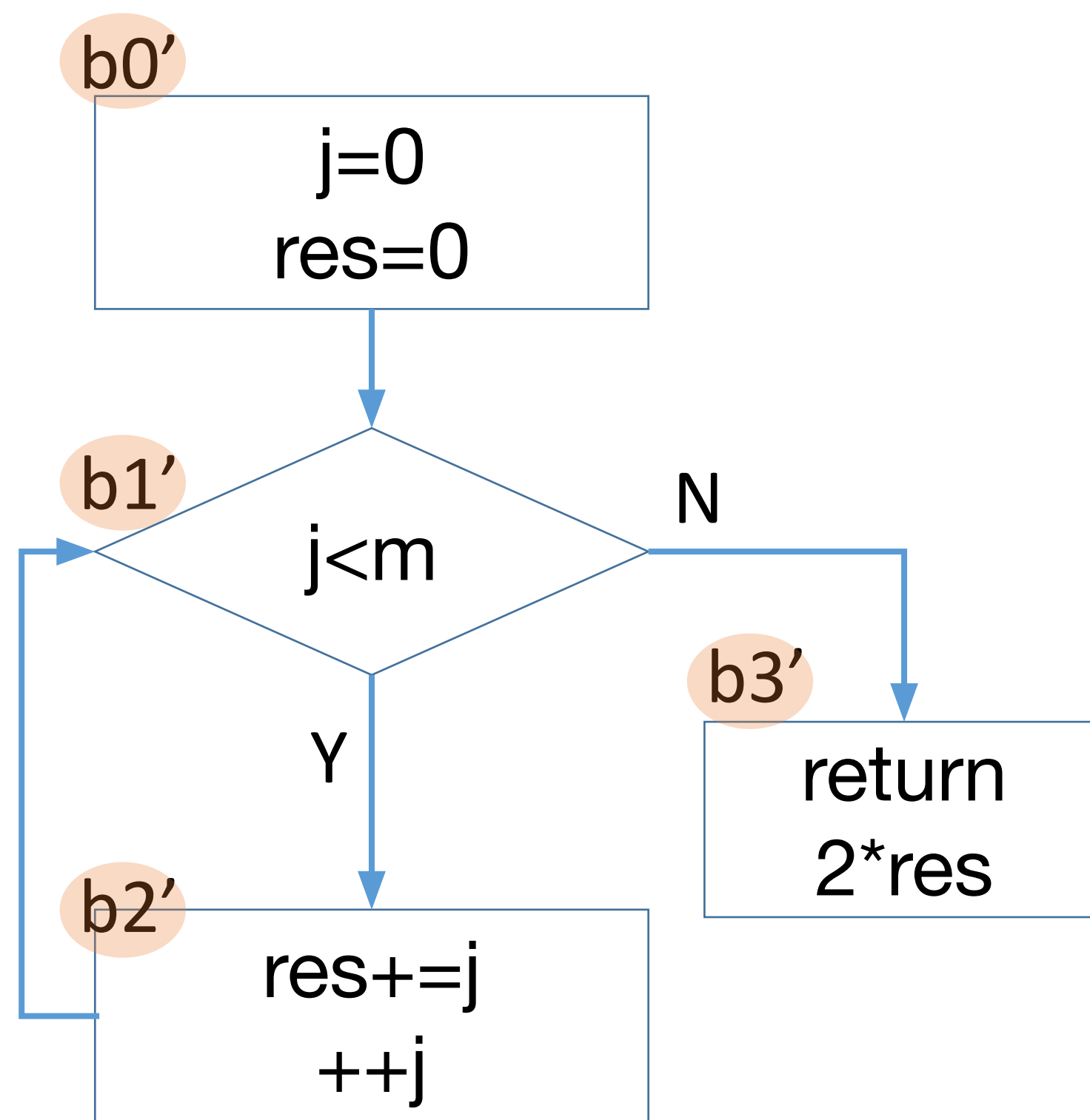
Program 2:  
Computes:  
 **$2 * \Sigma j$**   
For  $j \in [0, m)$

Correlation nodes	Invariants
$(b0, b0')$	$n = m$
$(b1, b1')$	$i = j,$ $n = m,$ $sum = 2*res$
$(b3, b3')$	$sum = 2*res$

# EXAMPLE 1



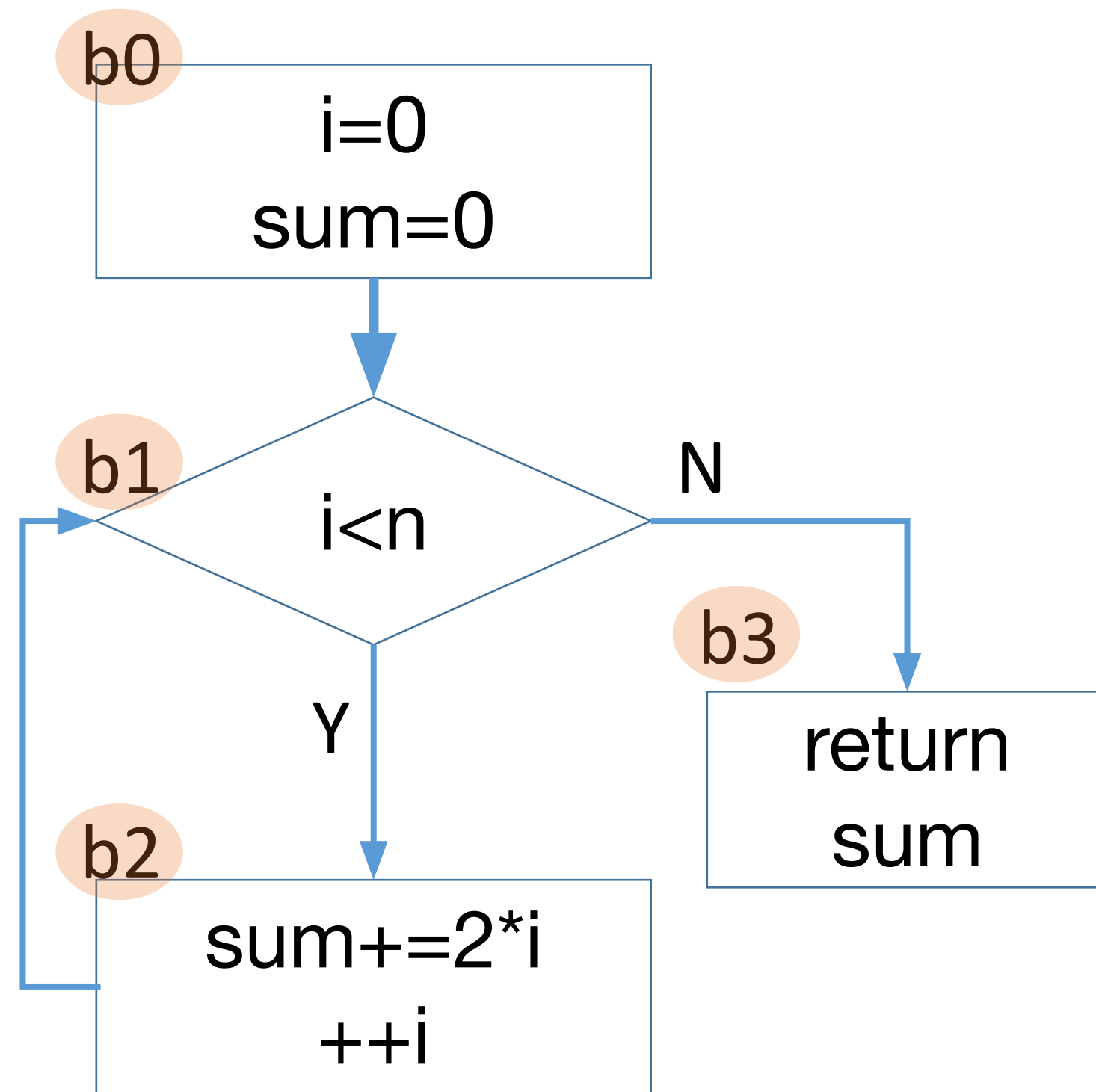
Program 1:  
Computes:  $\Sigma$   
 $(2*i)$   
For  $i \in [0, n)$



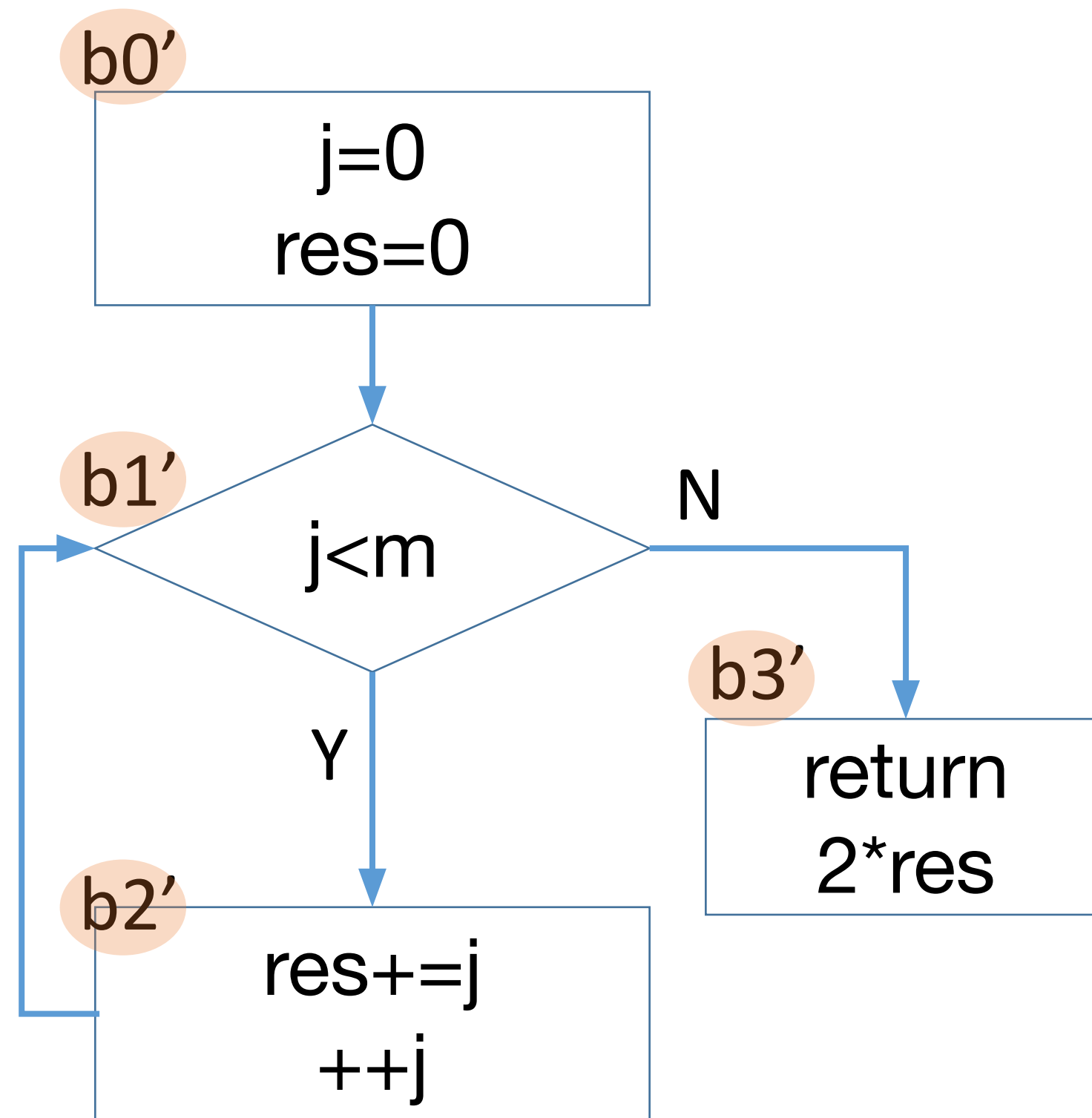
Program 2:  
Computes:  
 $2 * \Sigma j$   
For  $j \in [0, m)$

Correlation nodes	Invariants
(b0, b0')	$n = m$
(b1, b1')	$i = j,$ $n = m,$ $sum = 2*res$
(b3, b3')	$sum = 2*res$

# EXAMPLE 1



Program 1:  
Computes:  $\Sigma$   
 $(2*i)$   
For  $i \in [0, n)$

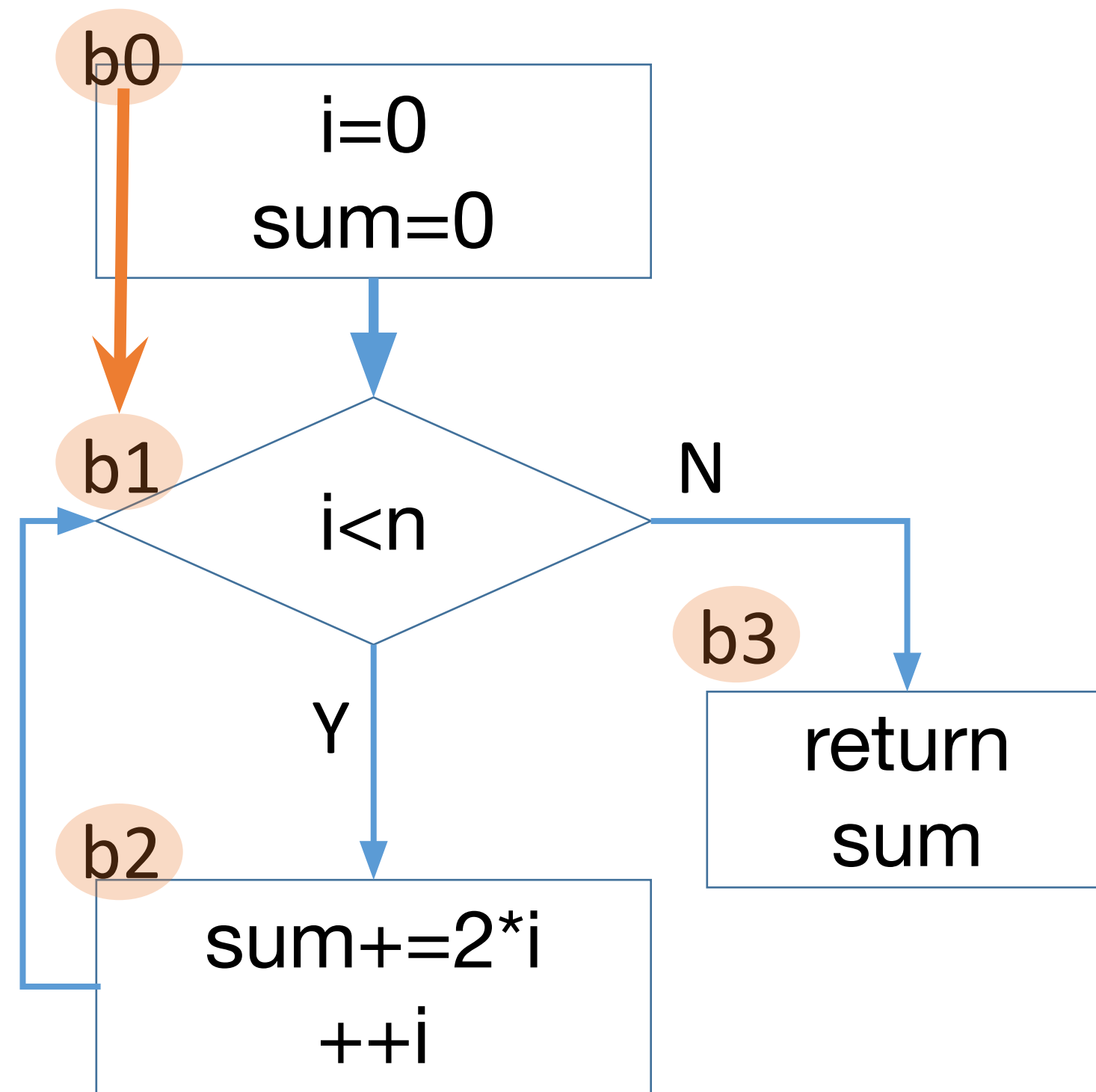


Program 2:  
Computes:  
 $2 * \Sigma j$   
For  $j \in [0, m)$

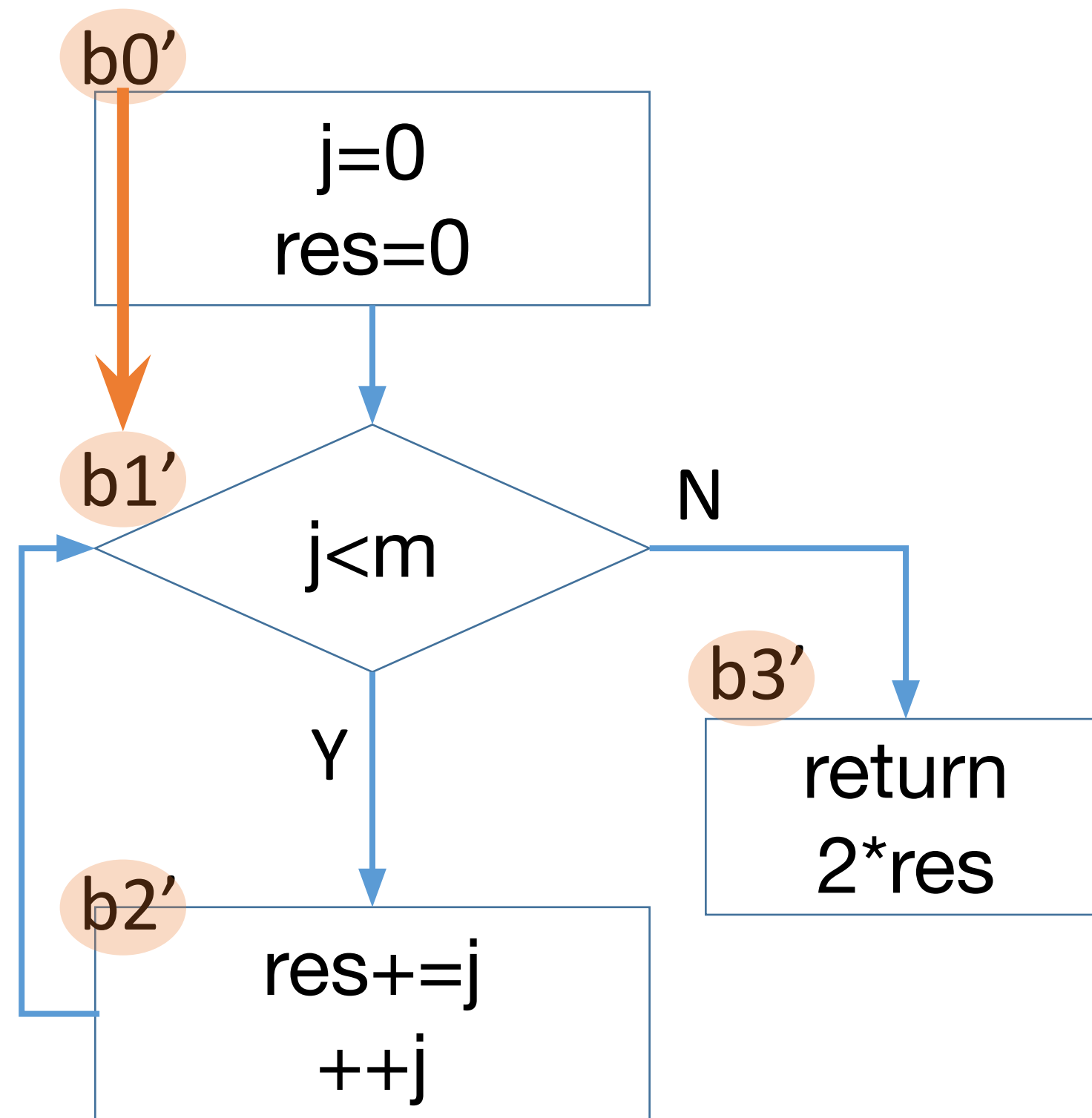
Assumption:  
Input equivalence:  
 $n = m$

Correlation nodes	Invariants
(b0, b0')	$n = m$
(b1, b1')	$i = j,$ $n = m,$ $sum = 2*res$
(b3, b3')	$sum = 2*res$

# EXAMPLE 1



Program 1:  
Computes:  $\Sigma$   
 **$(2*i)$**   
For  $i \in [0, n)$

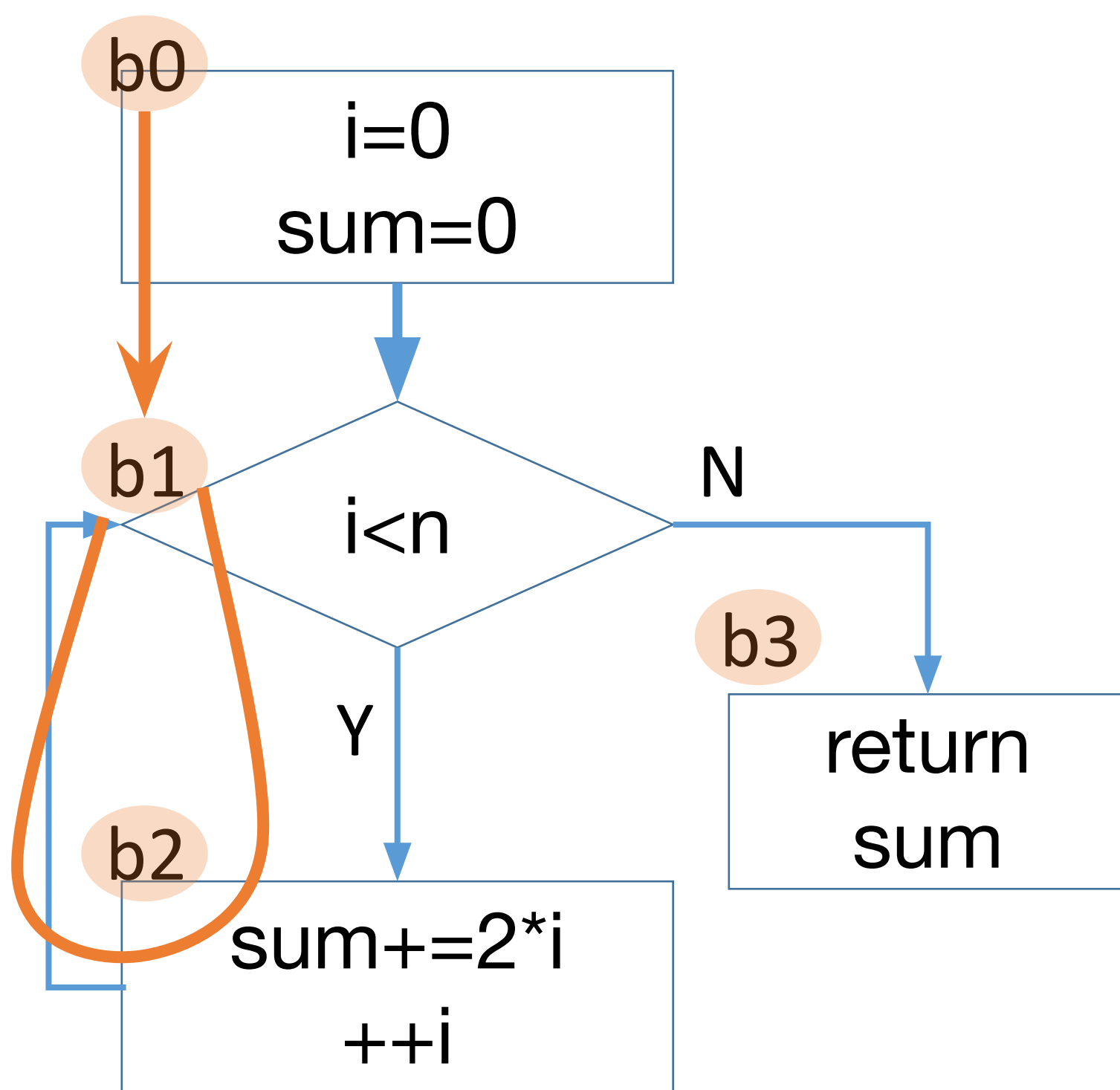


Program 2:  
Computes:  
 **$2 * \Sigma j$**   
For  $j \in [0, m)$

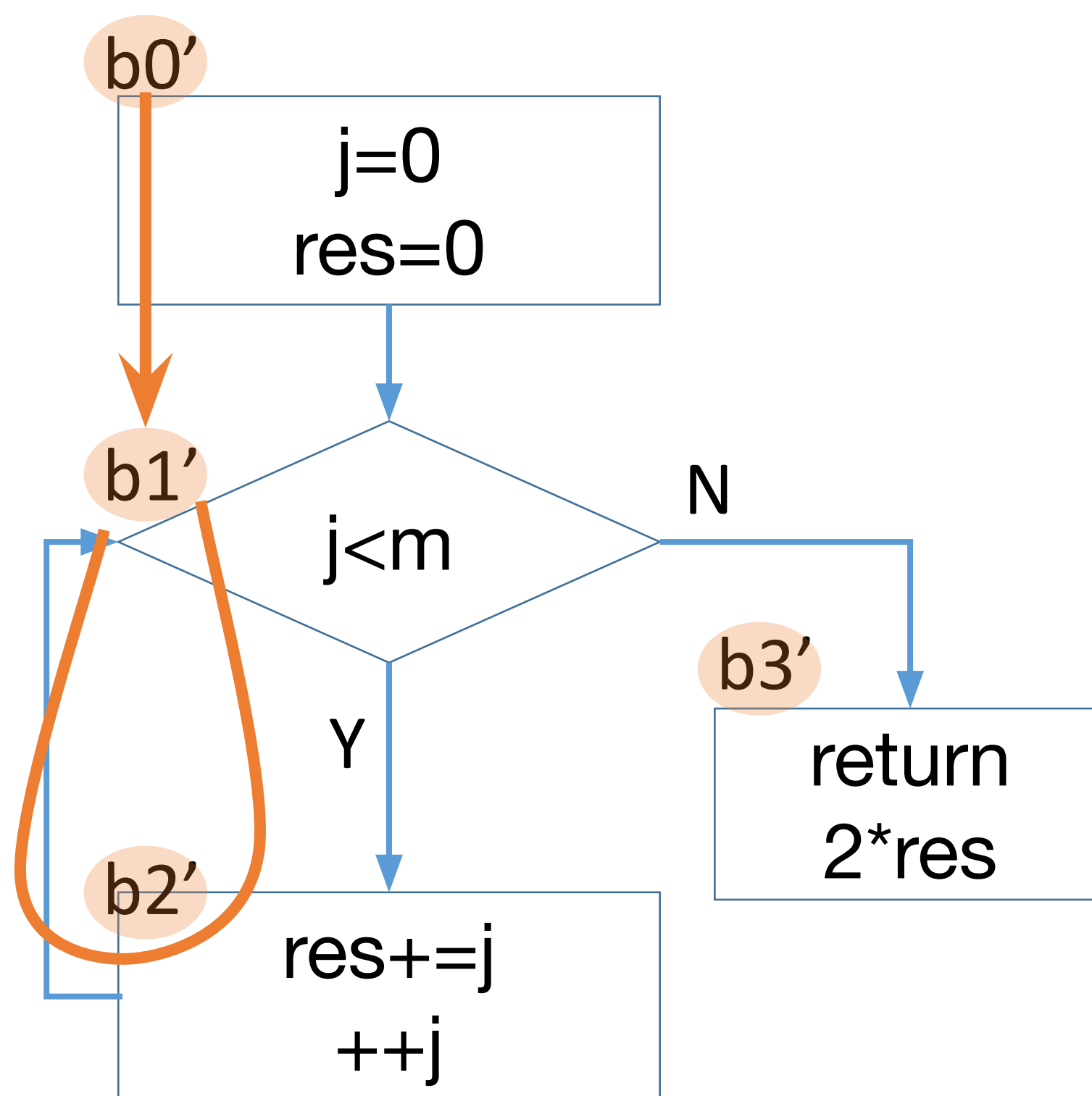
Assumption:  
Input equivalence:  
 $n = m$

Correlation nodes	Invariants
$(b0, b0')$	$n = m$
$(b1, b1')$	$i = j,$ $n = m,$ $sum = 2*res$
$(b3, b3')$	$sum = 2*res$

# EXAMPLE 1



Program 1:  
Computes:  $\Sigma$   
**(2\*i)**  
For  $i \in [0, n)$



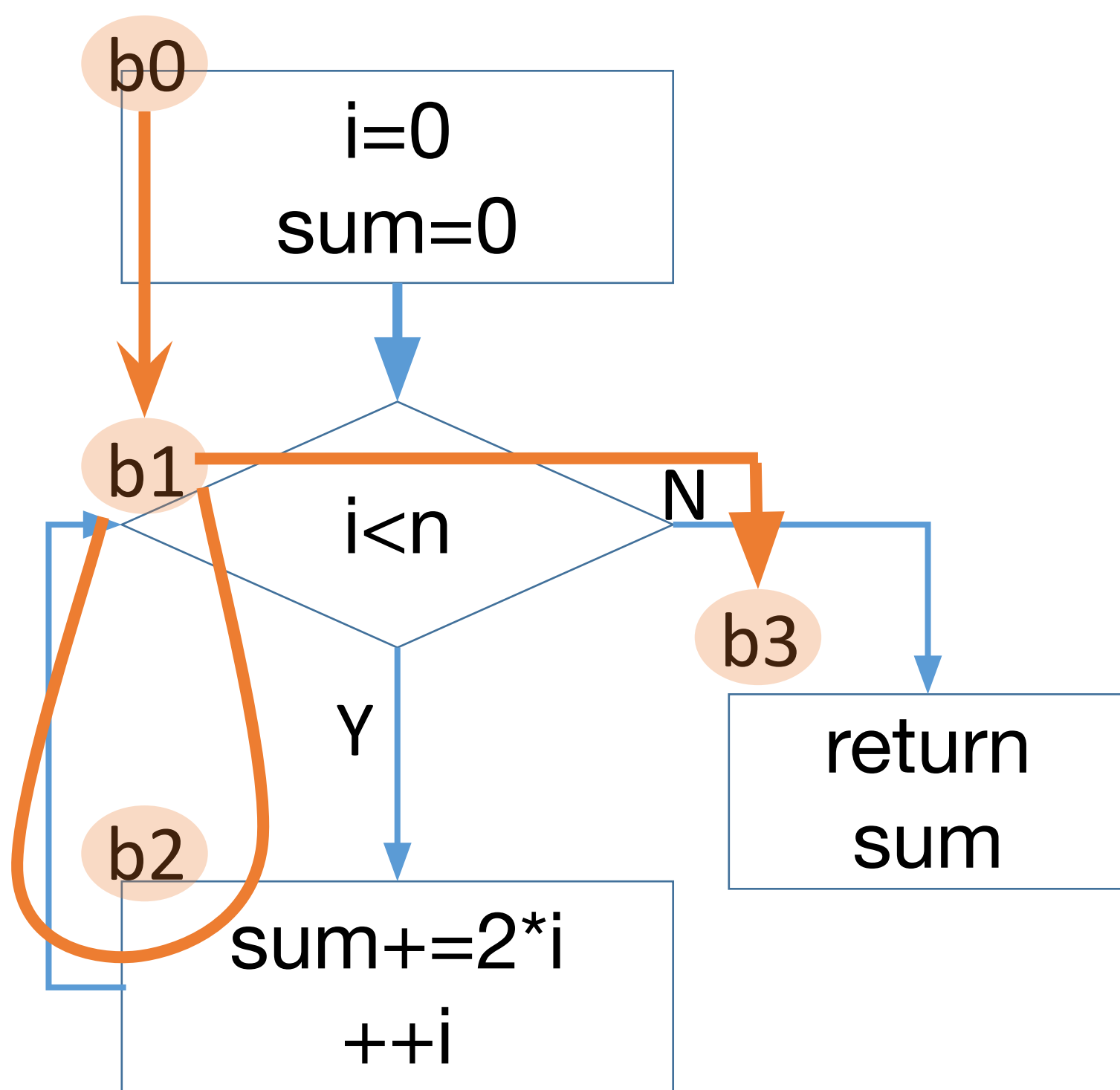
Program 2:  
Computes:  
**2 \*  $\Sigma$ j**  
For  $j \in [0, m)$

Assumption:  
Input equivalence:  
 $n = m$

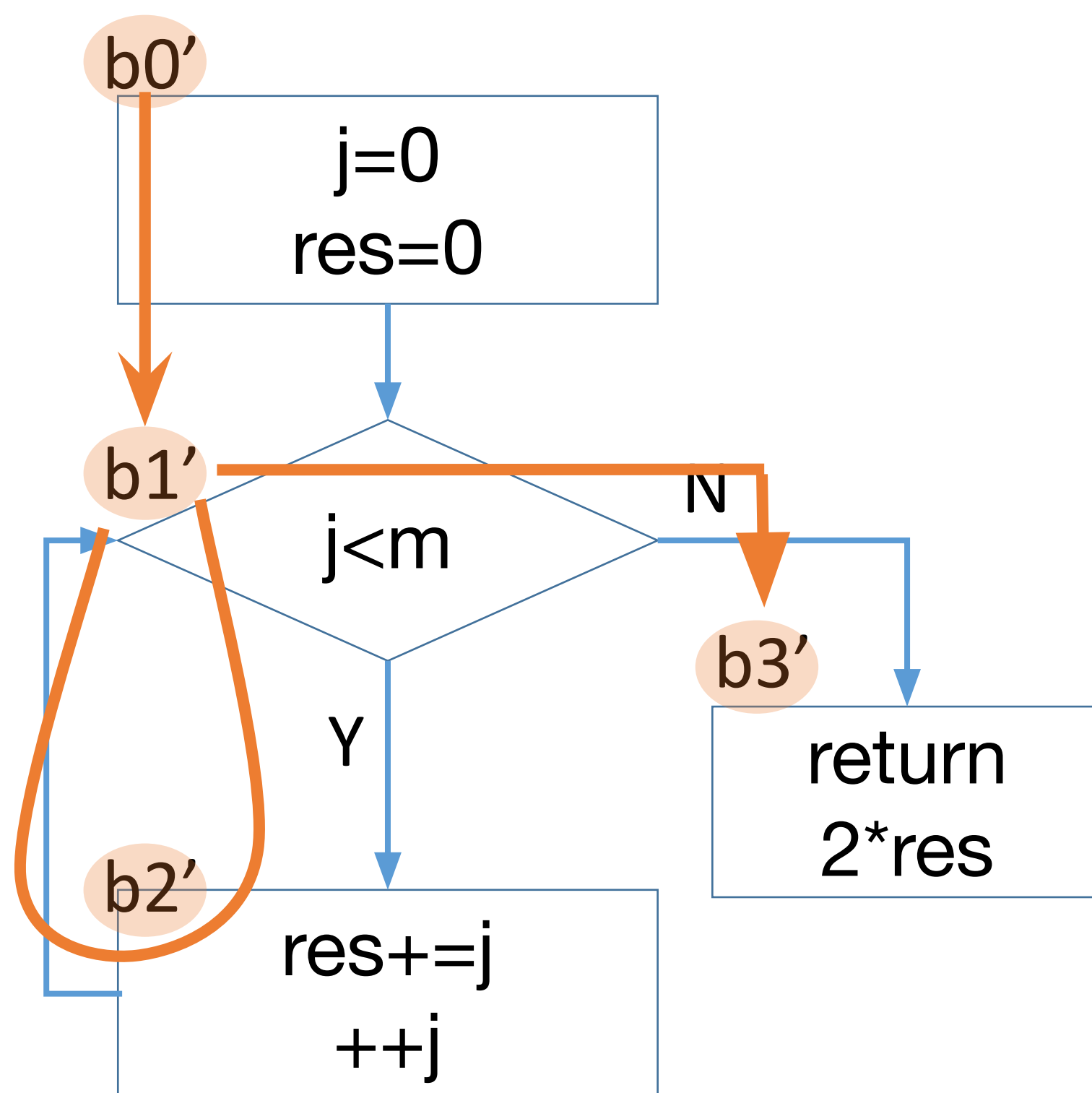
Correlation nodes	Invariants
(b0, b0')	$n = m$
(b1, b1')	$i = j,$ $n = m,$ $sum = 2 * res$
(b3, b3')	$sum = 2 * res$



# EXAMPLE 1



Program 1:  
Computes:  $\Sigma$   
 **$(2*i)$**   
For  $i \in [0, n)$



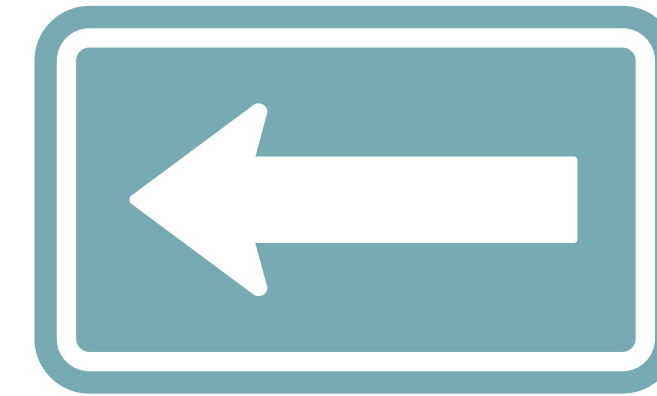
Program 2:  
Computes:  
 **$2 * \Sigma j$**   
For  $j \in [0, m)$

Assumption:  
Input equivalence:  
 $n = m$

Correlation nodes	Invariants
(b0, b0')	$n = m$
(b1, b1')	$i = j,$ $n = m,$ $sum = 2*res$
(b3, b3')	$sum = 2*res$

# STEPPING BACK...

An Equivalence Checker is a proof finder



This talk

An Inequivalence Checker is a bug finder

---

1. Try to Find an Equivalence Proof

2. Try to Find a Distinguishing Input

3. Neither found, give up :-)

# EQUIVALENCE CHECKING LITERATURE

Theoretical basis

## Simulation Relation, cut points

A. Turing. Checking a large routine. In *The early British computer conferences*, pages 70–72. MIT Press, Cambridge, MA, USA, 1989 (reproduction)  
Milner, R., "Program Simulation: An Extended Formal Notion", Memo 17, Computers and Logic Research Group, University College of Swansea, U.K. (1961).  
Milner, R., "A Formal Notion of Simulation Between Programs", Memo 14, Computers and Logic Research Group, University College of Swansea, U.K. (1970).  
Milner, R., "An algebraic definition of simulation between programs", IJCAI'71 Proceedings of the 2nd international joint conference on Artificial intelligence (1971)  
Manna, Z., "The Correctness of Programs", *J. of Computer and Systems Sciences*, Vol. 3, No. 2. 119-127 (1969).  
...

D. W. Currie, A. J. Hu, and S. P. Rajan. Automatic formal verification of DSP software. In *DAC*, pages 130–135, 2000.  
X. Feng and A. J. Hu. Automatic formal verification for scheduled VLIW code. In *LCTES-SCOPES*, pages 85–92, 2002.  
X. Feng and A. J. Hu. Cutpoints for formal equivalence verification of embedded software. In *EMSOFT*, pages 307–316, 2005.  
T. Matsumoto, H. Saito, and M. Fujita. Equivalence checking of C programs by locally performing symbolic simulation on dependence graphs. In *ISQED*, pages 370–375, 2006.  
T. Arons, E. Elster, L. Fix, S. Mador-Haim, M. Mishaeli, J. Shalev, E. Singerman, A. Tiemeyer, M. Y. Vardi, and L. D. Zuck. Formal verification of backward compatibility of microcode. In *CAV*, pages 185–198, 2005.  
Lopes, N.P., Menendez, D., Nagarakatte, S., Regehr, J.: Provably correct peephole optimizations with alive. In: *Proceedings of the 36th ACM SIGPLAN Conference on Programming Language Design and Implementation*. pp. 22–32. *PLDI 2015*, ACM (2015)  
...

## Loop free code

## Partial equivalence (with bounded unrolling)

D.Jackson and D.A.Ladd. SemanticDiff: A tool for summarizing the effects of modifications. In *ICSM*, pages 243–252, 1994.  
Lahiri, S., Hawblitzel, C., Kawaguchi, M., Rebelo, H.: Symdiff: A language-agnostic semantic diff tool for imperative programs. In: *CAV '12*. Springer (2012)  
Lahiri, S., Sinha, R., Hawblitzel, C.: Automatic rootcausing for program equivalence failures in binaries. In: *Computer Aided Verification (CAV'15)*. Springer (2015)  
S. Person, M. B. Dwyer, S. G. Elbaum, and C. S. Pasareanu. Differential symbolic execution. In *SIGSOFT FSE*, pages 226–237, 2008  
D. A. Ramos and D. R. Engler. Practical, low-effort equivalence verification of real code. In *CAV*, pages 669–685, 2011.  
Lopes, N.P., Monteiro, J.: Automatic equivalence checking of programs with uninterpreted functions and integer arithmetic. *Int. J. Softw. Tools Technol. Transf.* 18(4), 359–374 (Aug 2016)  
....

## Regression verification

Hawblitzel, C., Lahiri, S.K., Pawar, K., Hashmi, H., Gokbulut, S., Fernando, L., Detlefs, D., Wadsworth, S.: Will you still compile me tomorrow? static cross-version compiler validation. In: *ESEC/FSE 2013*, ACM (2013)  
Strichman, O., Godlin, B.: Regression verification - a practical way to verify programs. In: *Verified Software: Theories, Tools, Experiments*, vol. 4171, pp. 496–501. Springer Berlin Heidelberg (2008)  
Felsing, D., Grebing, S., Klebanov, V., Rümmer, P., Ulbrich, M.: Automating regression verification. In: *ASE '14*, ACM (2014)

## Affine programs

Verdoolaege, S., Janssens, G., and Bruynooghe, M. 2009. Equivalence checking of static affine programs using widening to handle recurrences. In *Computer Aided Verification 21*. Springer, 599–613.  
Verdoolaege, S., Janssens, G., and Bruynooghe, Equivalence Checking of Static Affine Programs using Widening to Handle Recurrences (TOPLAS12)

## Data Driven (test cases are given)

Churchill, B., Sharma, R., Bastien, J., Aiken, A.: Sound loop superoptimization for google native client. In: *Proceedings of the Twenty-Second International Conference on Architectural Support for Programming Languages and Operating Systems*. pp. 313–326. *ASPLOS '17*, ACM (2017)  
Sharma, R., Schkufza, E., Churchill, B., Aiken, A.: Data-driven equivalence checking. In: *Proceedings of the 2013 ACM SIGPLAN International Conference on Object Oriented Programming Systems Languages and Applications*. pp. 391–406. *OOPSLA '13*, ACM (2013)  
...

## Translation validation (Pass based, knowledge of transformations)

V.Menon, K.Pingali, and N. Mateev. Fractal symbolic analysis. *ACM Trans. Program. Lang. Syst.*, 25(6):776–813, 2003.  
Kundu, S., Tatlock, Z., Lerner, S.: Proving optimizations correct using parameterized program equivalence. In: *PLDI '09*, ACM (2009)  
Tate, R., Stepp, M., Tatlock, Z., Lerner, S.: Equality saturation: a new approach to optimization. In: *POPL '09*  
Stepp, M., Tate, R., Lerner, S.: Equality-based translation validator for llvm. In: *Proceedings of the 23rd International Conference on Computer Aided Verification*. pp. 737–742. *CAV'11*, Springer-Verlag (2011)  
B. Goldberg, L. D. Zuck, and C. W. Barrett. Into the loops: Practical issues in translation validation for optimizing compilers. *Electr.NotesTheor.Comput.Sci.*,132(1):53–71,2005.  
G. C. Necula. Translation validation for an optimizing compiler. In *PLDI*, pages 83–94, 2000.  
A. Pnueli, M. Siegel, and E. Singerman. Translation validation. In *TACAS*, pages 151–166, 1998.  
Kanade, A., Sanyal, A., Khedker, U.P.: Validation of gcc optimizers through trace generation. *Softw. Pract. Exper.* 39(6), 611–639 (Apr 2009)  
Pnueli, A., Siegel, M., Singerman, E.: Translation validation. In: *Proceedings of the 4th International Conference on Tools and Algorithms for Construction and Analysis of Systems*. pp. 151–166. *TACAS '98*, Springer-Verlag (1998)  
Tristan, J.B., Govereau, P., Morrisett, G.: Evaluating value-graph translation validation for llvm. In: *Proceedings of the 32nd ACM SIGPLAN Conference on Programming Language Design and Implementation*. pp. 295–305. *PLDI '11*, ACM (2011)  
Zaks, A., Pnueli, A.: Covac: Compiler validation by program analysis of the crossproduct. In: *Proceedings of the 15th International Symposium on Formal Methods*. pp. 35–51. *FM '08*, Springer-Verlag (2008)  
...

Application specific/limitations

# STILL MISSING...

An **Automatic** Equivalence Checker

that works across a **long and unknown** sequence of transformations

for **practically useful** programs written in **commonly-used syntaxes**

in a **scalable** way

# EQUIVALENCE CHECKING RESEARCH ROADMAP

Prior  
Work

Translation Validation  
across a selected set  
of transformations



# EQUIVALENCE CHECKING RESEARCH ROADMAP

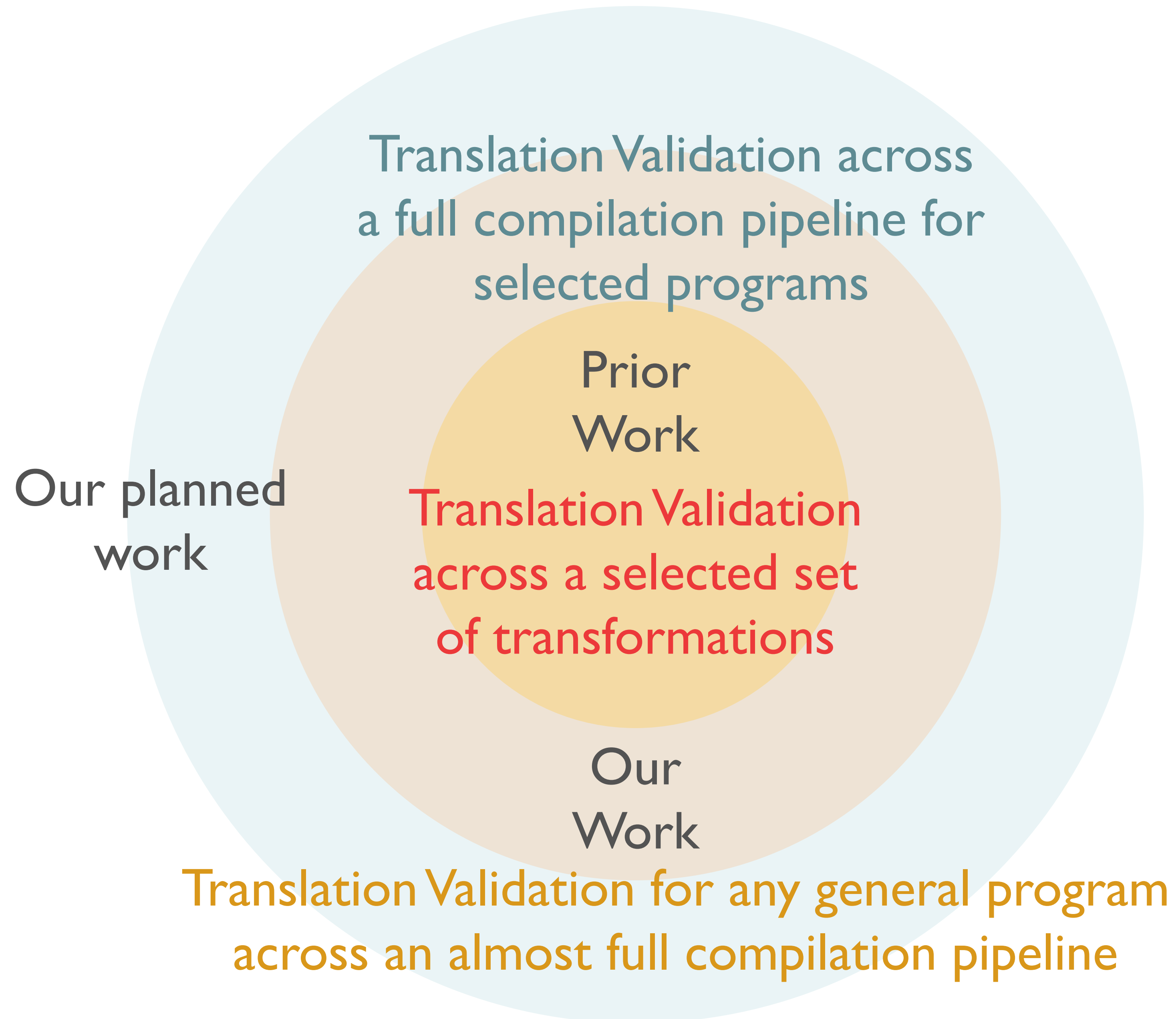
Translation Validation across  
a full compilation pipeline for  
selected programs

Prior  
Work

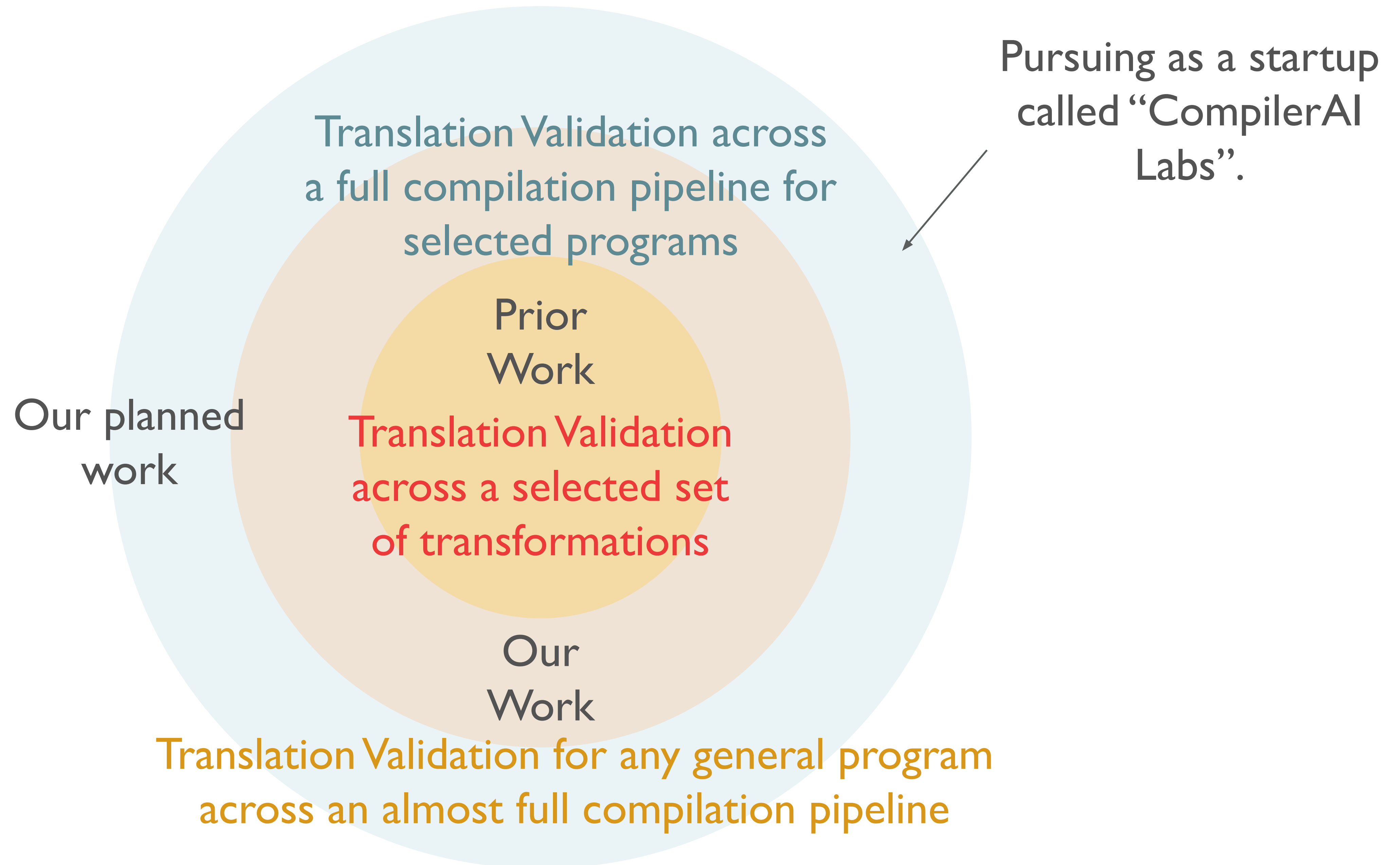
Translation Validation  
across a selected set  
of transformations

Our  
Work

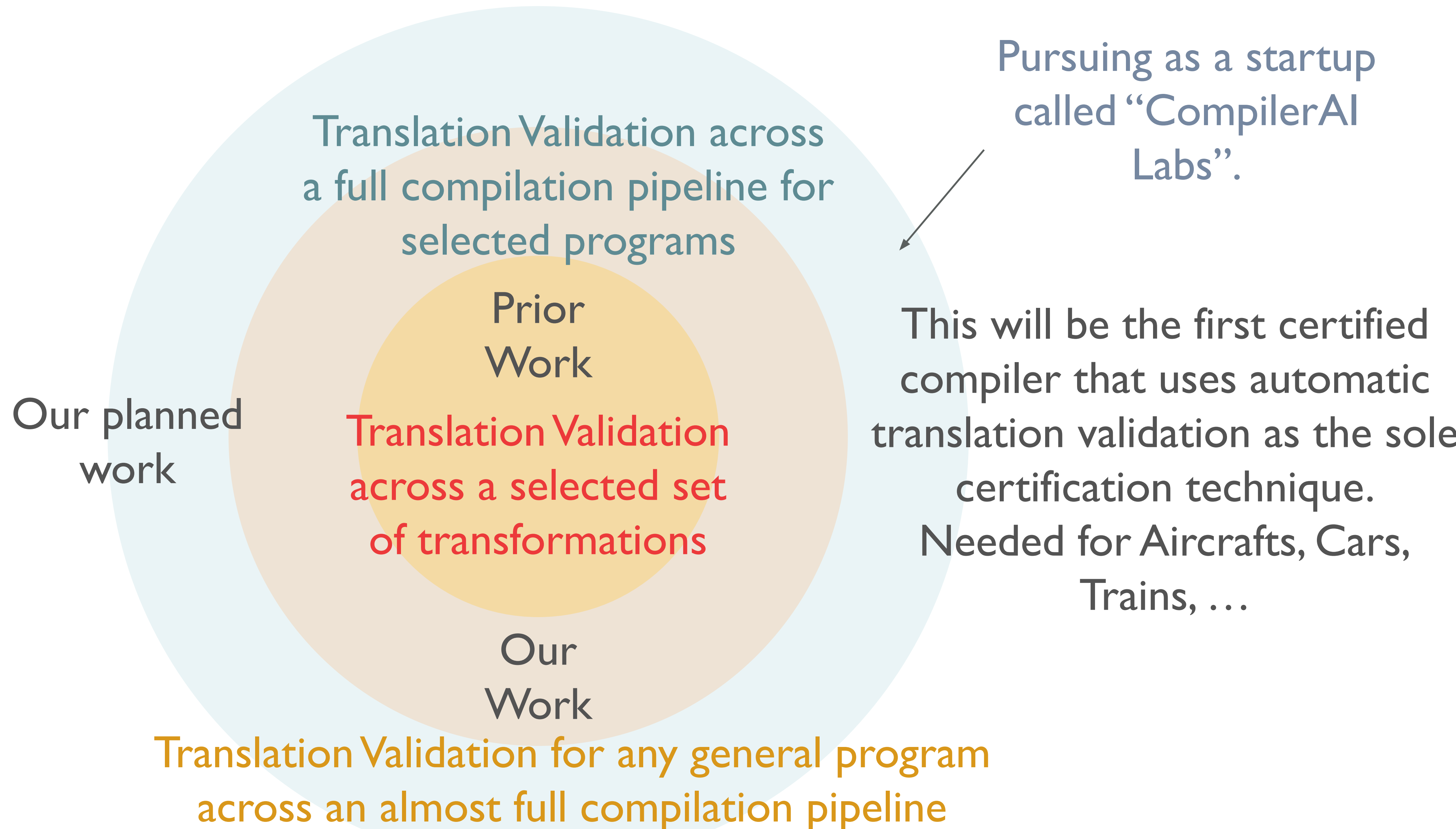
# EQUIVALENCE CHECKING RESEARCH ROADMAP



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# EQUIVALENCE CHECKING RESEARCH ROADMAP



# Key Ideas

- **Scalable Search Algorithm for a Bisimulation Relation**
  - Includes Modeling of Undefined Behaviour Semantics
  - Leverages SMT Solvers, e.g., Z3, Yices, CVC4 for discharge of first-order-logic proof obligations

[M. Dahiya et. al.. Blackbox Equivalence Checking Across Compiler Optimizations, , APLAS 2017]

[M. Dahiya et. al., Modeling Undefined Behaviour for Checking Equivalence Across Compiler Optimizations, HVC 2017]



# Key Ideas

- **Automatic Identification of bisimulation proofs**
  - Would require millions of years through a naive search
  - Translation Validator from C-to-x86

[S. Gupta et. al., Effective Use of SMT Solvers for Program Equivalence Checking through Invariant Sketching and Query Decomposition, SAT 2018]

[S. Gupta et. al., Counterexample-Guided Correlation Algorithm for Translation Validation, OOPSLA 2020]

# EXAMPLE 3: VECTORIZATION

```
int LEN, a[LEN], b[LEN];
int c[LEN], d[LEN];
C0: void s441() {
C1:     for (int i = 0; i < LEN; i++) {
C2:         if (d[i] < 0) {
C3:             a[i] += b[i] * c[i];
C4:         } else if (d[i] == 0) {
C5:             a[i] += b[i] * b[i];
C6:         } else {
C7:             a[i] += c[i] * c[i];
C8:         }
C9:     }
C10: }
```

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int c[LEN], d[LEN];
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C6:     } else {
C7:       a[i] += c[i] * c[i];
C8:     }
C9:   }
C10: }
```

```
A0: s441:
A1:   r1 = 0
A2:   xmm1 = a[r1 .. r1+3]
A3:   xmm2 = xmm1 + b[r1 .. r1+3]*c[r1 .. r1+3]
A4:   xmm3 = xmm1 + b[r1 .. r1+3]*b[r1 .. r1+3]
A5:   xmm4 = xmm1 + c[r1 .. r1+3]*c[r1 .. r1+3]
      // pcmptgd
A6:   xmm0 = (d[r1] < 0), .. , (d[r1+3] < 0)
A7:   xmm1 = xmm0 ? xmm2 : xmm1 // pblendvb
      // pcmpeqd
A8:   xmm0 = (d[r1] == 0), .. , (d[r1+3] == 0)
A9:   xmm1 = xmm0 ? xmm3 : xmm1 // pblendvb
      // pcmptgd
A10:  xmm0 = (d[r1] > 0), .. , (d[r1+3] > 0)
A11:  xmm1 = xmm0 ? xmm4 : xmm1 // pblendvb
A12:  a[r1 .. r1+3] = xmm1
A13:  r1 += 4
A14:  if (r1 != LEN) goto A2
A15:  ret
```

Key Idea

Counterexample Guided Best-First Search



# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
#define LEN 1000
int original() {
    int sum = 0;
    int mid = LEN / 2;
    for ( int i = 0; i < LEN ; i ++ ) {
        if ( i < mid ) sum += c[a[i]];
        if ( i >= mid ) sum += b[i];
    }
    return sum ;
}
```

```
int loopSplitting() {
```

```
    int sum = 0;
```

```
    int mid = LEN / 2;
```

```
    for ( int i = 0; i < mid ; i ++ ) {
```

```
        if ( i < mid ) sum += c[a[i]];
        if ( i >= mid ) sum += b[i];
```

```
    }
```

```
    }
```

```
    for ( int i = mid; i < LEN ; i ++ ) {
```

```
        if ( i < mid ) sum += c[a[i]];
        if ( i >= mid ) sum += b[i];
```

```
    }
```

```
    }
```

```
    return sum ;
```

```
}
```



# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
int loopSplitting() {
```

```
    int sum = 0;
```

```
    int mid = LEN / 2;
```

```
    for ( int i = 0; i < mid ; i ++ ) {  
        if ( i < mid ) sum += c[a[i]];  
        if ( i >= mid ) sum += b[i];  
    }
```

```
    for ( int i = mid; i < LEN ; i ++ ) {  
        if ( i < mid ) sum += c [a[i]];  
        if ( i >= mid ) sum += b[i];  
    }
```

```
    return sum ;
```

```
}
```

```
int loopUnswitching() {
```

```
    int sum = 0;
```

```
    int mid = LEN / 2;
```

```
    for ( int i = 0; i < mid ; i ++ ) {  
        sum += c[a[i]];  
    }
```

```
    for ( int i = mid; i < LEN ; i ++ ) {  
        sum += b[i];  
    }
```


```
    return sum ;
```

```
}
```

# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
int loopUnswitching() {  
    int sum = 0;  
    int mid = LEN / 2;  
    for ( int i = 0; i < mid ; i++) {  
        sum += c[a[i]];  
    }  
    for ( int i = mid; i < LEN ; i++) {  
        sum += b[i];  
    }  
    return sum ;  
}
```

```
int loopUnrolling() {  
    int sum = 0;  
    int mid = LEN / 2;  
    for ( int i = 0; i < mid ; i++) {  
        sum += c[a[i]];  
    }  
    for ( int i = mid; i < LEN ; i +=4) {  
        sum += b[ i ];  
        sum += b[ i+1 ];  
        sum += b[ i +2];  
        sum += b[ i +3];  
    }  
    return sum ;  
}
```



# EXAMPLE 5 : LOOP TRANSFORMATIONS

```
int loopUnrolling() {  
    int sum = 0;  
    int mid = LEN / 2;  
    for ( int i = 0; i < mid ; i ++ ) {  
        sum += c[a[i]];  
    }  
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        sum += b[ i ];  
        sum += b[ i+1 ];  
        sum += b[ i +2];  
        sum += b[ i +3];  
    }  
    return sum ;  
}
```

A0 : loopVectorizedAndRegAllocated :

A1 : r1 = 0; r2 = 0;

A2 : r2 += c [ a [ r1 ] ]

A3 : r1 ++

A4 : if ( r1 != mid ) goto A2

A5 : r1 = &b[mid]; r3=& b[LEN]; xmm0 = 0

A6 : xmm0 += \* r1 , .. , \*( r1 +12)

A7 : r1 += 16

A8 : if ( r1 != r3 ) goto A6

A9 : xmm0 += ( xmm0 >> 8)

A10 : xmm0 += ( xmm0 >> 4)

A11 : r2 += xmm0 [31:0]

EA : ret r2

# End-to-End Equivalence Check

```

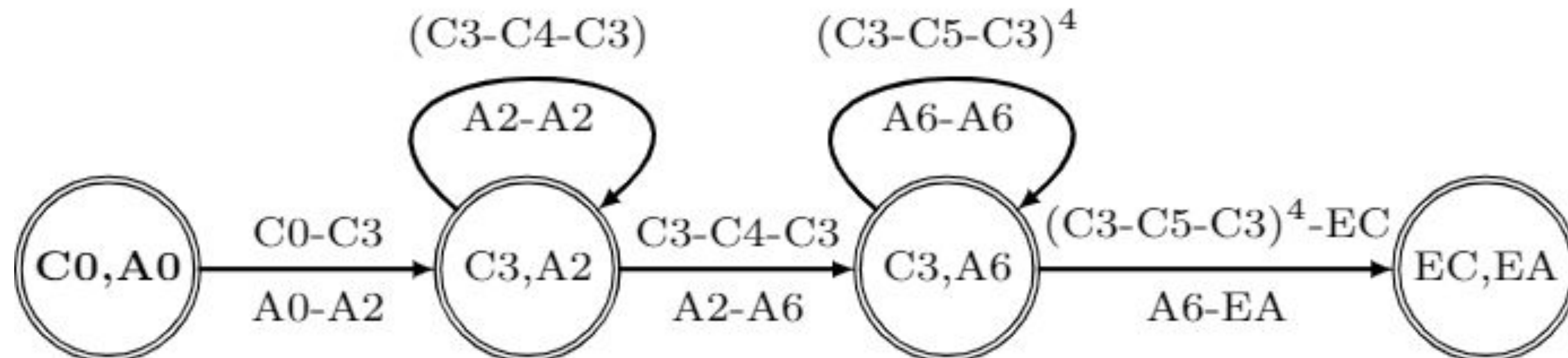
#define LEN 1000
C0: int original() {
C1:  int sum = 0;
C2:  int mid = LEN / 2;
C3:  for ( int i = 0; i < LEN ; i ++ ) {
C4:    if ( i < mid ) sum += c[a[ i ]];
C5:    if ( i >= mid ) sum += b[i];
C6:  }
EC:  return sum ;
    }

```

```

A0 : loopVectorizedAndRegAllocated :
A1 :  r1 = 0; r2 = 0;
A2 :    r2 += c [ a [ r1 ]]
A3 :    r1 ++
A4 :    if ( r1 != mid ) goto A2
A5 :  r1 = &b[mid]; r3=& b[LEN]; xmm0 = 0
A6 :    xmm0 += * r1 , .. , *( r1 +12)
A7 :    r1 += 16
A8 :    if ( r1 != r3 ) goto A6
A9 :  xmm0 += ( xmm0 >> 8)
A10 : xmm0 += ( xmm0 >> 4)
A11 : r2 += xmm0 [31:0]
EA  : ret r2

```



# Incremental Construction of the Product CFG



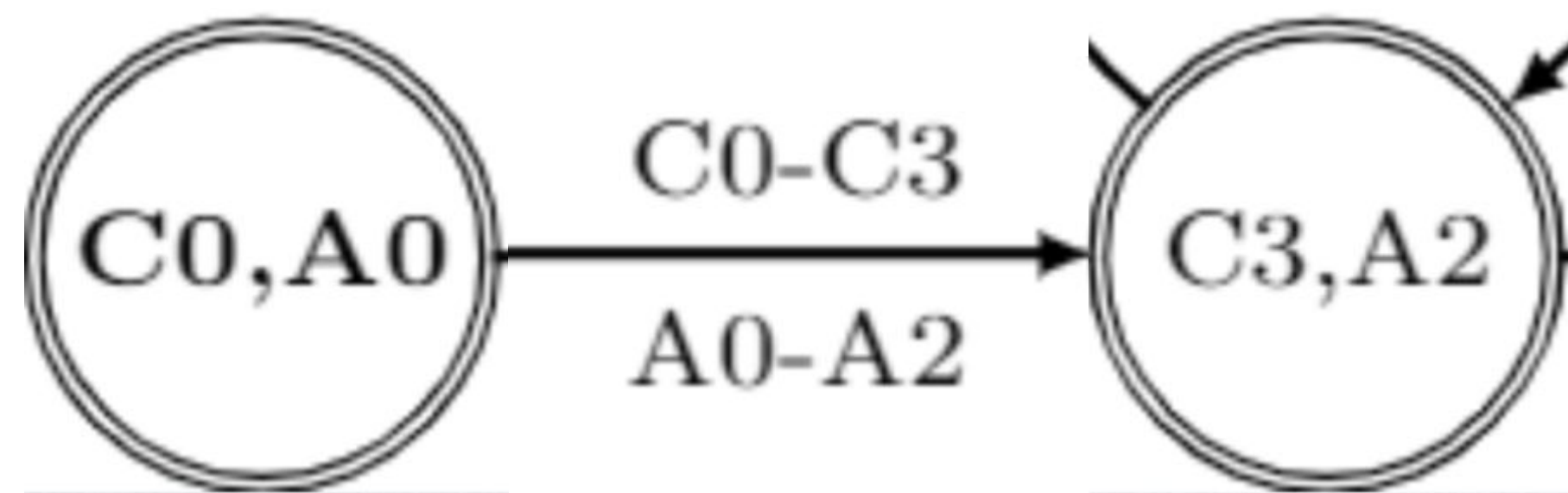


# Incremental Construction of the Product CFG



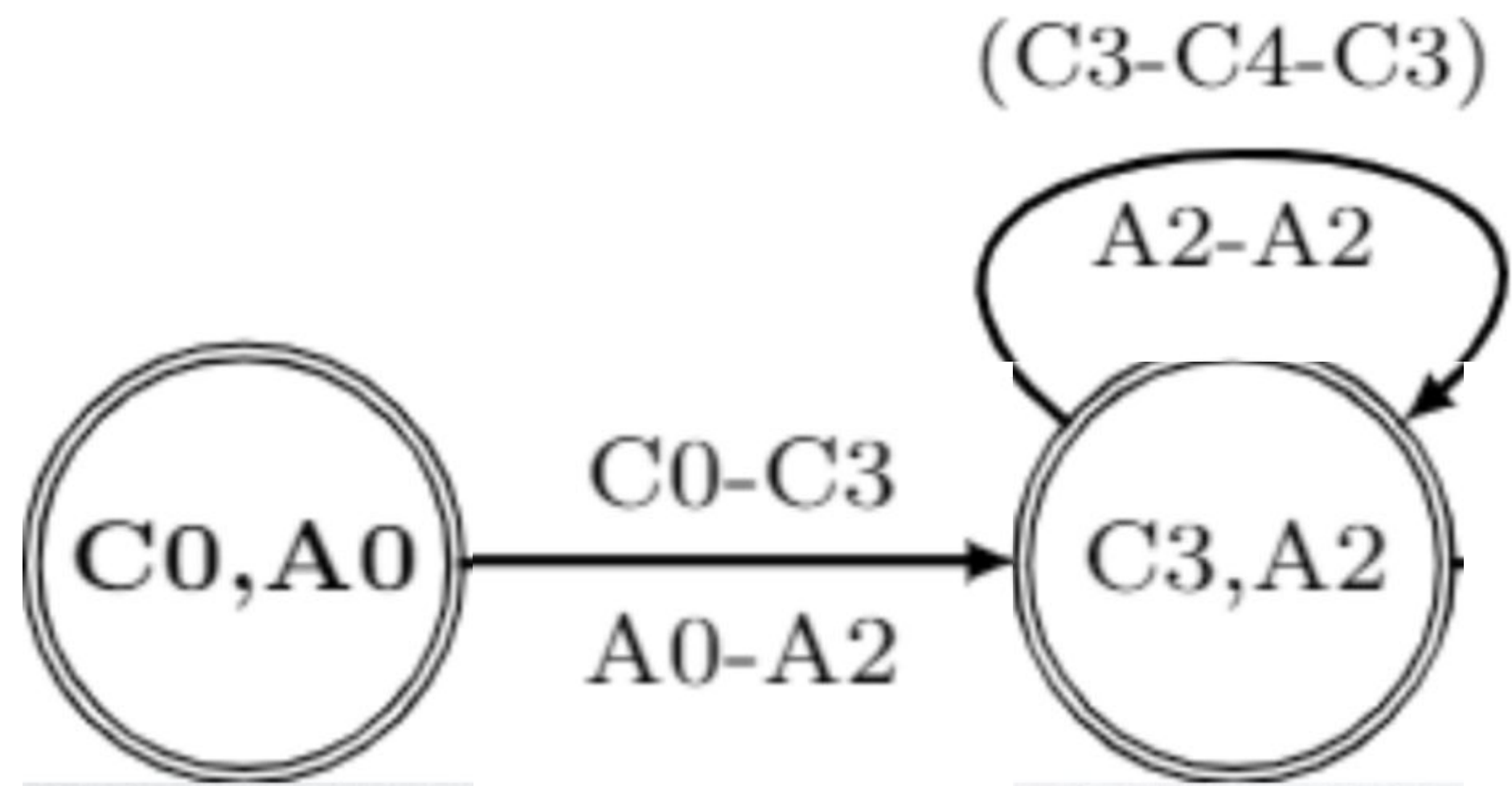
# Incremental Construction of the Product CFG

Use off-the-shelf invariant inference algorithms to infer affine, equality and inequality invariants on bitvectors and memory states



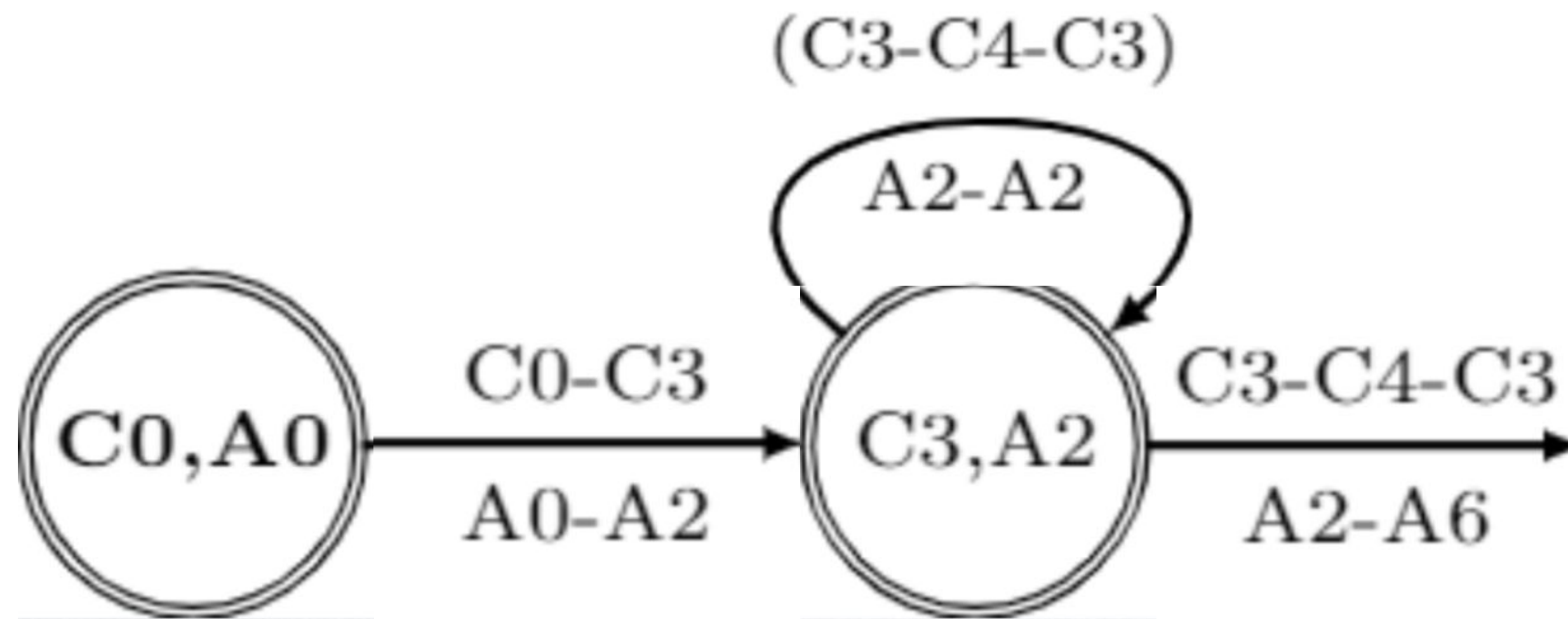
Infer Invariants at  
 $(C3, A2)$

# Incremental Construction of the Product CFG

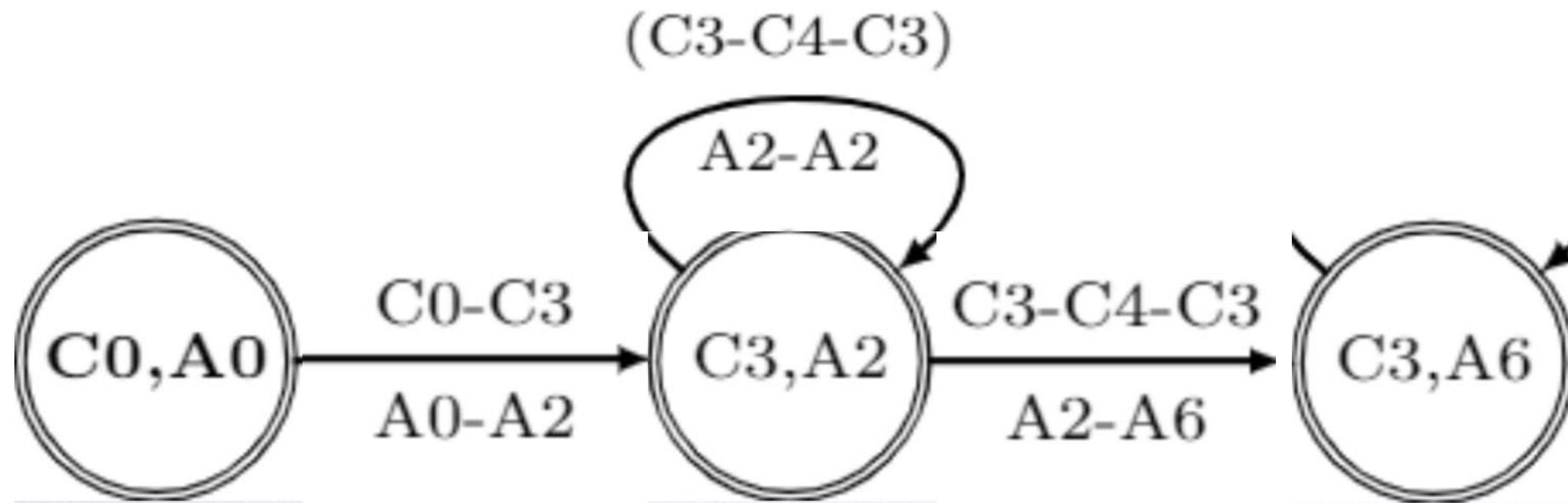


Relax Invariants  
at  $(C3, A2)$

# Incremental Construction of the Product CFG



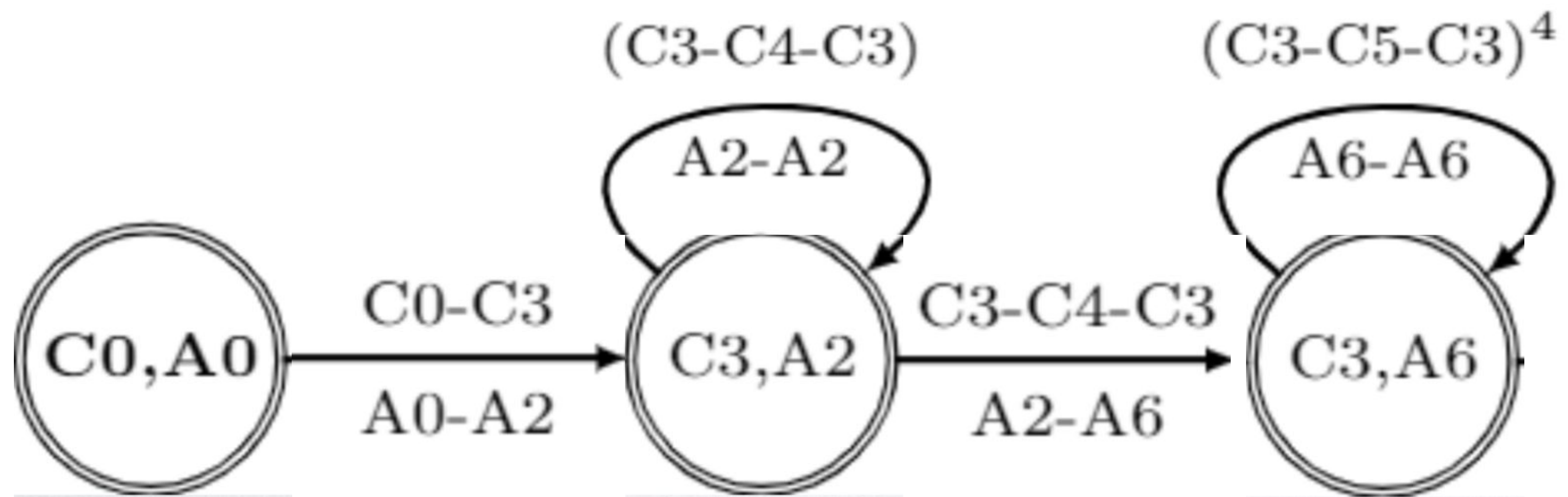
# Incremental Construction of the Product CFG



Infer Invariants at  
 $(C_3, A_6)$

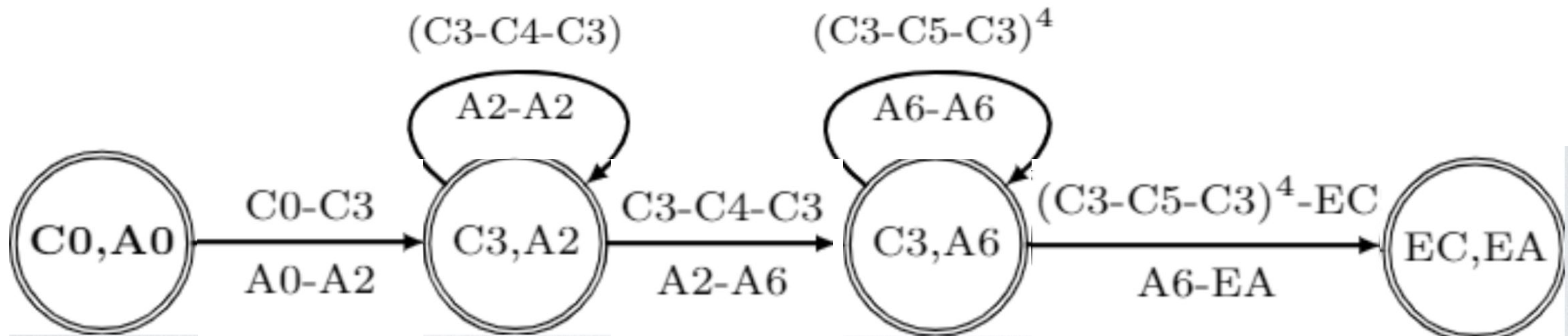


# Incremental Construction of the Product CFG



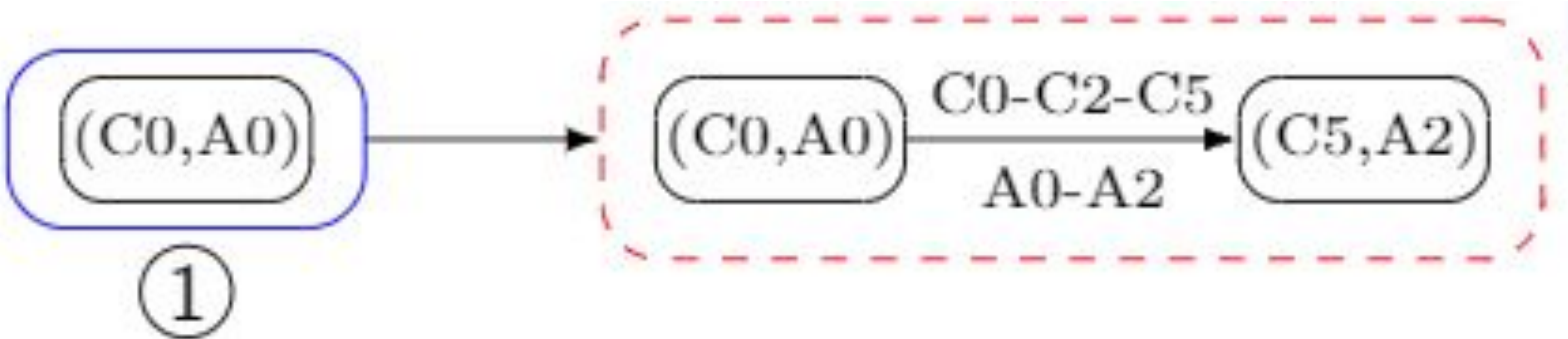
Relax Invariants  
at  $(C_3, A_6)$

# Incremental Construction of the Product CFG

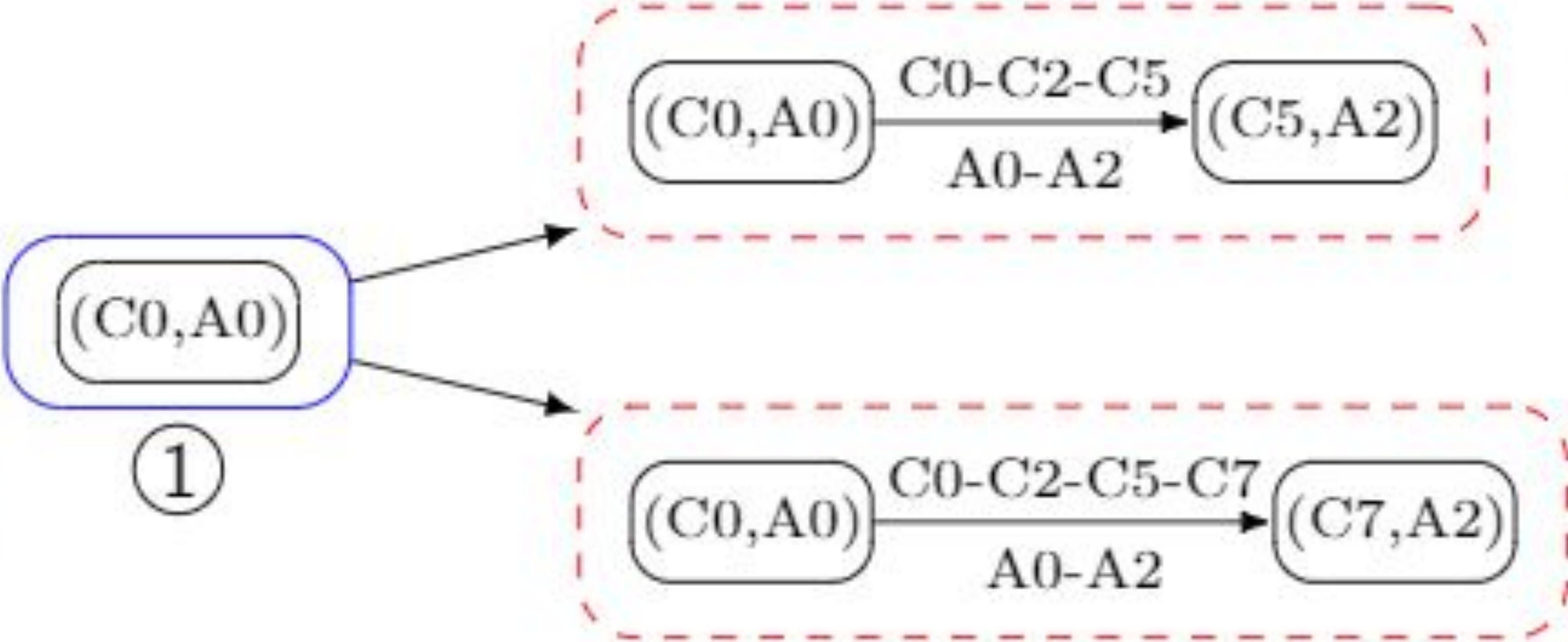


Check equivalence of  
return values under  
inferred invariants

# SEARCH SPACE

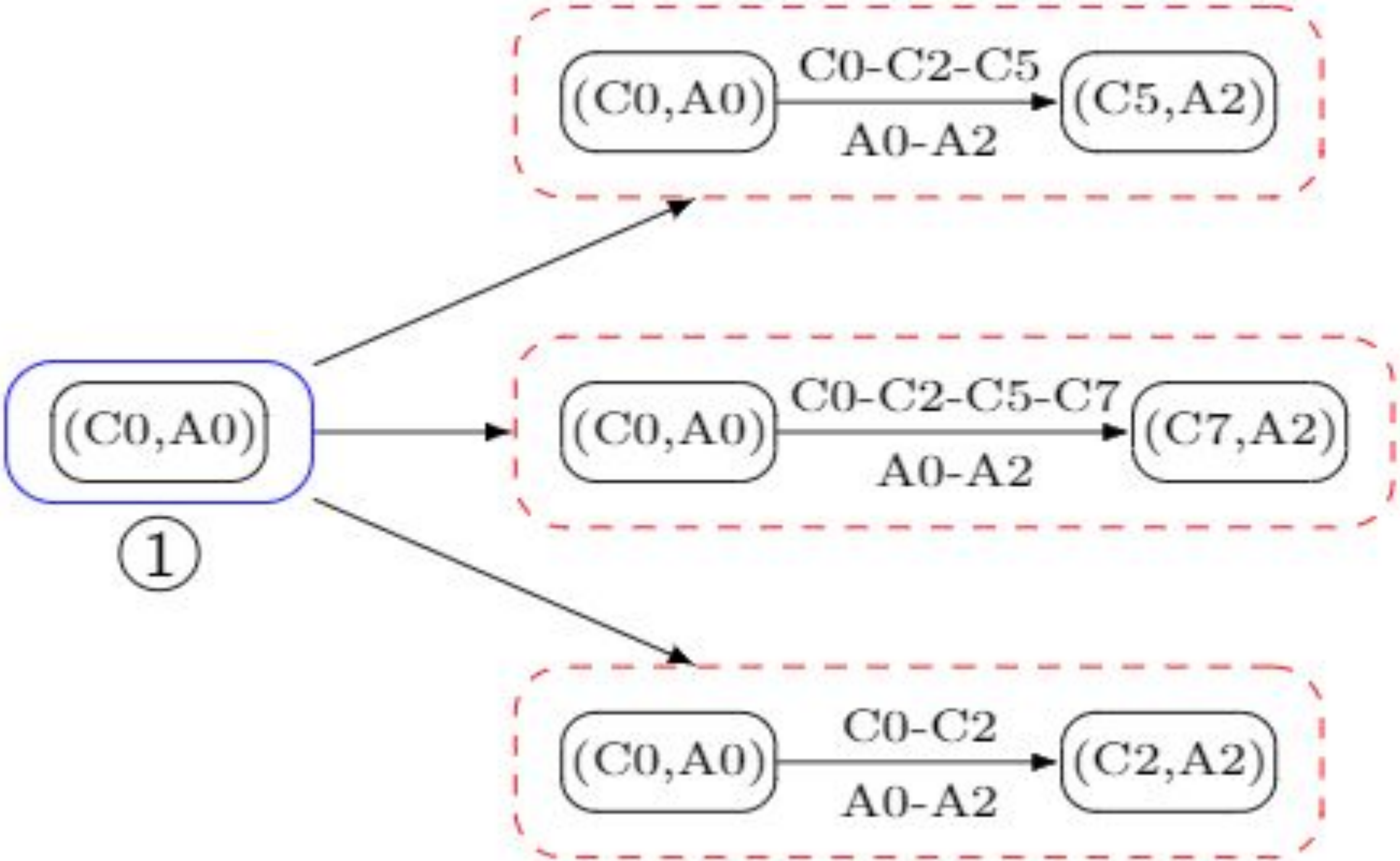


# SEARCH SPACE



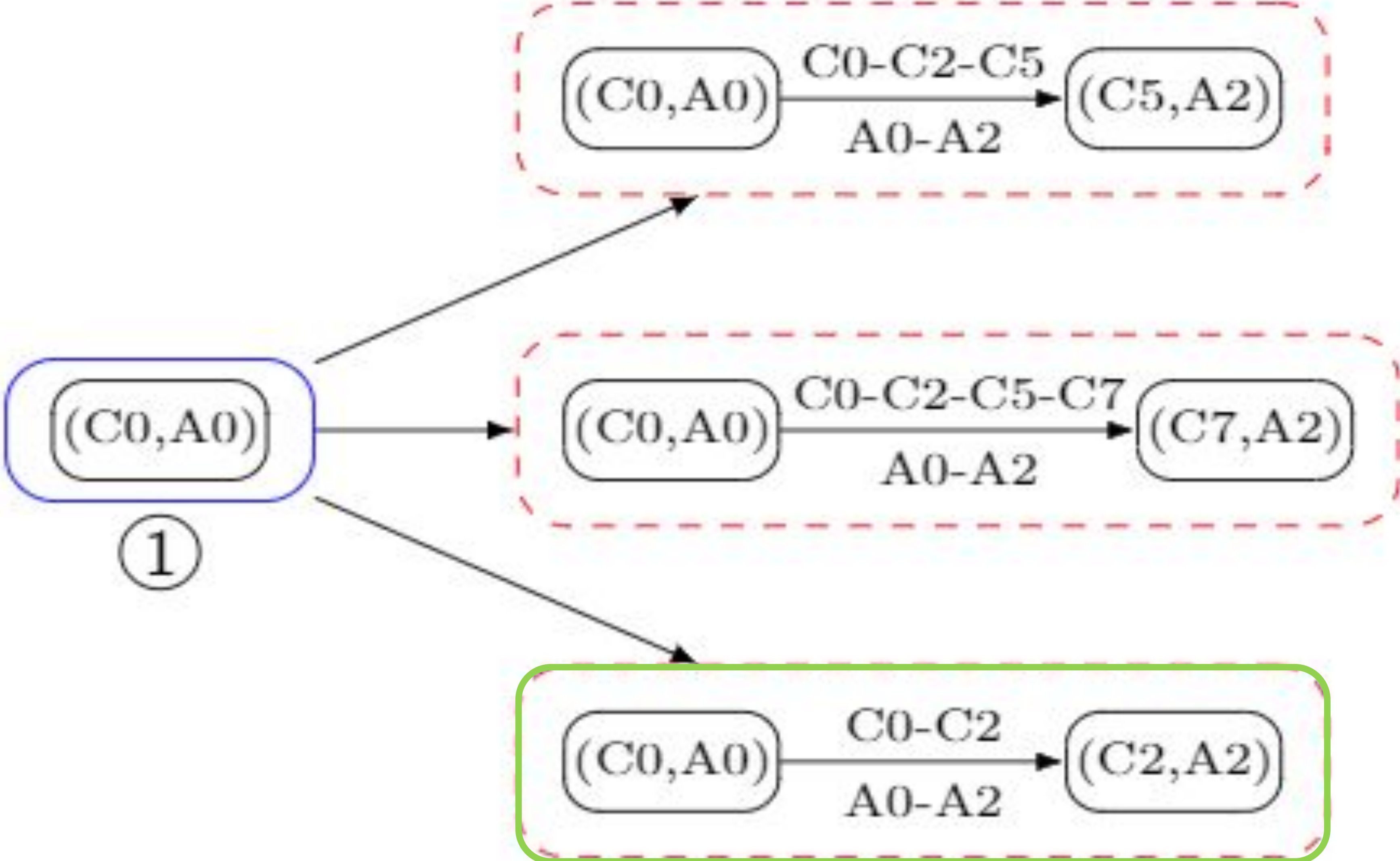


# SEARCH SPACE

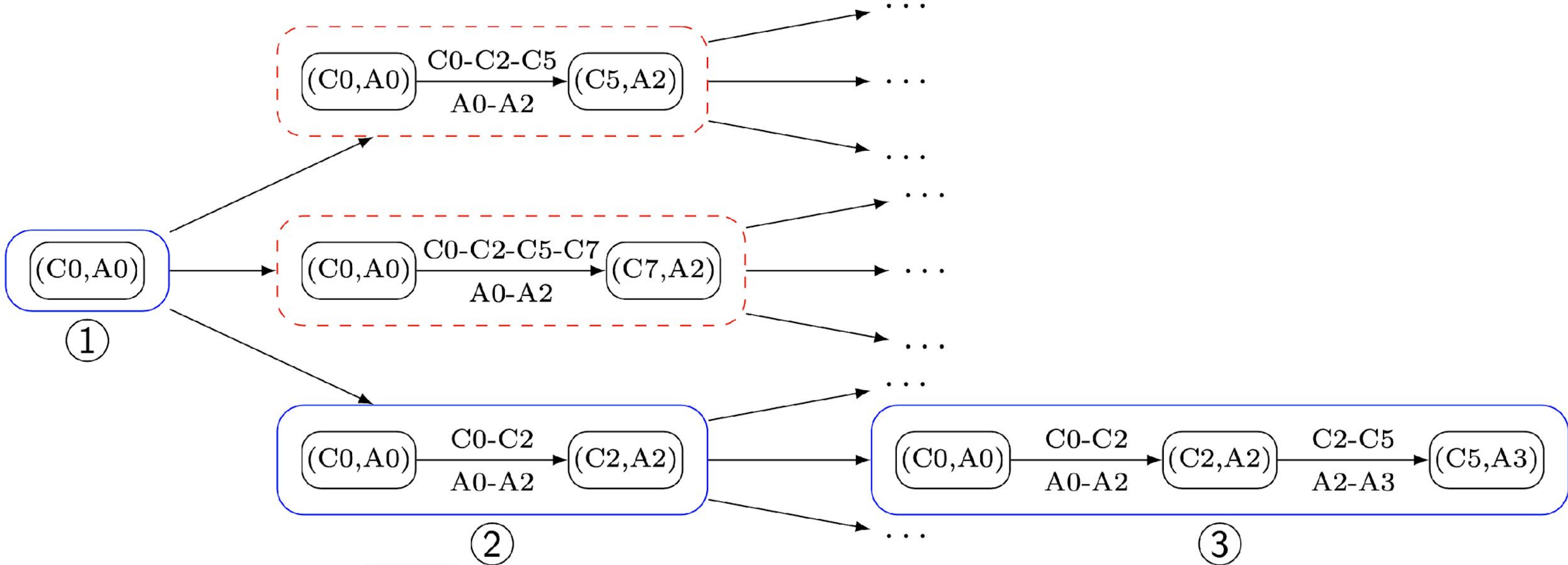




# SEARCH SPACE



# SEARCH SPACE

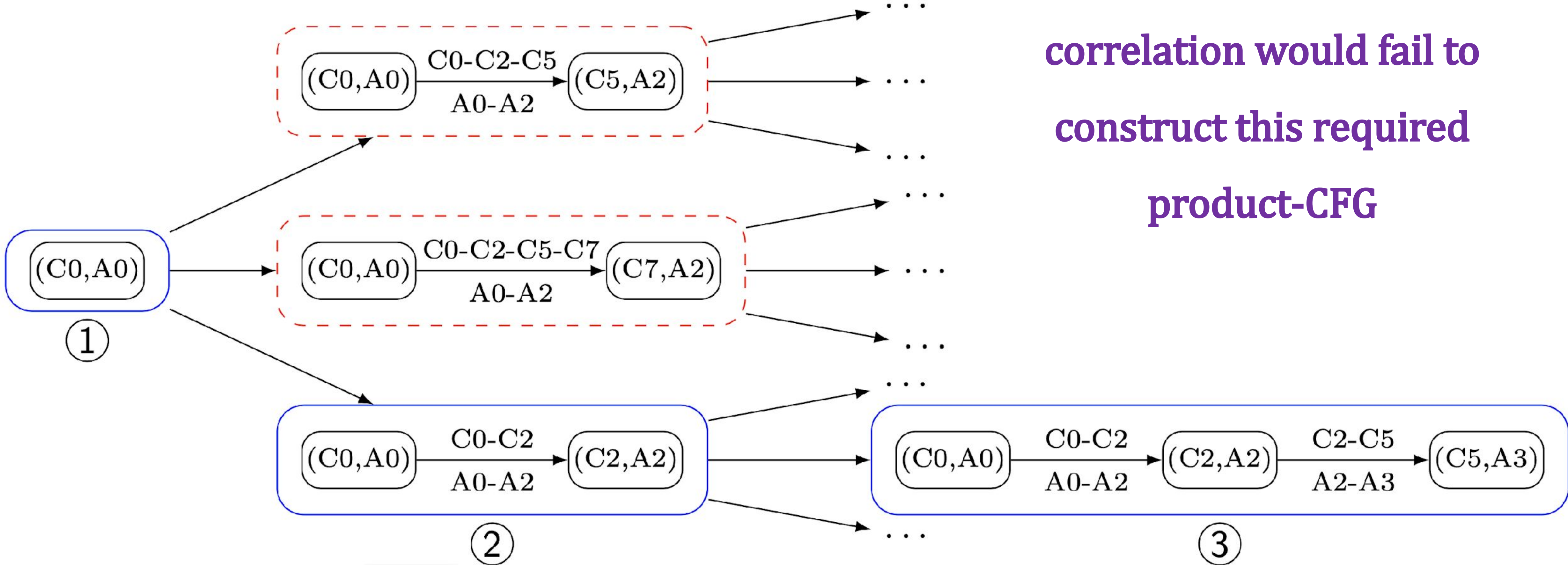


**Exhaustive search would take years to compute equivalence**



# SEARCH SPACE

Prior work on data driven correlation would fail to construct this required product-CFG



Exhaustive search would take years to compute equivalence

# Counterexamples

During invariant inference, we make potential GUESSES for invariants. We try to prove a GUESS using an SMT Solver.

- If the GUESS is provable, we have found an invariant.
- If not, the SMT solver returns a counterexample

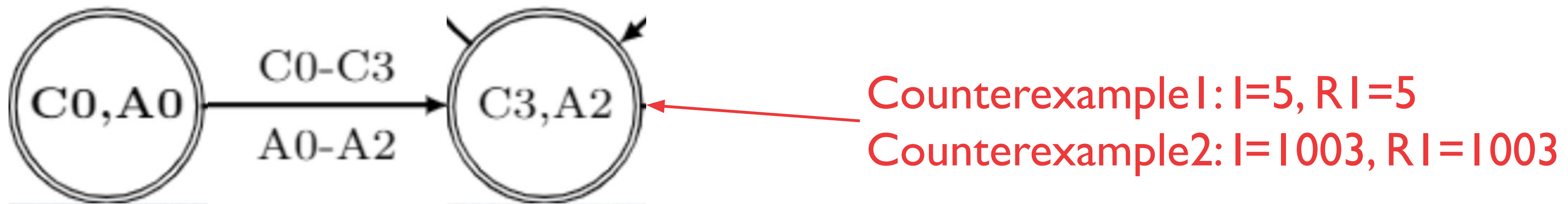


Infer Invariants at  
(C3, A2)

# Counterexamples

A counterexample at a node is a potential concrete machine state that may occur at that particular node during execution.

The concrete state would involve valuations for (related) variables of both C and A.

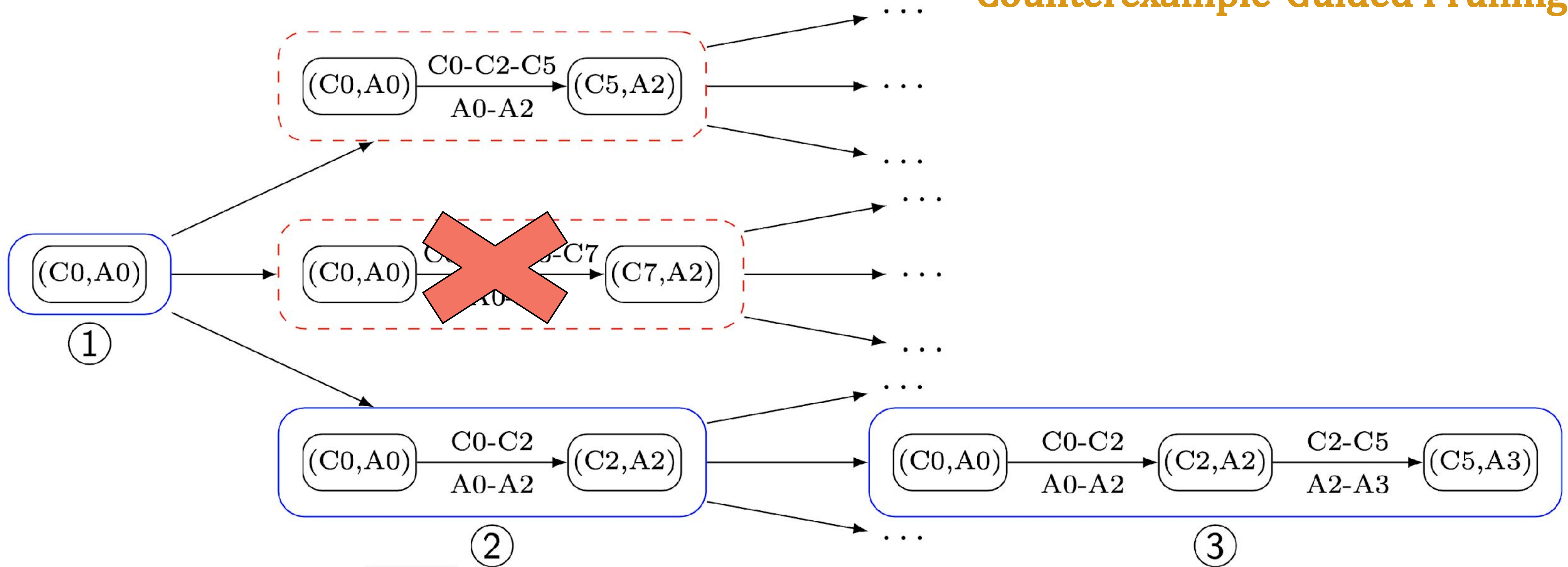


Infer Invariants at  
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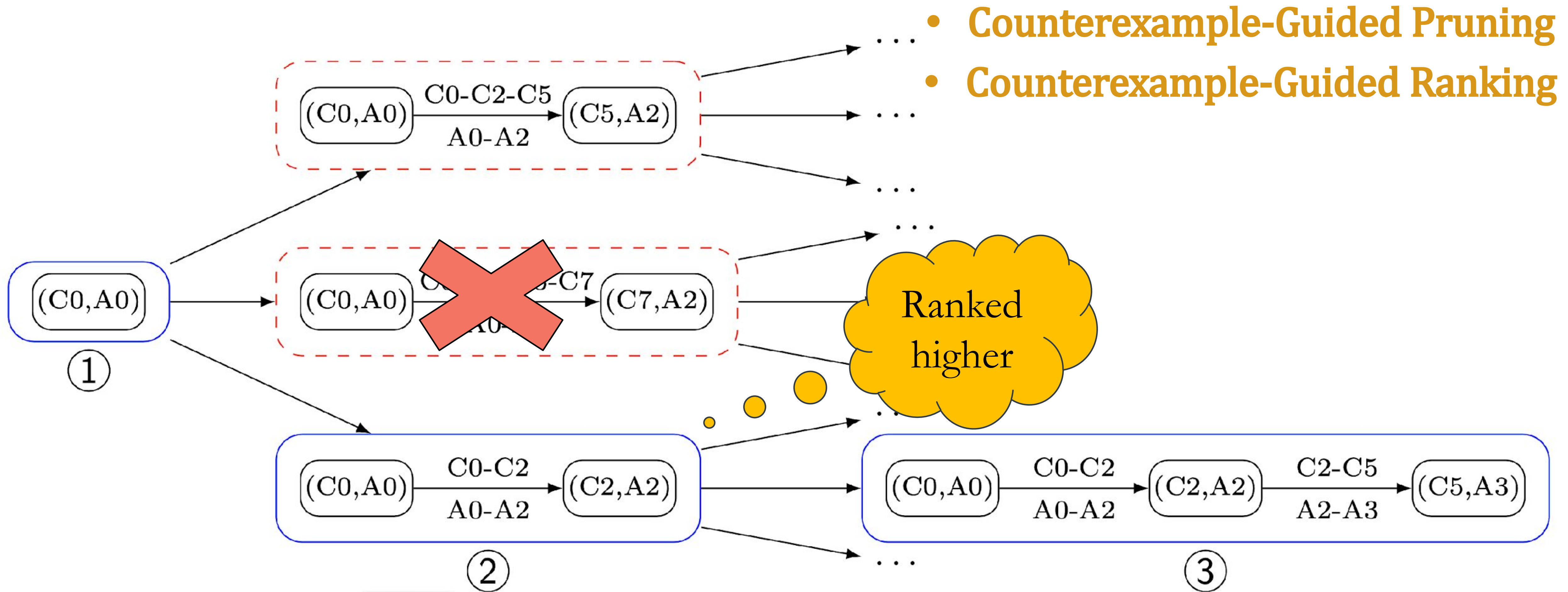


# COUNTEREXAMPLE GUIDED BEST-FIRST SEARCH

- Counterexample-Guided Pruning



# COUNTEREXAMPLE GUIDED BEST-FIRST SEARCH



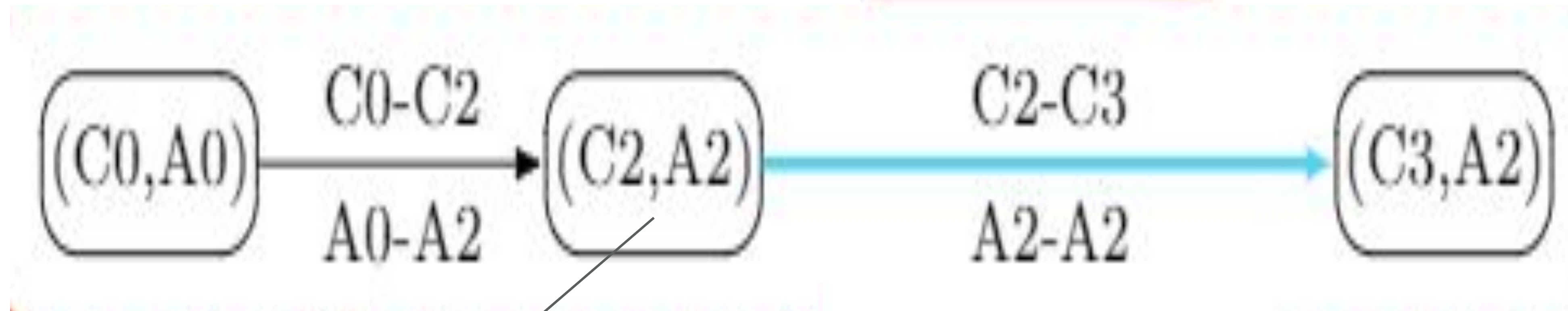
Counterexample Guided Best-First Search

. Counterexample Guided Pruning



# COUNTEREXAMPLE EXECUTION

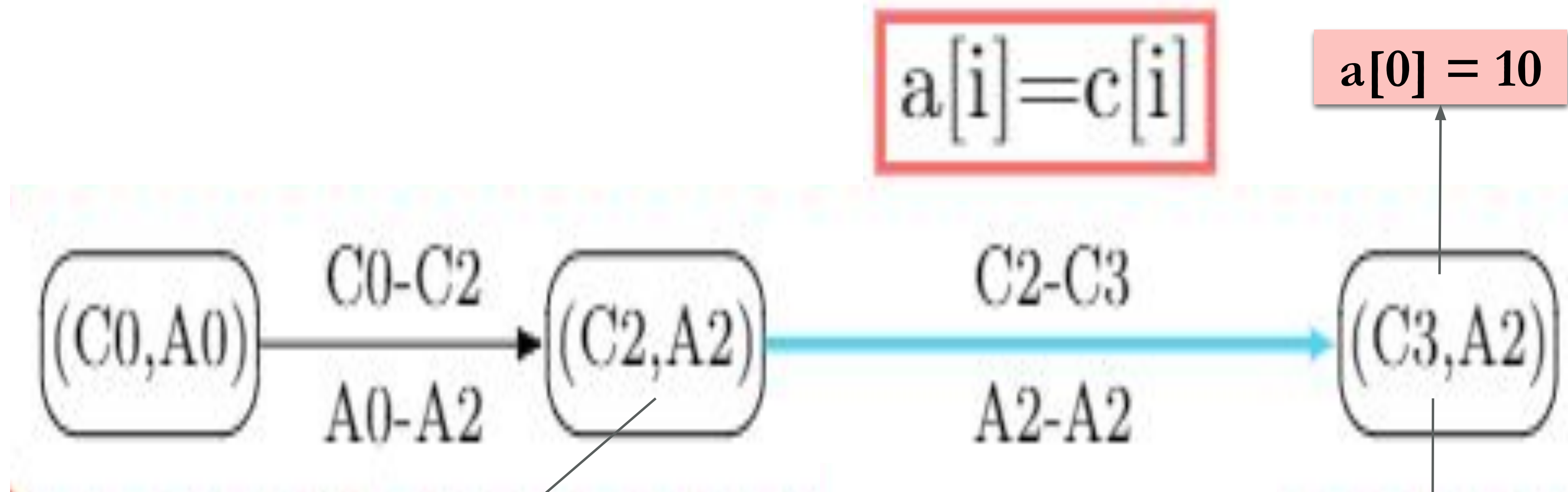
$$a[i] = c[i]$$



$$a[r1] = b[r1]$$

$i=0, r1=0,$   
 $b[0] = 5, c[0] = 10$

# COUNTEREXAMPLE EXECUTION



$i=0, r1=0,$   
 $b[0] = 5, c[0] = 10$

$$a[r1] = b[r1]$$

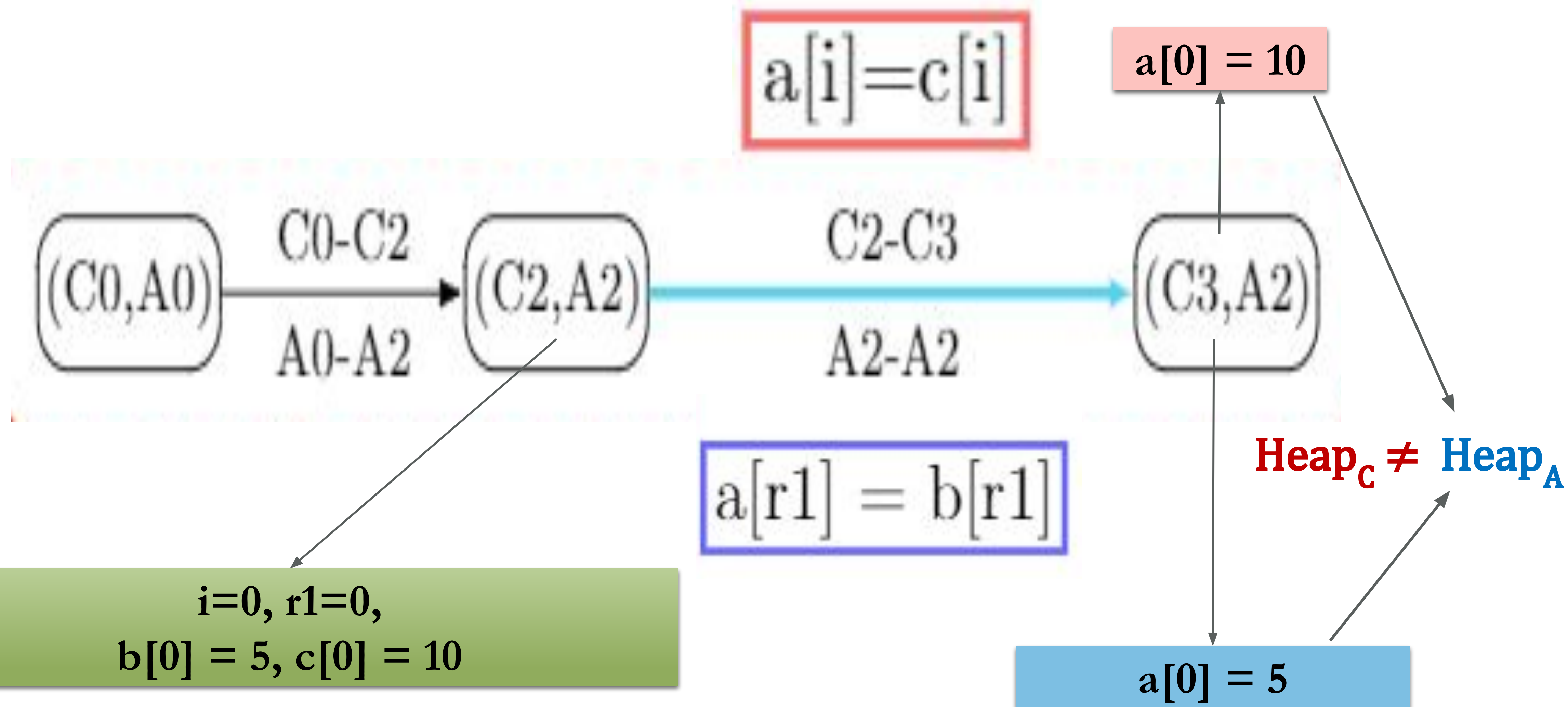
$$a[i] = c[i]$$

$$a[0] = 10$$

$$a[0] = 5$$

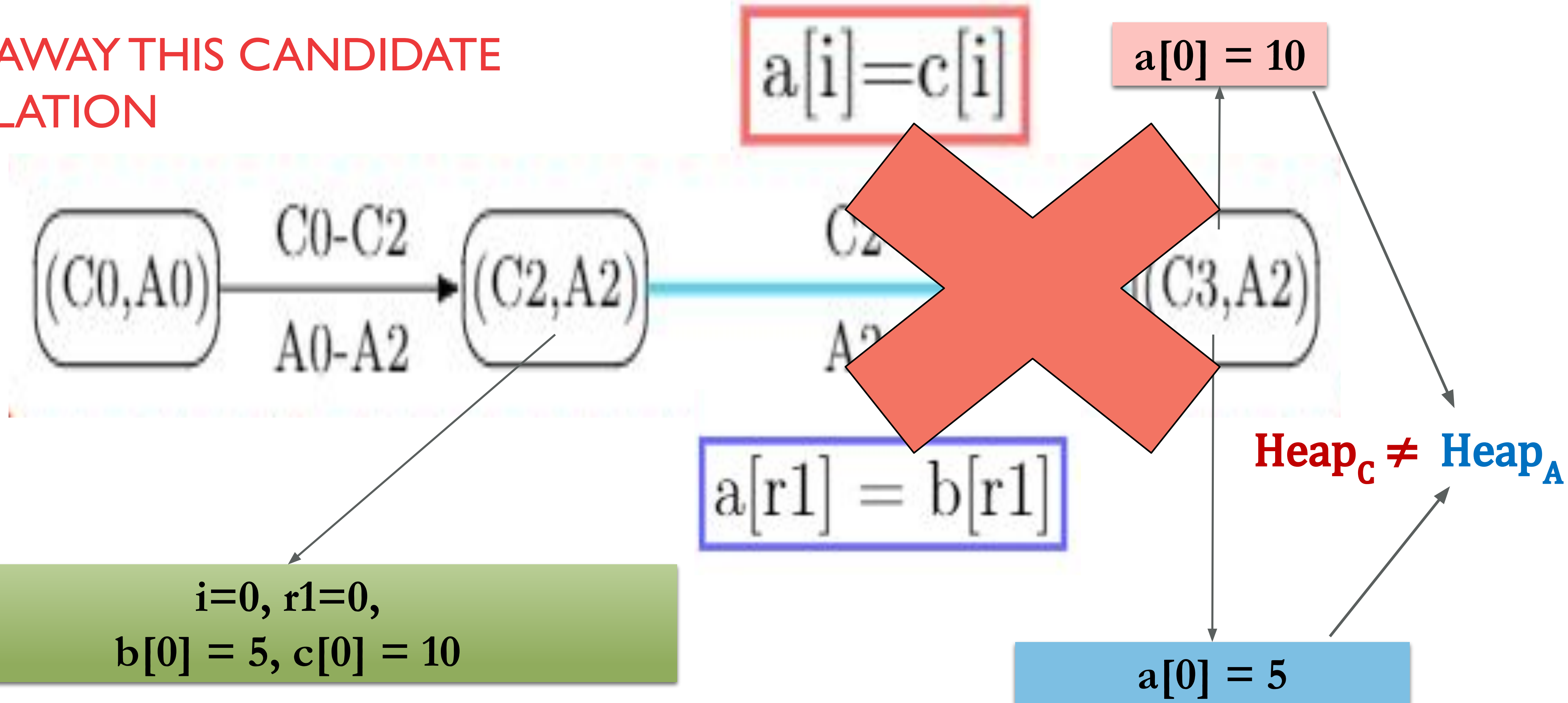


# Counterexample Guided Pruning



# Counterexample Guided Pruning

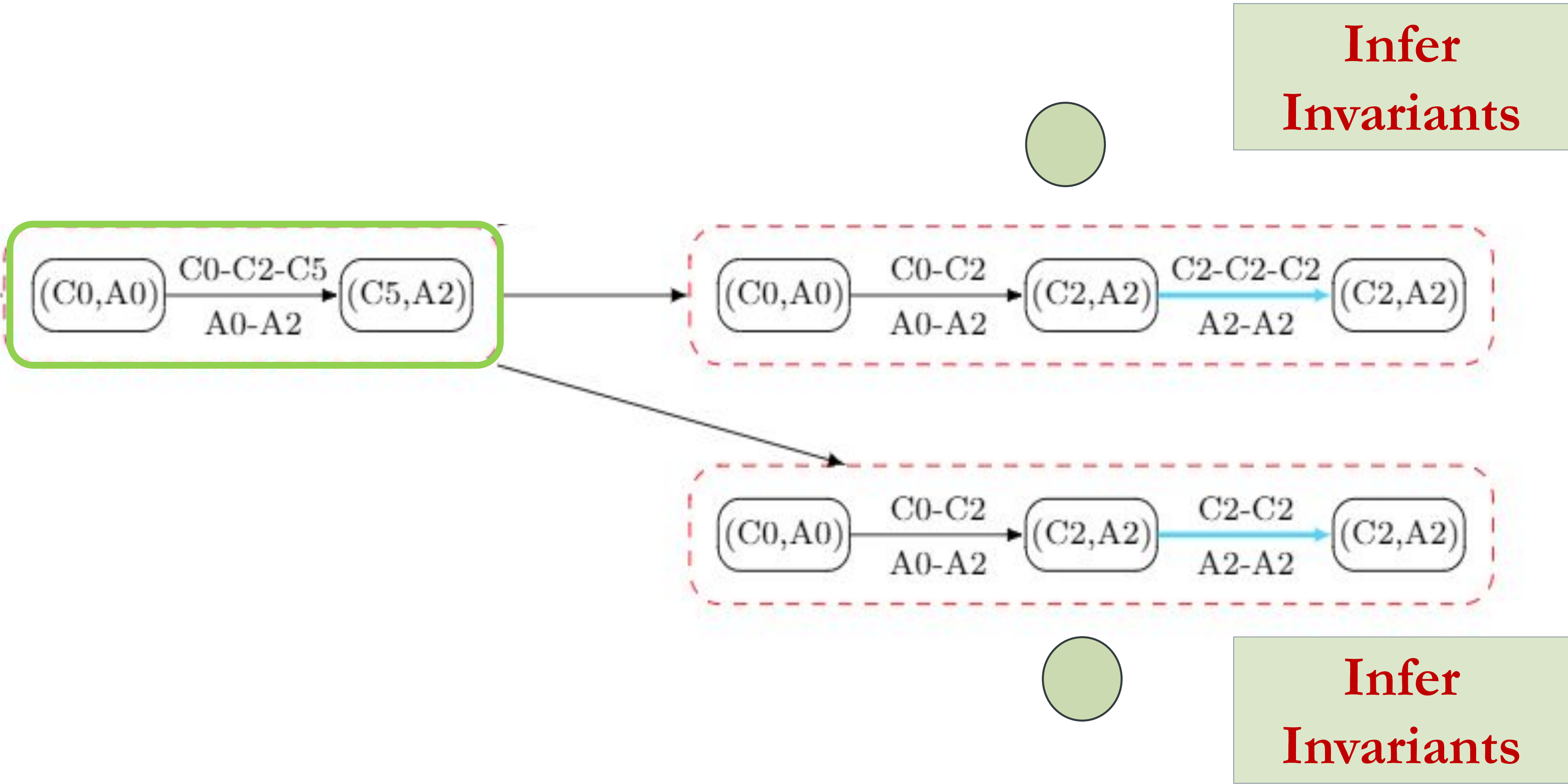
PRUNE AWAY THIS CANDIDATE  
CORRELATION



# Counterexample Guided Best-First Search

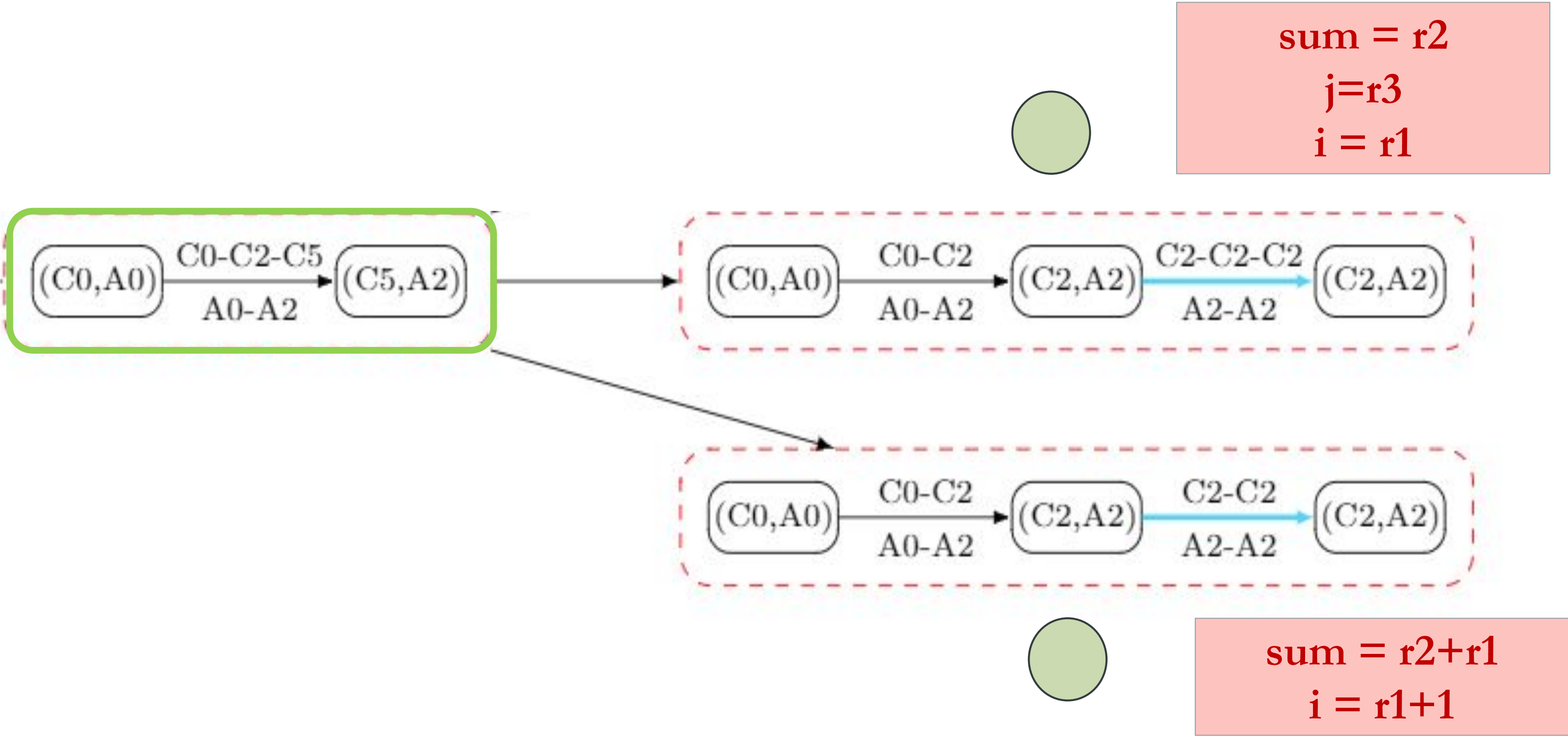
- . Counterexample Guided Pruning
- . Counterexample Guided Ranking

# Infer Invariant Covers for Executed Counterexamples



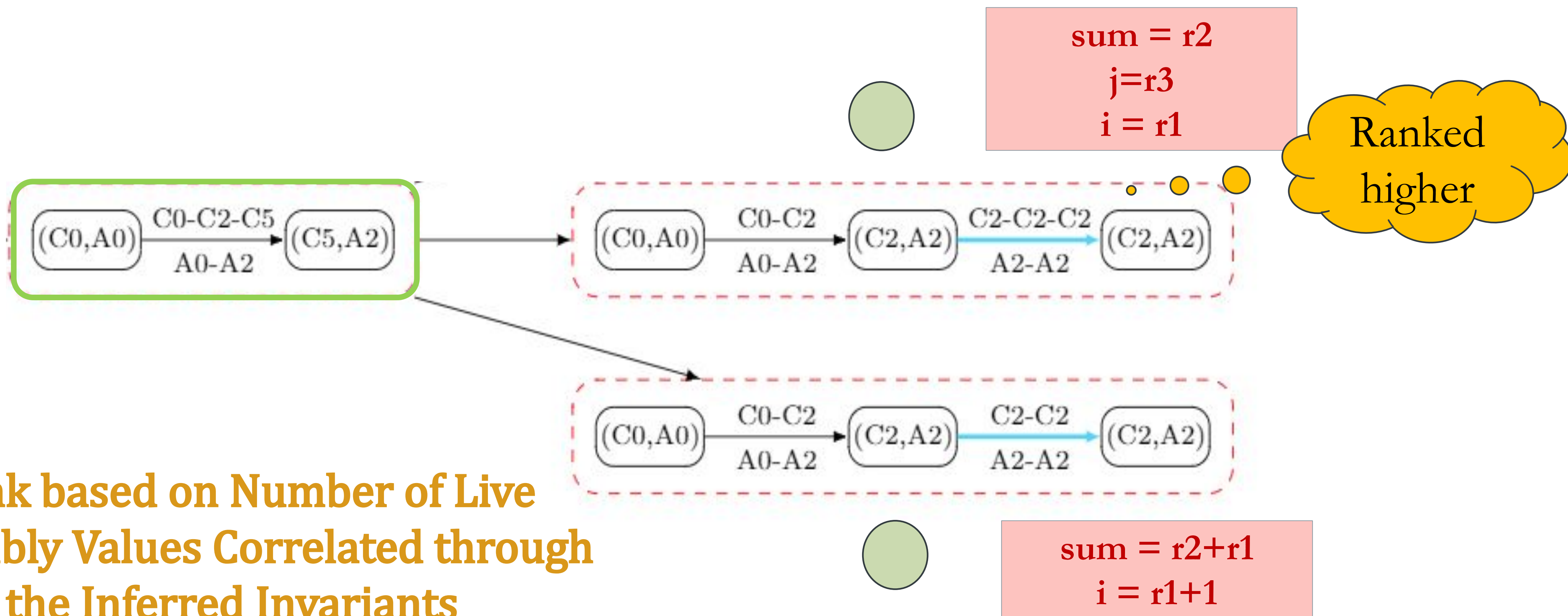


# Infer Invariant Covers for Executed Counterexamples



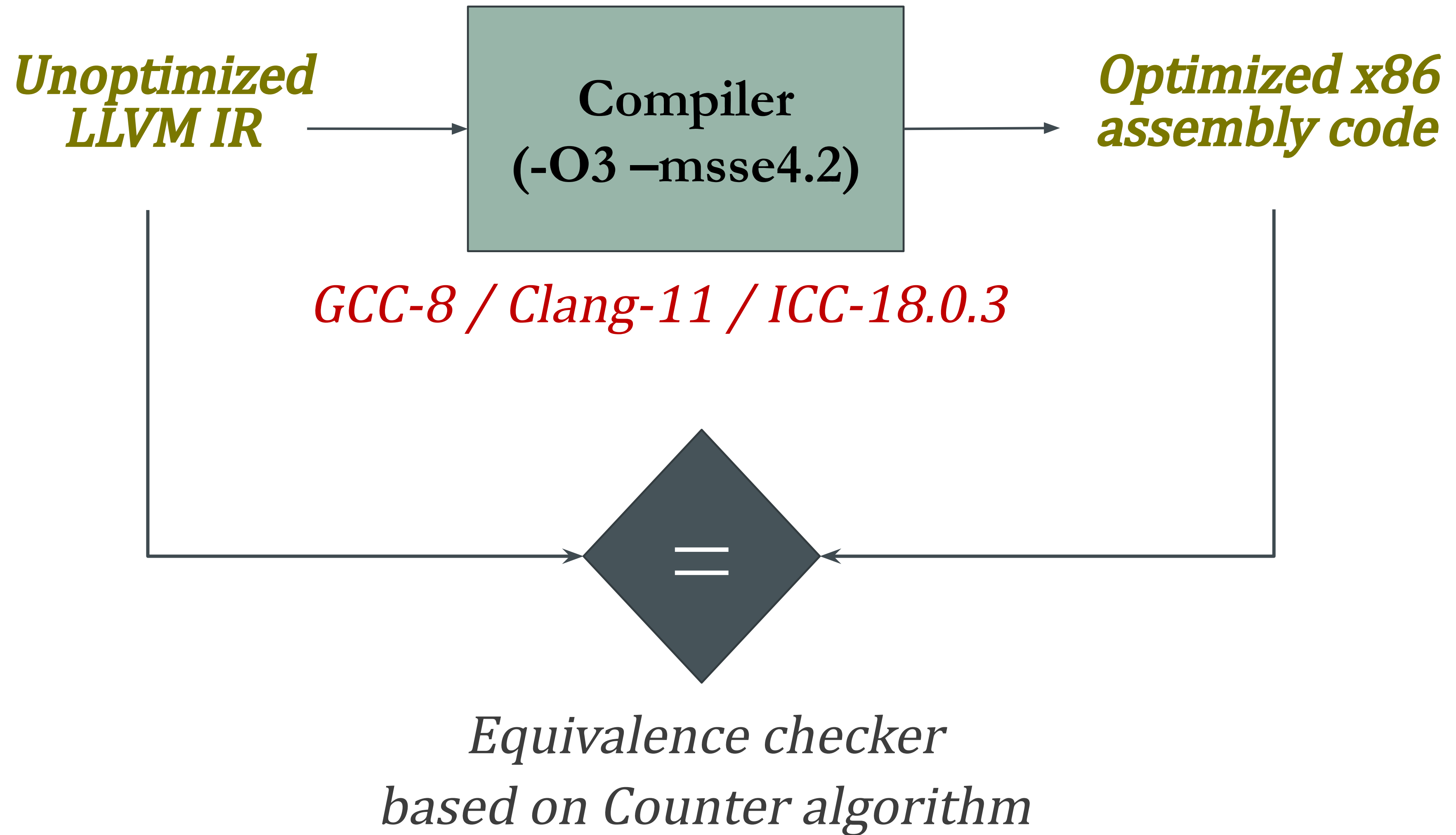


# Infer Invariant Covers for Executed Counterexamples



Rank based on Number of Live Assembly Values Correlated through the Inferred Invariants

# Counter Evaluation



# Counter Evaluation

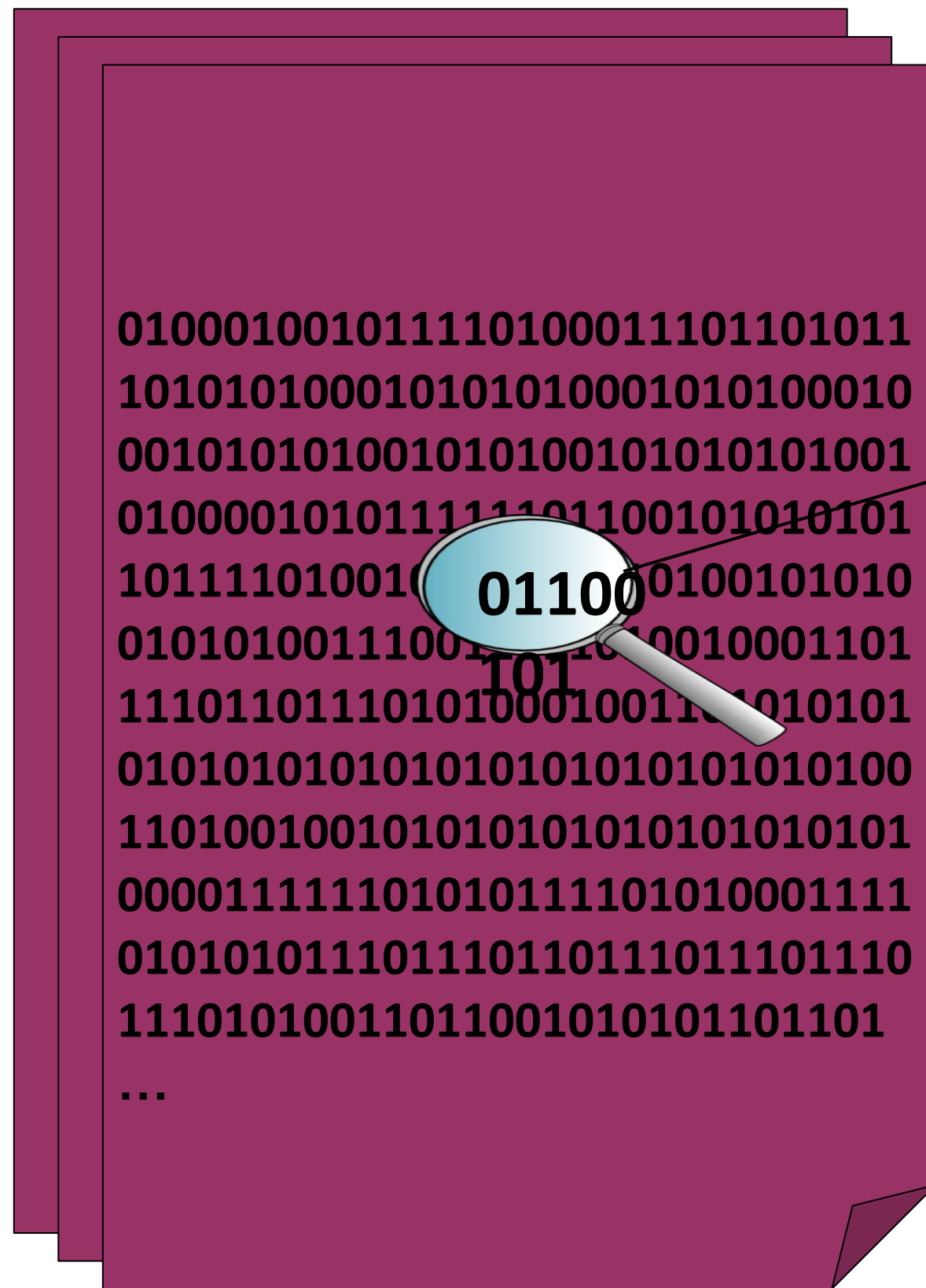
- TSVC Benchmarks : TestSuite for Vectorizing Compilers
  - 208 function-compiler pairs tested
  - **175 function-compiler pairs pass**

# Counter Evaluation

- TSVC Benchmarks : TestSuite for Vectorizing Compilers
  - 208 function-compiler pairs tested
  - **175 function-compiler pairs pass**
- LORE Repository for Loop Nests
  - **27 different vectorizable loop patterns, all pass**
  - 16 with multiple potentially-nested loops
  - 6 where multiple control flow paths in the loop body
  - 17 use multi-dimensional arrays

# Peephole Superoptimization

## Step I



Harvest instruction sequences that can potentially be optimized.  
Canonicalize and store them.

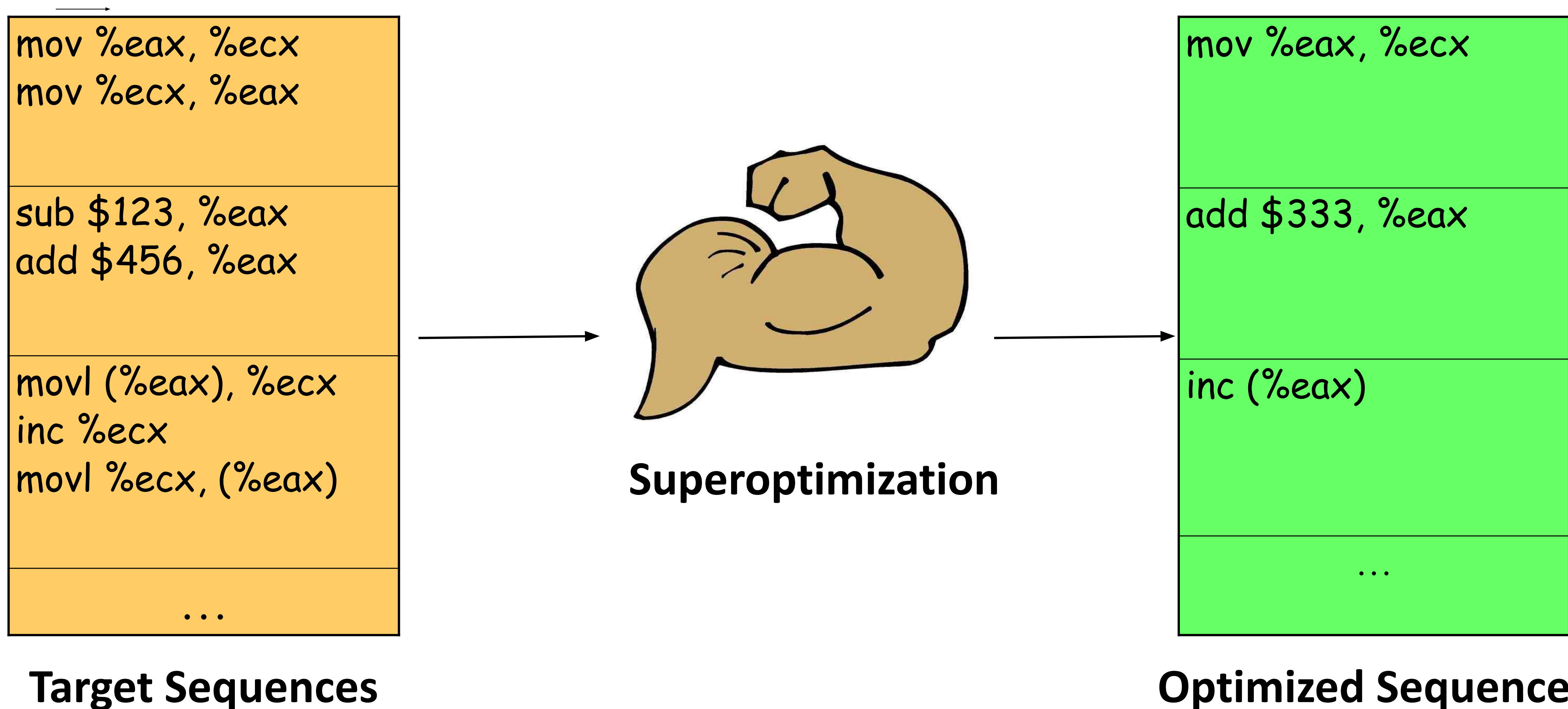
<code>mov %eax, %ecx mov %ecx, %eax</code>
<code>sub \$123, %eax add \$456, %eax</code>
<code>movl (%eax), %ecx inc %ecx movl %ecx, (%eax)</code>
...

**Target Sequences**



# Peephole Superoptimization

## Step 2



# Peephole Superoptimization

## Step 3

<code>mov %eax, %ecx</code> <code>mov %ecx, %eax</code>	<code>mov %eax, %ecx</code>
<code>sub \$123, %eax</code> <code>add \$456, %eax</code>	<code>add \$333, %eax</code>
<code>movl (%eax), %ecx</code> <code>inc %ecx</code> <code>movl %ecx, (%eax)</code>	<code>inc (%eax)</code>
...	...

**Table of Peephole Optimizations**

# Why is this nowhere near enough?

- Invariants are not captured, e.g.,  $x = \text{constant}$

pattern	replacement
//reg1 is known to be a constant C0 mov reg1, reg2 add \$C1, reg2	mov \$(C0+C1), reg2



# Why is this nowhere near enough?

- Local Memory Usage in the Pattern is *not* Modeled

pattern	replacement
<pre>char x[42]; ... printf(x);</pre>	<pre>sub \$42, %esp ... printf(%esp)</pre>



# Why is this nowhere near enough?

- Local Memory Usage in the Replacement is *not* Modeled

pattern

```
if (x == 0) {  
  y = 42;  
} else if (x == 1) {  
  y = ...;  
} else if (x = ...) {  
  y = ...  
} ...
```

replacement

```
y = PrecomputedArray[x];
```





# Why is this nowhere near enough?

- No preservation of debugging information

pattern	unoptimized	optimized
sum += a[i]; sum += a[i+1]; ... sum += a[i+7];	addl a[i], reg addl a[i+1], reg ... addl a[i+7], reg	psubb %mm0, %mm0 psadbw &a[i], %mm0 movd %mm0, reg

Can correlate reg with sum  
after every instruction  
Done by compiler  
developers

A superoptimized  
implementation erases this  
information.  
Can reconstruct! [CGO22]

# Serious?

- Aliasing information is not captured, e.g., heap access vs. stack access
- Invariants are not captured, e.g.,  $x = \text{constant}$
- Loops are not supported
- Local Memory Usage is not supported

# Serious?

- Aliasing information is not captured, e.g., heap access vs. stack access
- Invariants are not captured, e.g.,  $x = \text{constant}$
- Loops are not supported
- Local Memory Usage is not supported



# Invariant Sketching

